

Simulation of the lidar returns from clouds with  
a Monte Carlo radiative transfer model

Chen Zhou

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# Background

- Clouds play an important role in weather and climate
  - Precipitation
  - Cloud-aerosol-radiation interactions
- **Uncertainties** on clouds are **large**
  - Cloud and climate change: clouds radiative effect **enhance global warming** by **0%-100%** (large uncertainty).
- Lidar are widely used to detect clouds
- Simulation of lidar signals from clouds would help understand the cloud properties, and improve the lidar retrieval algorithms.

# Simulation processes

- 1. Calculate **single scattering** properties.
- 2. Simulate the lidar signals from clouds with Monte Carlo radiative transfer model.  
(Why is a RTM needed? Multiple scattering.)
- 3. Compare with observations, and analyze the optical properties of ice clouds.

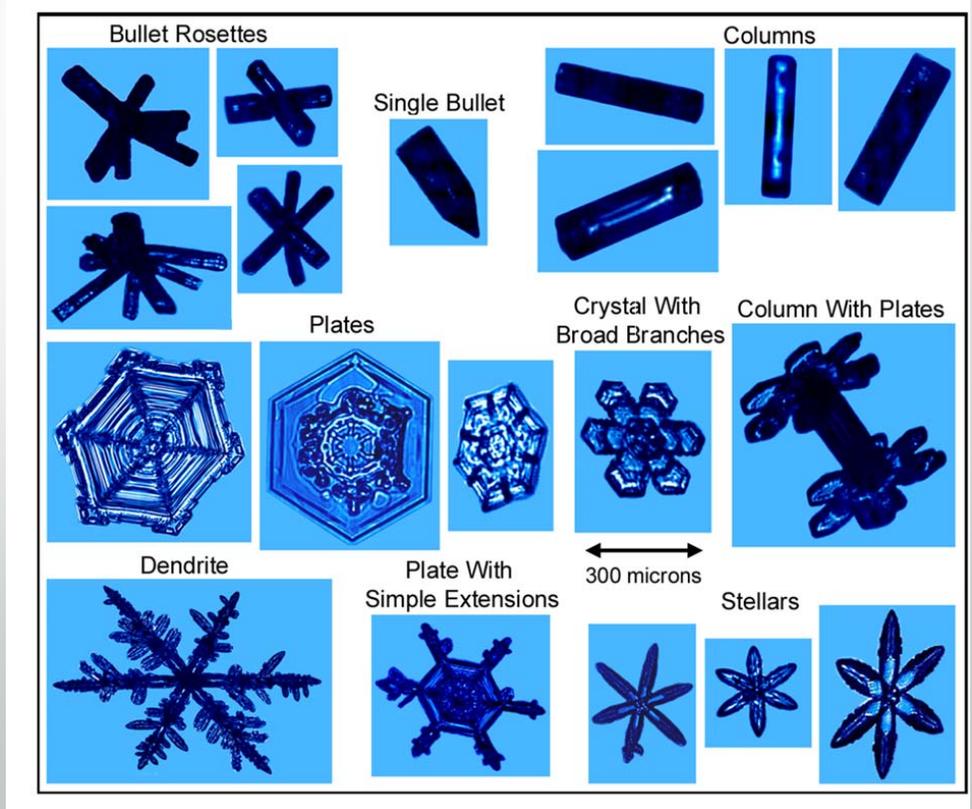
# Single scattering properties

Single scattering properties are especially important for lidar signals, especially for **backscattering properties**.

- 1. Shape of cloud particles
- 2. Orientation of cloud particles
- 3. Calculation with scattering models

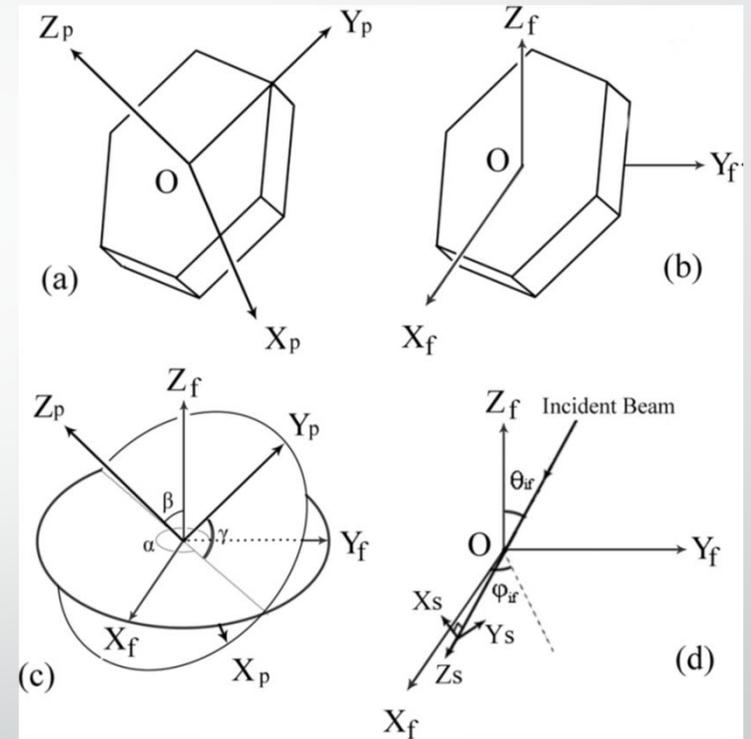
# Shape of cloud particles

- Water cloud droplets: spheres
  - Note: very larger ones might be considered as spheroids
- Ice clouds:
  - Columns
  - Plates
  - Column/plate aggregates
  - Bullet rosettes
  - Droxtels
  - Irregular (rough) shapes

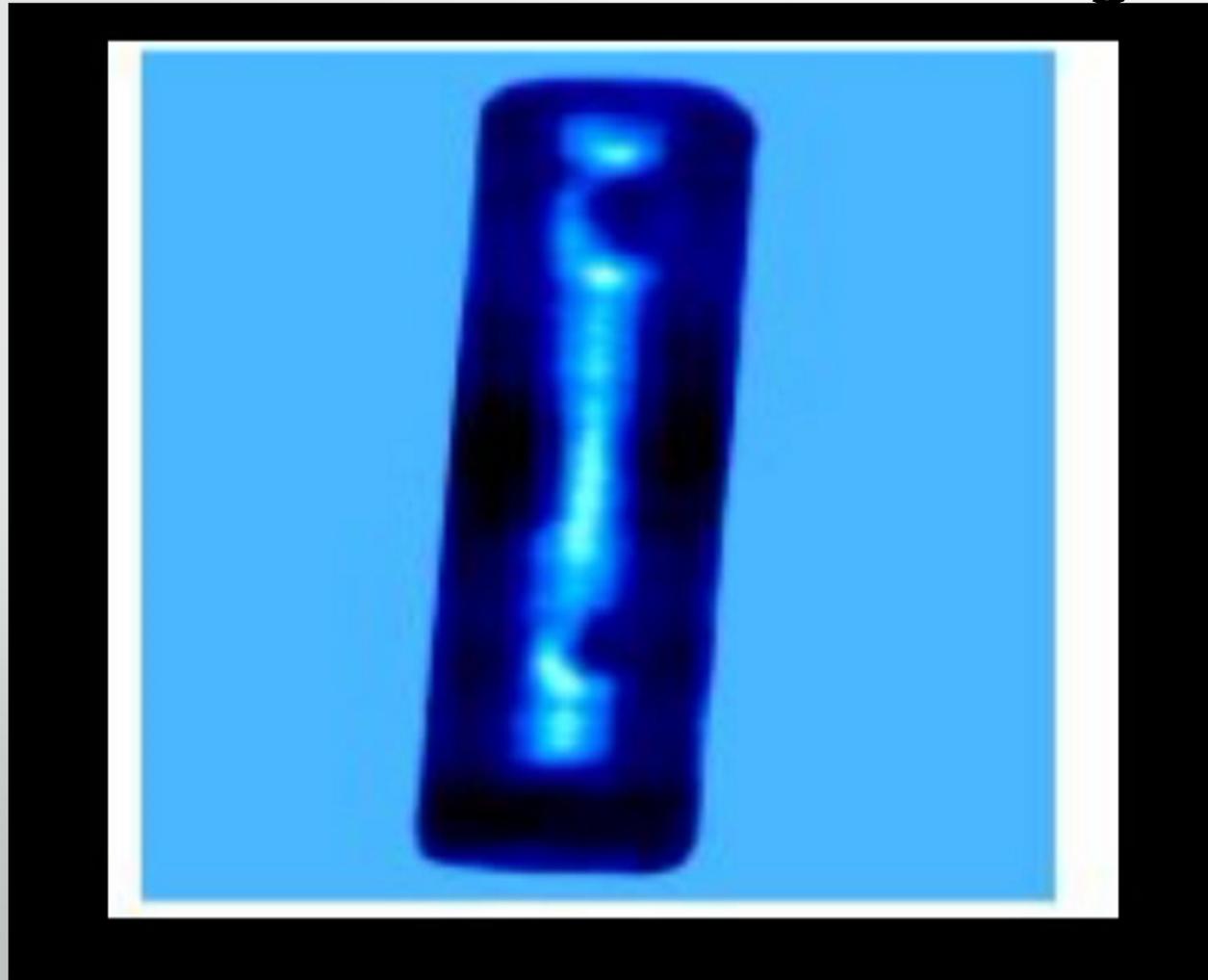


# Orientation of ice cloud particles

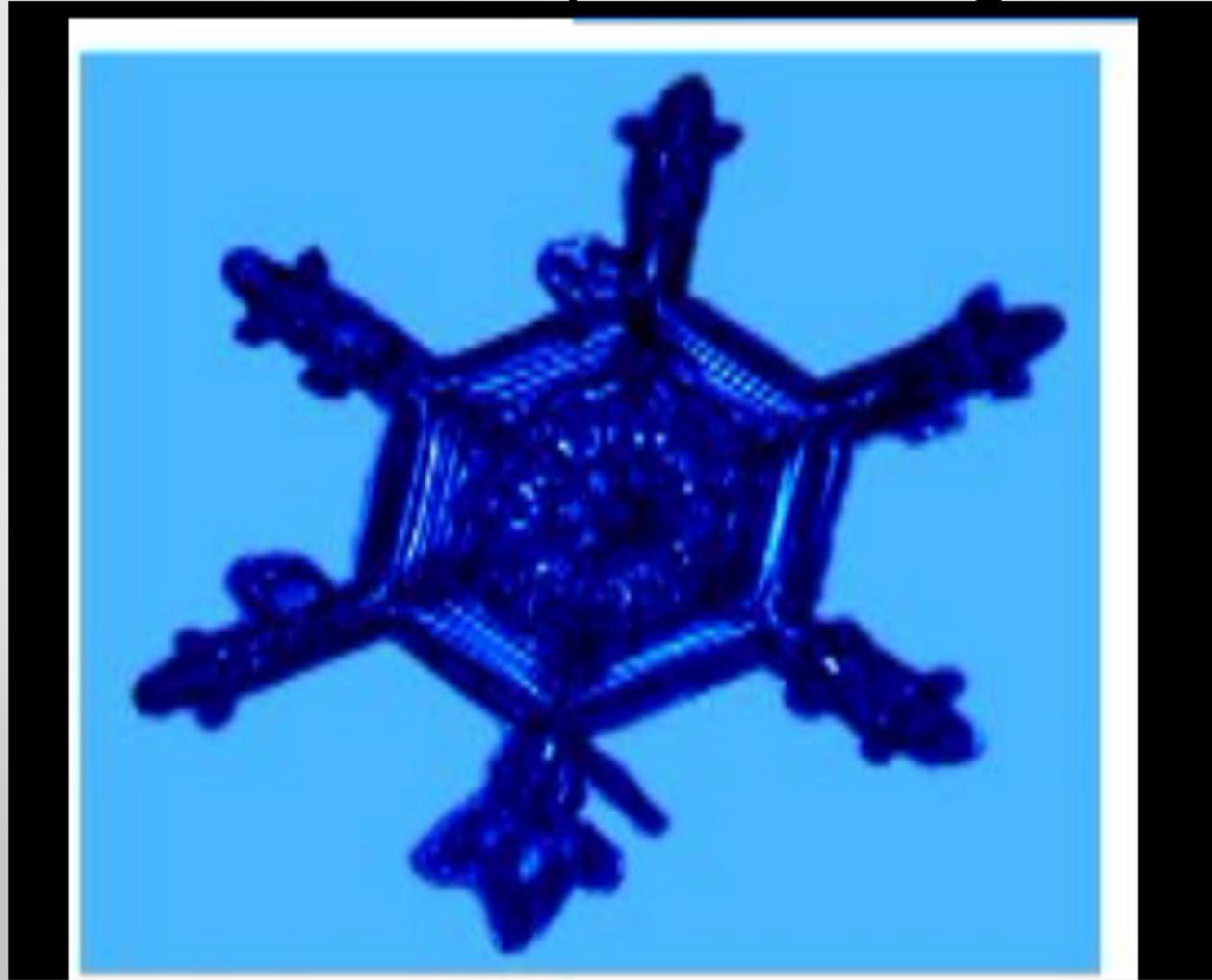
- Most radiative transfer models **assume** cloud particles are all **randomly oriented**.
- However, plates and columns might be **horizontally oriented** when they fall in fluid (air).



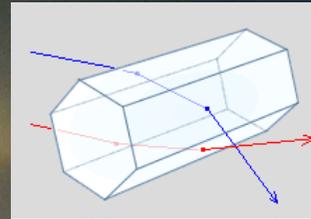
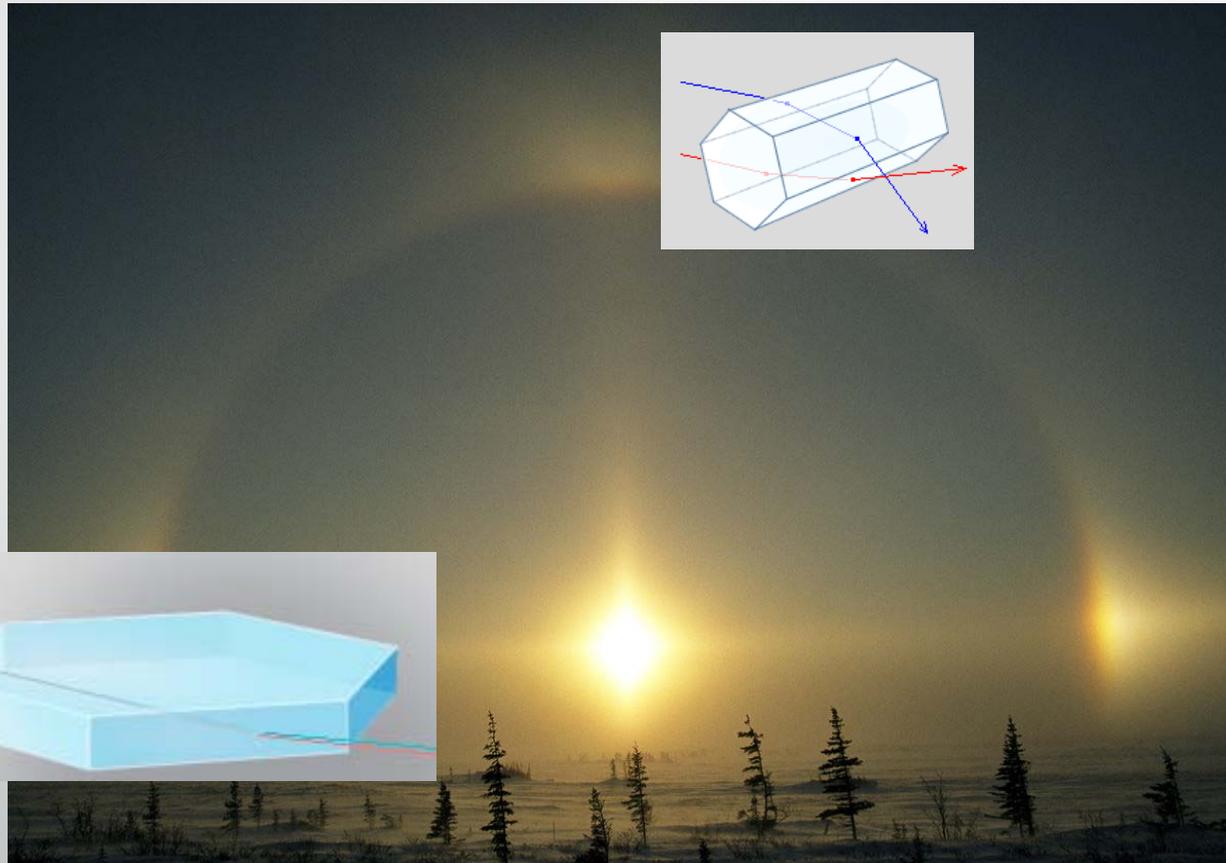
A simple experiment:  
orientation of a column falling in fluid



A simple experiment:  
orientation of a plate falling in fluid



# Sundog: Horizontally oriented particles



Tangent arc:  
Oriented columns



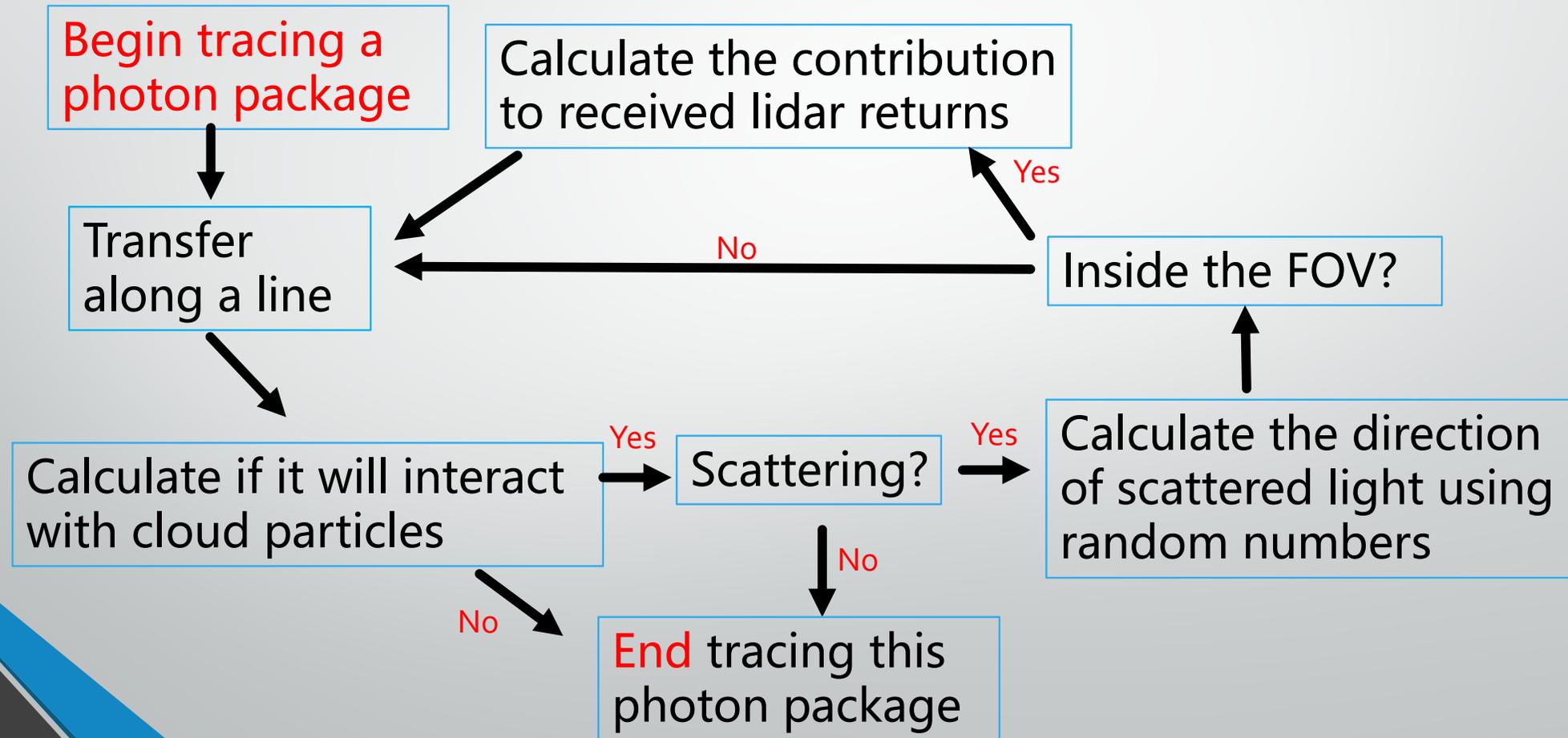
Sundog:  
Oriented plates

# Single scattering properties of ice cloud particles

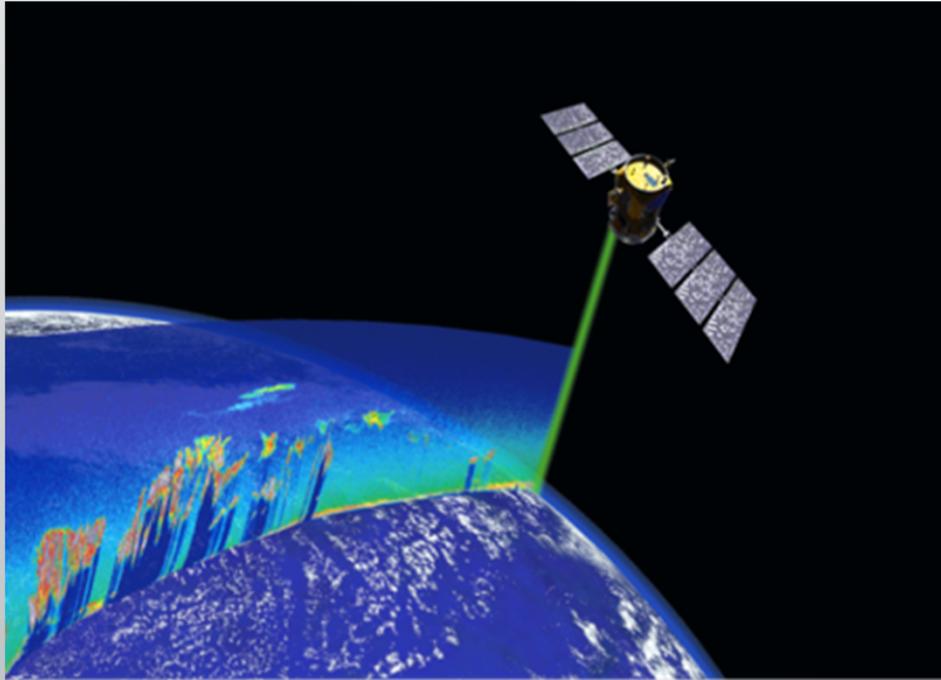
- 1. Spherical water cloud droplets  
Lorenz-Mie theory
- 2. Randomly oriented particles (including 6 habits)  
IGOM (Yang et al. 2005)  
Phase function  $\mathbf{P}=\mathbf{P}(\theta_s)$
- 3. Horizontally oriented plates and columns  
PGOH (Bi et al. 2011)  
Phase matrix  $\mathbf{P}=\mathbf{P}(\theta_{i'}, \varphi_{i'}, \theta_{s'}, \varphi_{s'})$

# Monte Carlo radiative transfer model

Simulate  $N$  photon packages ( $N=200$  million) , and then calculate their contribution to lidar returns.

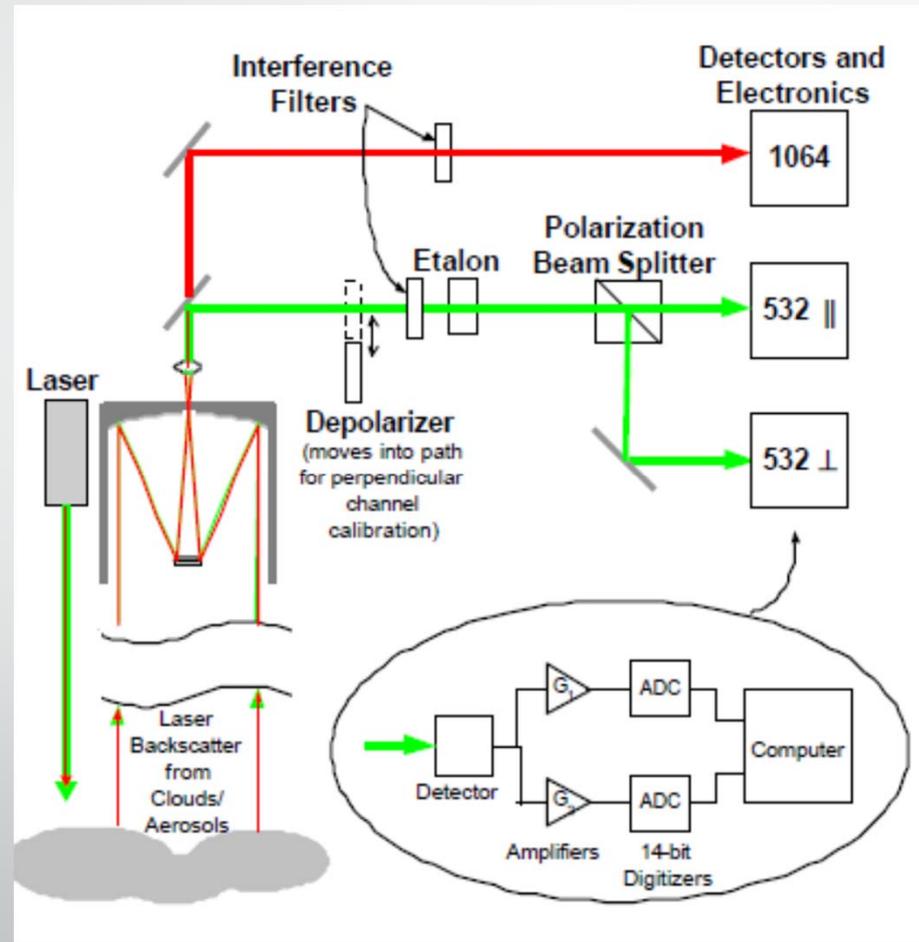


# Simulation: CALIPSO - CALIOP



- Altitude:  $\sim 700\text{km}$
- Wavelength:  $532\text{nm}$ ;  $1064\text{nm}$
- FOV:  $130\mu\text{rad}$
- Diameter:  $1\text{m}$
- Time: 2006年-今
- Off-nadir angle:  $0.3^\circ/3^\circ$
- Horizontal resolution:  $333\text{m}$
- Vertical resolution:  $30\text{m}$

# CALIPSO



# Simulated variables

- Attenuated backscatter

$$\gamma' = \int_{\text{cloud\_base}}^{\text{cloud\_top}} \frac{\beta'_{\perp}(z)}{\cos\theta_{\text{off-nadir}}} dz + \int_{\text{cloud\_base}}^{\text{cloud\_top}} \frac{\beta'_{\parallel}(z)}{\cos\theta_{\text{off-nadir}}} dz$$

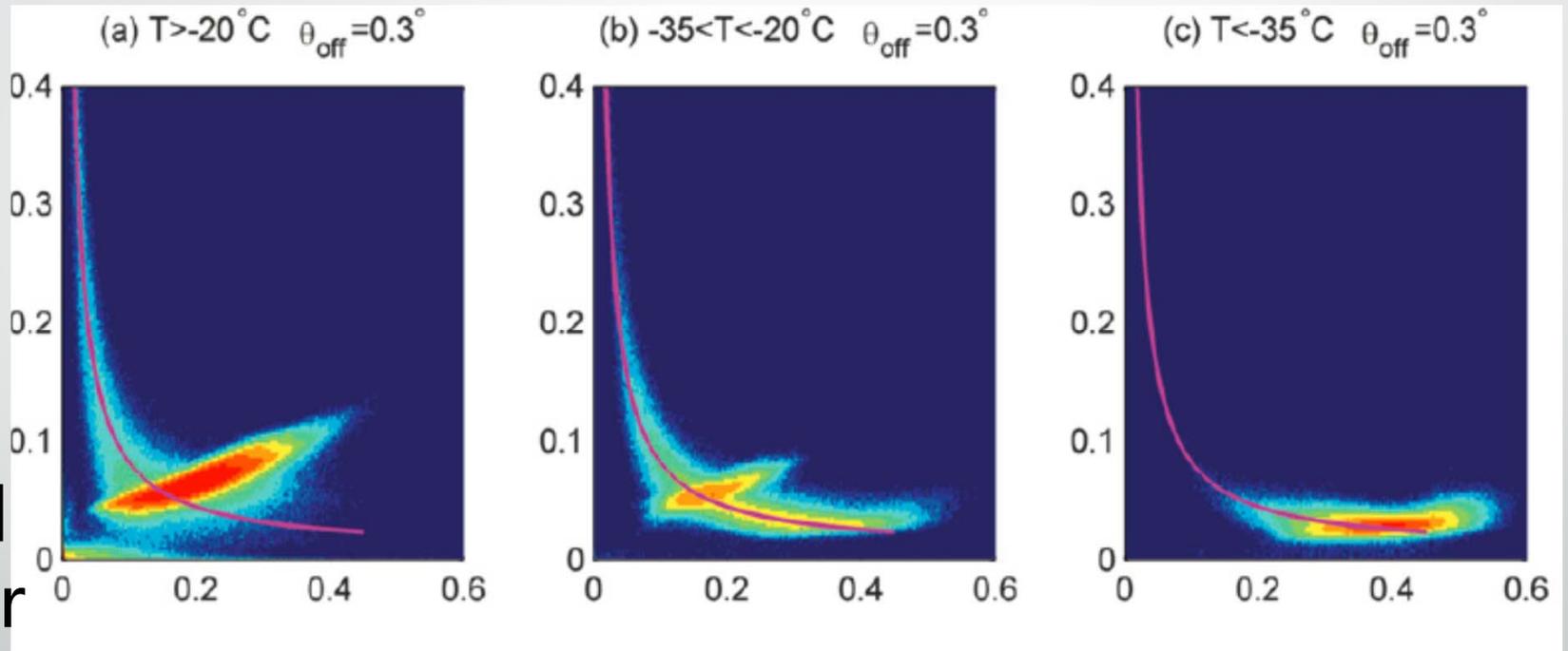
- Depolarization

$$\delta = \frac{\int_{\text{cloud\_base}}^{\text{cloud\_top}} \beta'_{\perp}(z) dz}{\int_{\text{cloud\_base}}^{\text{cloud\_top}} \beta'_{\parallel}(z) dz}$$

# Probability density function of opaque clouds

Off-nadir angle: 0.3 degree

$\gamma'$   
Layer-  
integrated  
backscatter

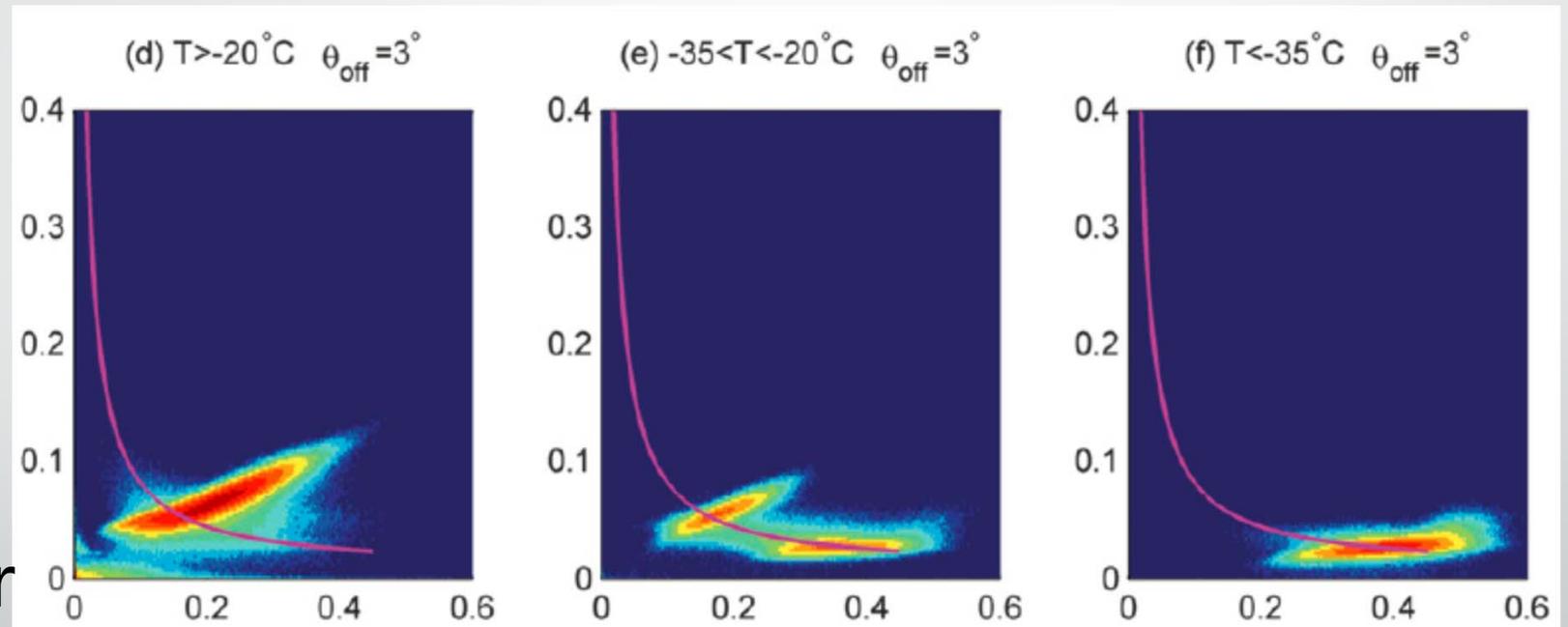


Layer integrated depolarization  $\delta$

# Probability density function of opaque clouds

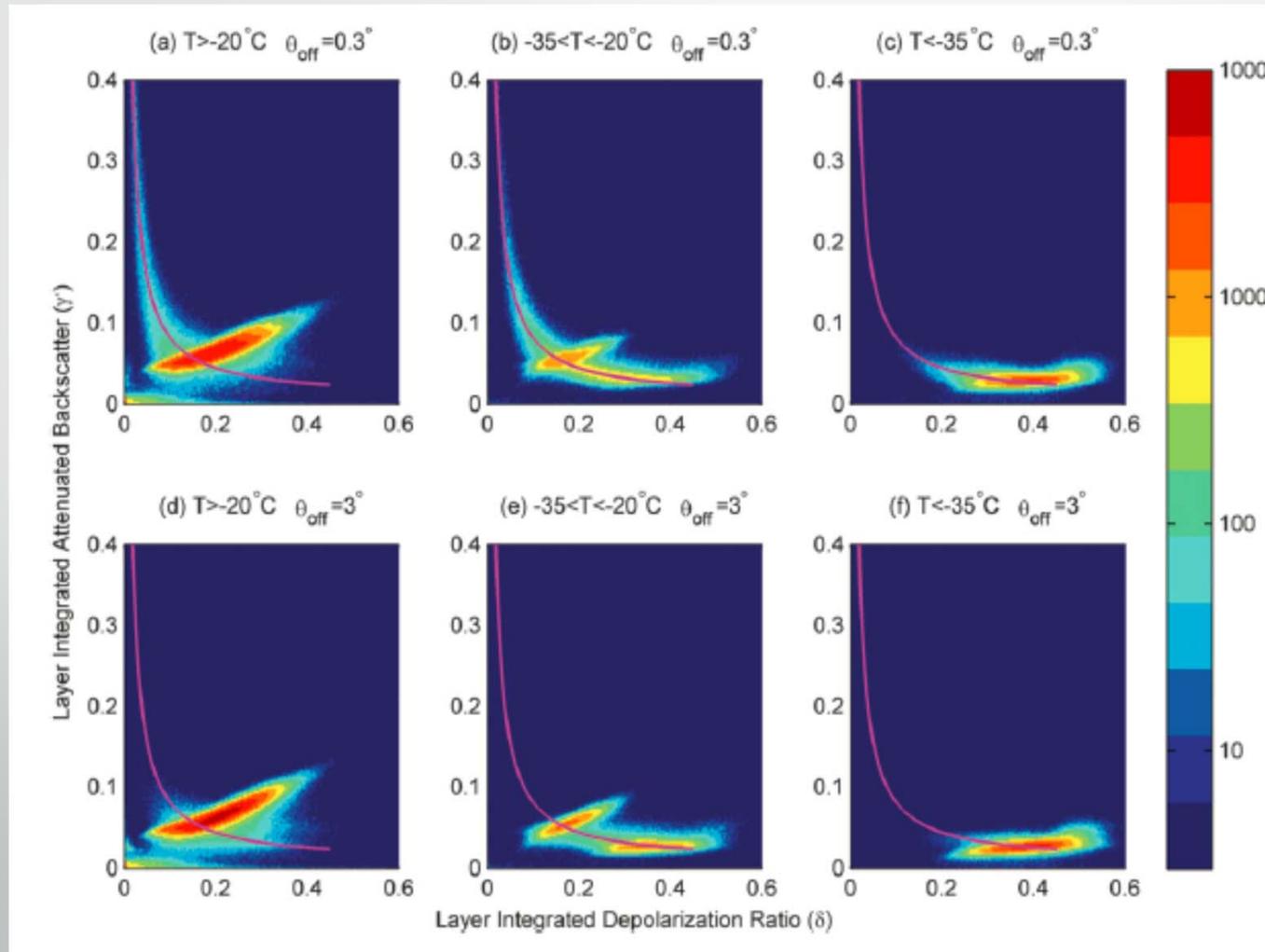
Off-nadir angle: 0.3 degree

$\gamma'$   
Layer-  
integrated  
backscatter



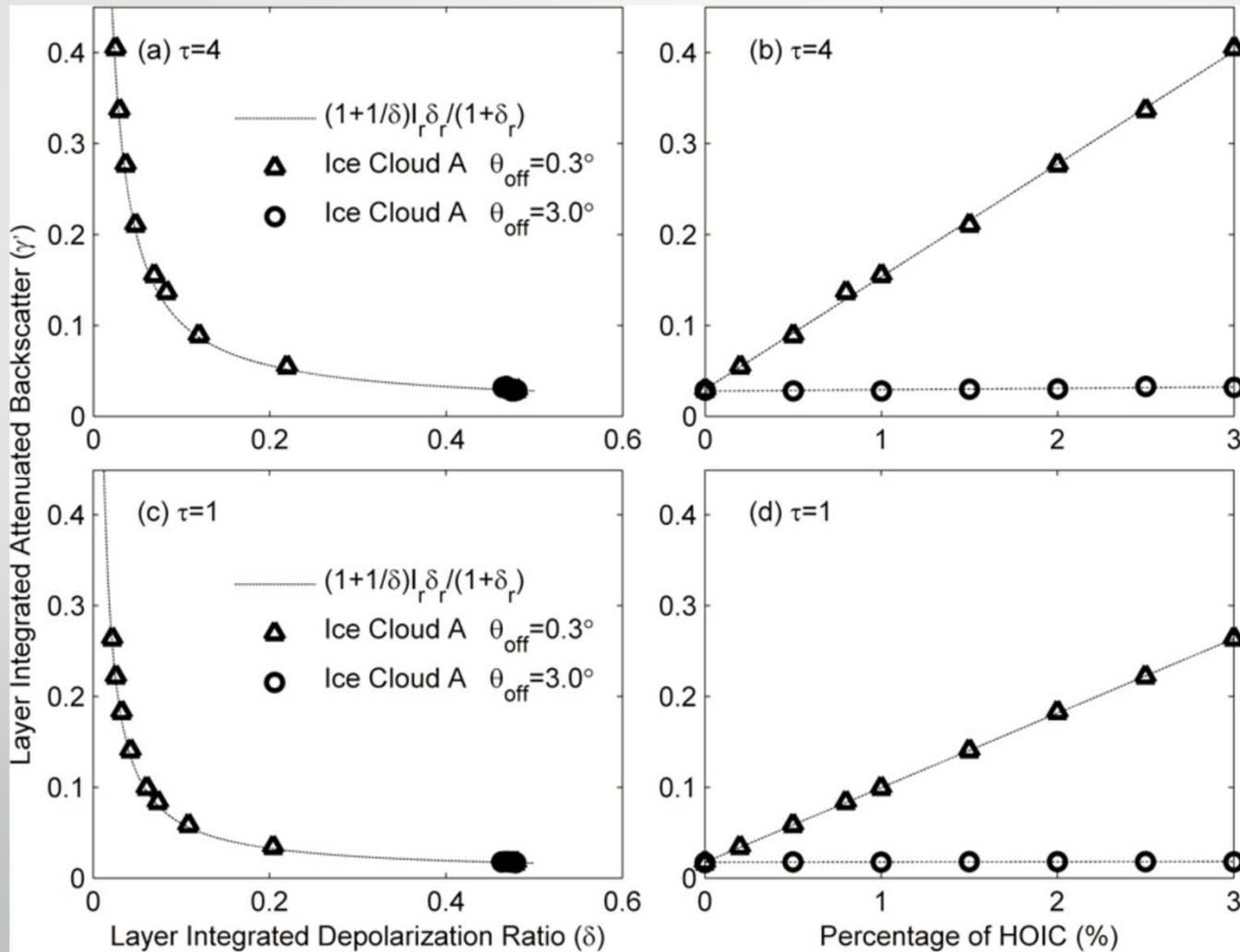
Layer integrated depolarization  $\delta$

Why does the “tail” disappear when the off-nadir angle changes from 0.3 to 3 degrees?



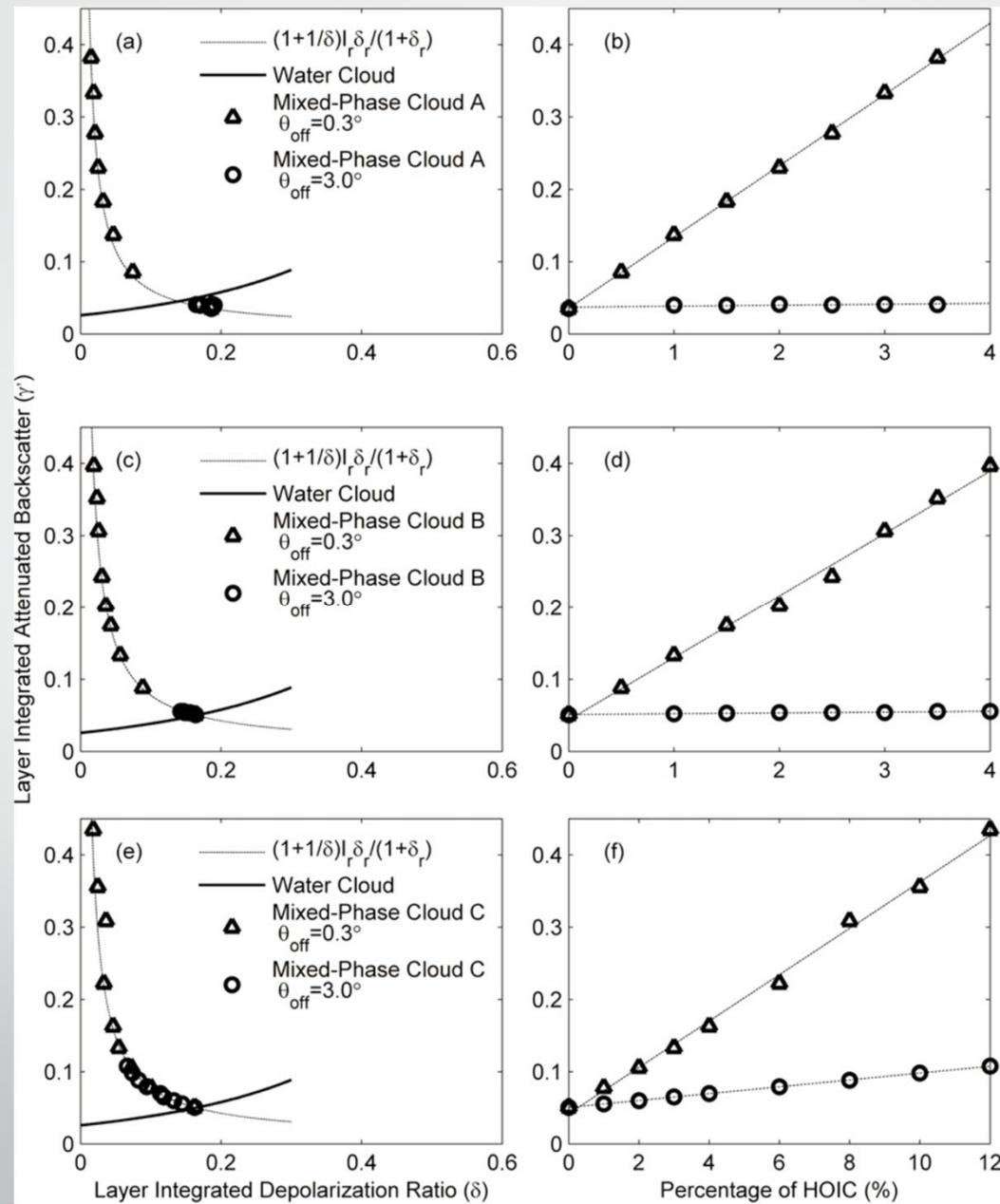
**Horizontally oriented ice plates**

# Simulation results: Ice clouds



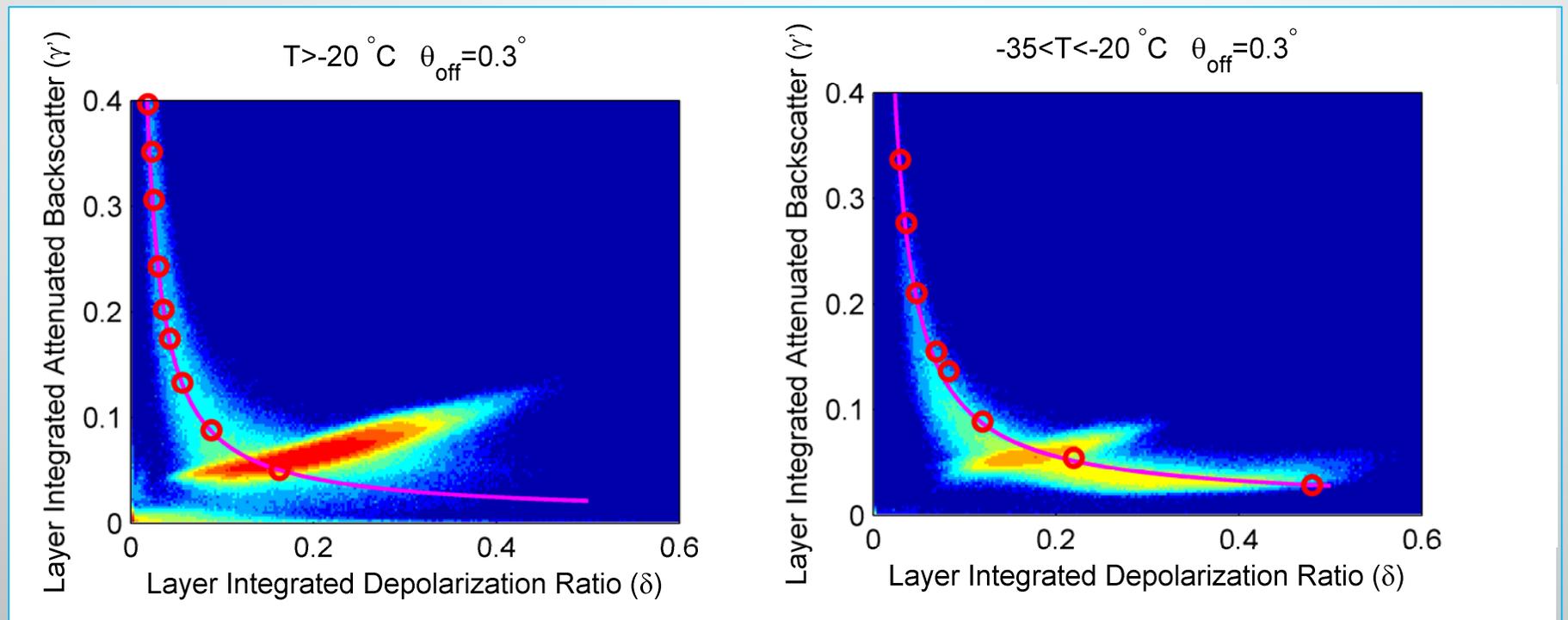
Zhou et al.  
(2012)

# Simulation: Mixed-phase clouds



Zhou et al.  
(2012)

# Comparison of simulations with observations (off-nadir=0.3)



Zhou et al.  
(2012)

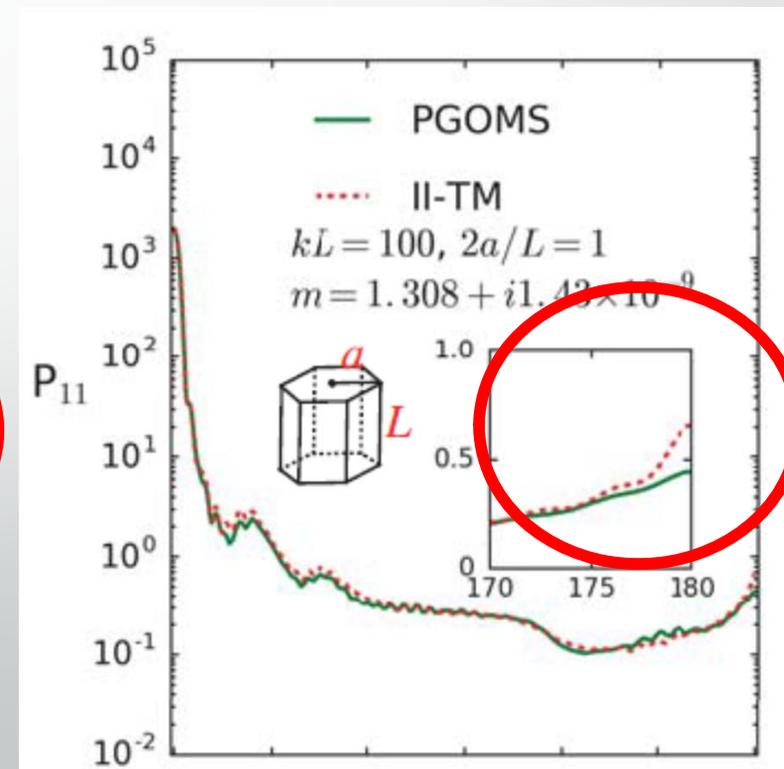
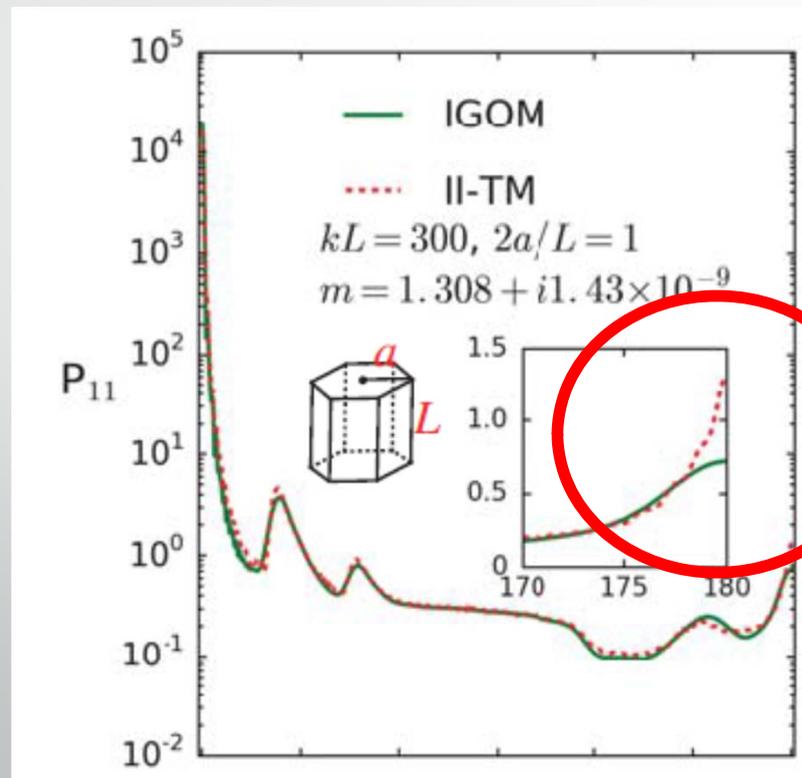
# Simulation results

- Horizontally oriented ice cloud particles:  
Consistent very well with observations
- Randomly oriented particles:  
The simulated backscatter is systematically lower than observations. (**underestimated by ~40%**)

**Why is there an underestimation?**

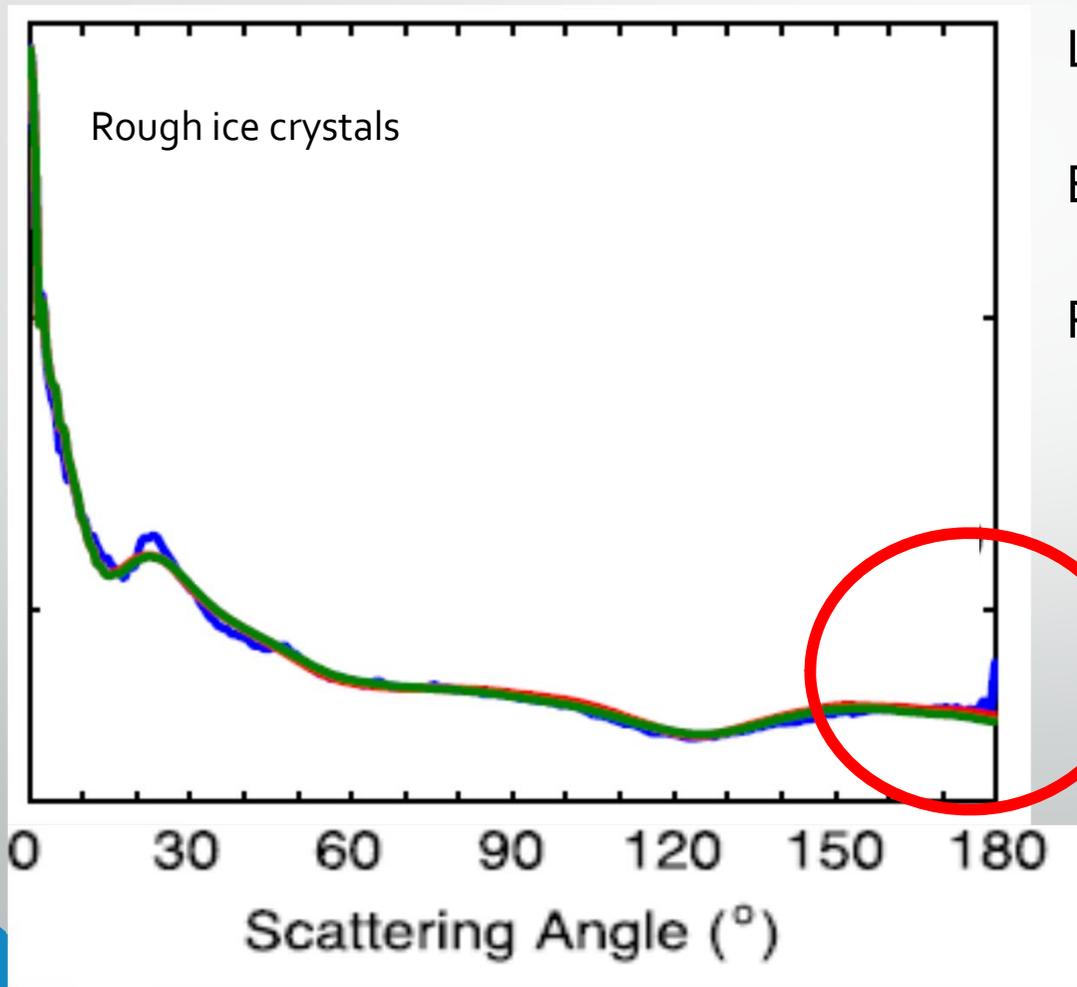
# Problem with the Geometric methods?

Geometric method simulate a backscatter much less than accurate models based on Maxwell's equations. **A process might be missing.**



Yang et al. (2019)

# A backscattering peak for ice crystals?



Liu et al. (2013)

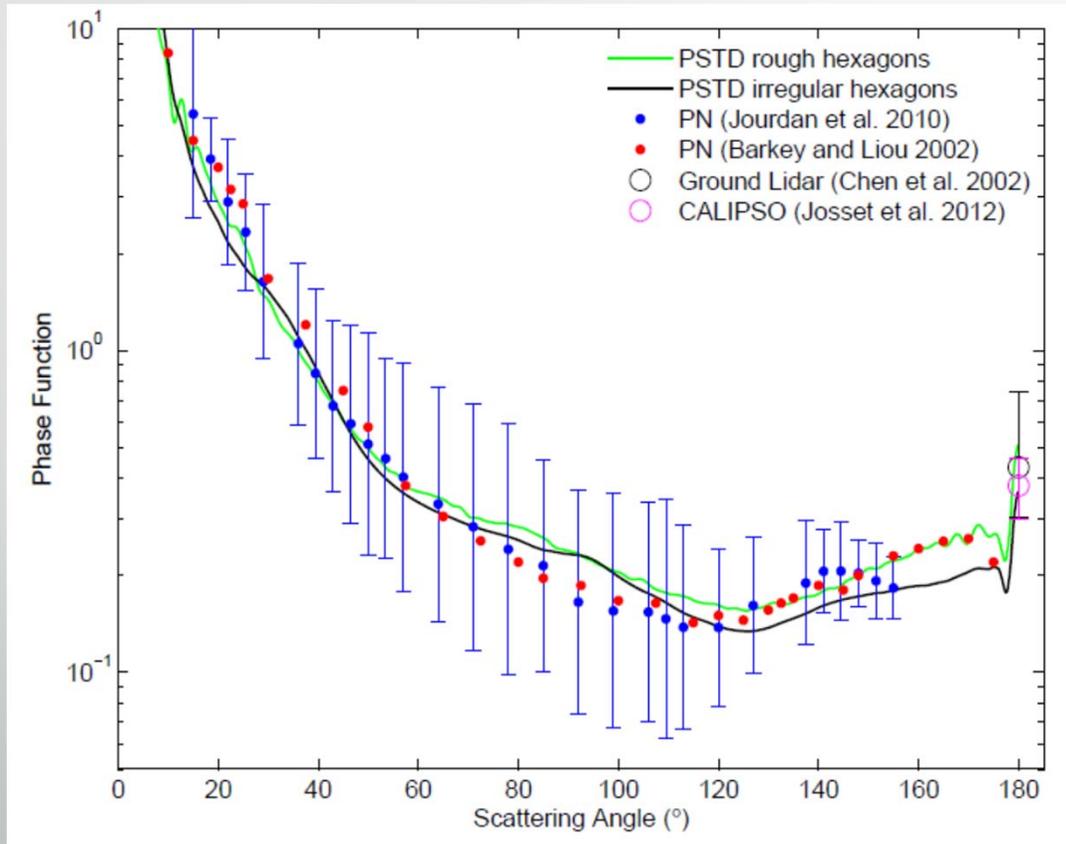
Blue: Rigid Method

Peak exist

Red/green: Geometric method

Peak not exist

# Observations: Backscattering peak exist



Why is there a peak?

Zhou and Yang (2015)

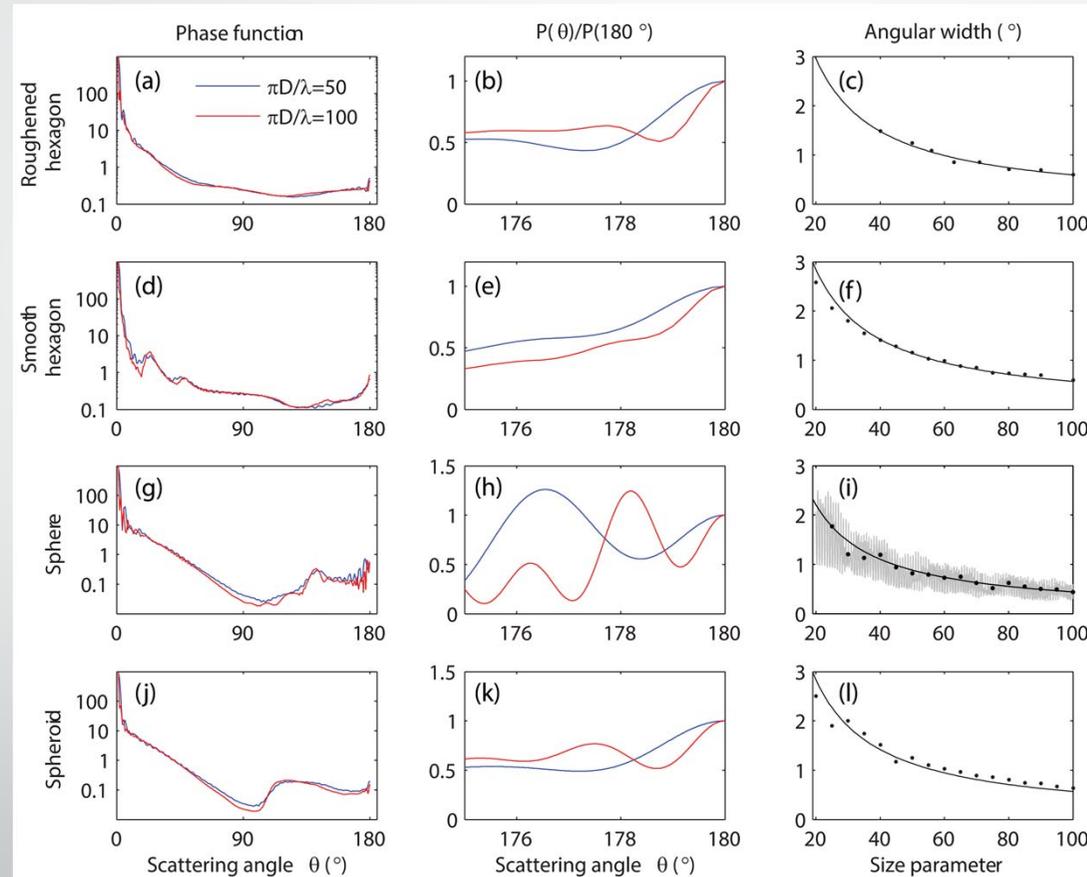
# The backscattering peak width is inversely proportional to the size parameter.

Rough hexagon

Regular hexagon

Sphere

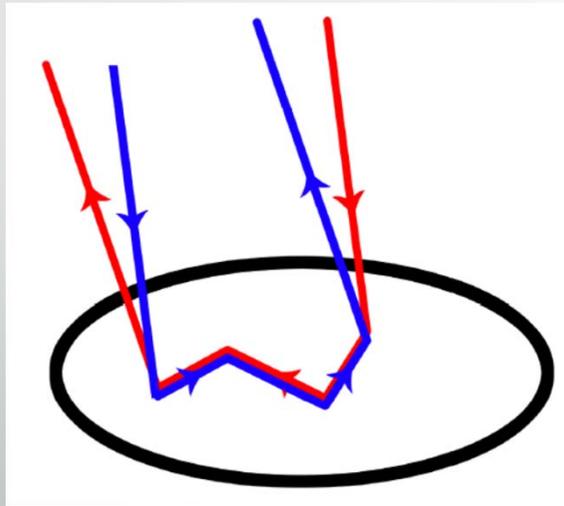
Spheroid



Zhou (2018)

# Coherent backscatter enhancement

**Interference** between conjugate terms representing reversible sequences of elementary scatterers is constructive at the backscattering direction, resulting in a coherent backscatter enhancement.



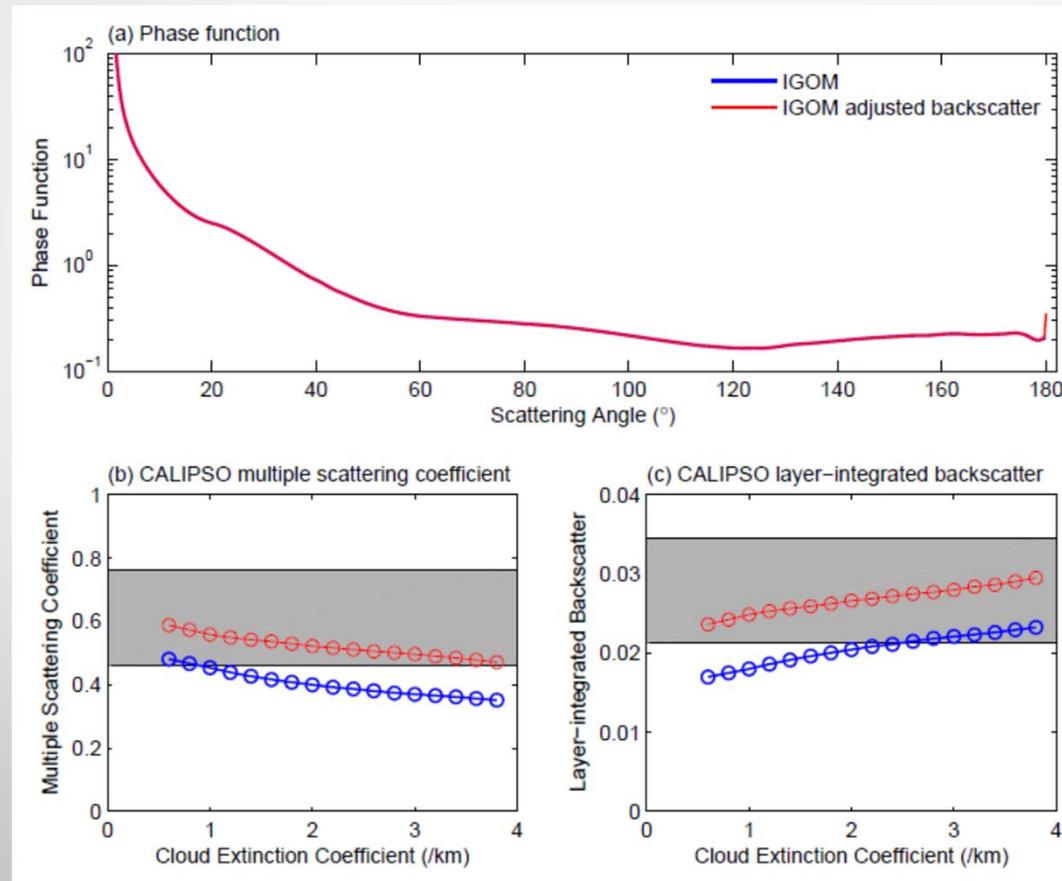
Zhou (2018)

$$\begin{aligned} \bar{E}^{sca}(\vec{r}_s, t) &= \int_{V_{int}} d\vec{r}_1 k_1^2 (\tilde{m}^2(\vec{r}_1) - 1) \bar{G}(\vec{r}_s, \vec{r}_1) \cdot \bar{E}^{inc}(\vec{r}_1, t) \\ &+ \sum_{n=2}^{\infty} \int_{V_{int}} \dots \int_{V_{int}} d\vec{r}_1 \dots d\vec{r}_n k_1^{2n} \prod_{i=1}^n (\tilde{m}^2(\vec{r}_i) - 1) \bar{G}(\vec{r}_s, \vec{r}_1) \bar{G}(\vec{r}_1, \vec{r}_2) \dots \bar{G}(\vec{r}_{n-1}, \vec{r}_n) \cdot \bar{E}^{inc}(\vec{r}_n, t) \end{aligned}$$

$$\begin{aligned} &\bar{E}_{c1,\parallel}(\vec{r}_s, t) + \bar{E}_{c2,\parallel}(\vec{r}_s, t) \\ &= \sum_{n=2}^{\infty} \int_{V_{int}} \dots \int_{V_{int}, |\vec{r}_n| > |\vec{r}_1|} d\vec{r}_1 \dots d\vec{r}_n k_1^{2n} \prod_{i=1}^n (\tilde{m}^2(\vec{r}_i) - 1) \\ &\cdot (\hat{r}_{\parallel} \otimes \hat{r}_{\parallel}) \cdot \prod_{i=1}^{n-1} \left\{ \left( \frac{3}{k_1^2 r_{i,i+1}^2} - \frac{3i}{k_1 r_{i,i+1}} - 1 \right) \hat{r}_{i,i+1} \otimes \hat{r}_{i,i+1} + \left( 1 + \frac{i}{k r_{i,i+1}} - \frac{1}{k^2 r_{i,i+1}^2} \right) \bar{I} \right\} \cdot \hat{r}_0 \\ &G(\vec{r}_1, \vec{r}_2) \dots G(\vec{r}_{n-1}, \vec{r}_n) E_0 [\exp(i\vec{k}_i \cdot \vec{r}_n - i\omega t) G(\vec{r}_s, \vec{r}_1) + \exp(i\vec{k}_i \cdot \vec{r}_1 - i\omega t) G(\vec{r}_s, \vec{r}_n)]. \end{aligned}$$

$$\begin{aligned} &|\bar{E}_{c1,\parallel}(\vec{r}_s, t) + \bar{E}_{c2,\parallel}(\vec{r}_s, t)|^2 = |2\bar{E}_{c1,\parallel}(\vec{r}_s, t)|^2 \\ &= 2(|\bar{E}_{c1,\parallel}(\vec{r}_s, t)|^2 + |\bar{E}_{c2,\parallel}(\vec{r}_s, t)|^2), [backscatter] \end{aligned}$$

By **adjusting** the IGOM simulated phase function with the coherent backscatter theory, we are now able to simulate the observed backscatter for randomly oriented particles well.



Zhou and Yang (2015)

# Conclusions

- 1. The lidar signals of ice cloud particles can be well simulated with a Monte Carlo radiative transfer model.
- 2. Horizontally oriented ice cloud particles exist in over **60%** of thick ice/mixed-phase clouds. The **equivalent** fraction of regular horizontally oriented plates is only **0.2%**, but the actual percentage can be much more.
- 3. There is a **backscattering peak** associated with the phase function of randomly oriented ice particles. The backscattering peak is largely induced by **coherent backscatter enhancement** in single scattering.

## Discussion: Fast RTM for lidar simulations

Monte Carlo radiative transfer model is expensive:

- CPU time: 5 min for 1 case with pure randomly oriented particles. 50 min for 1 case with oriented particles.
- Storage: the phase matrix for a specific oriented particle is **10 GB**.  $\mathbf{P} = \mathbf{P}(\theta_i, \varphi_i, \theta_s, \varphi_s)$

**We may want a fast RTM for lidar**

## Discussion: How to build a fast RTM for lidar?

- 1. Plane parallel models (i. e., adding-doubling) could not be used. None-uniform incident beam.
- 2. Monte Carlo is too slow.
- 3. Simple **lidar equations** requires predetermined parameters to account for multiple scattering.

Proposed solution:

- Combine the Monte Carlo results, and simple lidar equations.

# Discussion: Proposed fast RTM for lidar

- 1. Simulate the lidar signals of various clouds and aerosols with the Monte Carlo radiative transfer model, and build a database.
- 2. Retrieve **statistical relationships** between multiple scattering coefficient, depolarization, FOV, extinction coefficient, and particle type (including orientation) with the database.
- 3. For a specific volume, calculate **the multiple scattering coefficient** and **depolarization** from the above **statistical relationship**, and insert to the traditional lidar equation.