

# The ECMWF 4D-Var Analysis in the Tropics: covariance **B**, dynamic and diabatic balance

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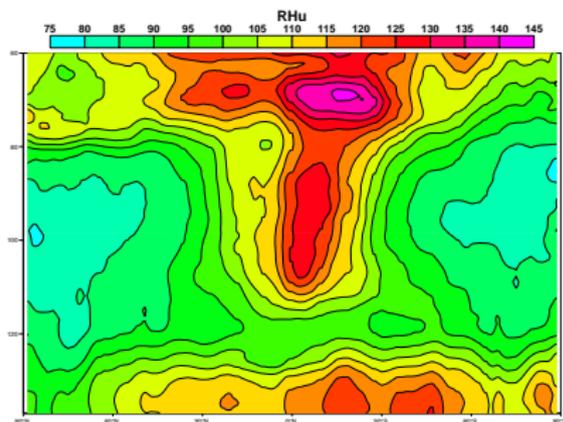
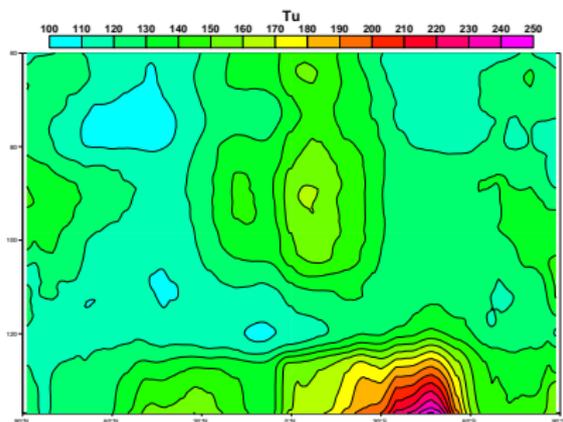
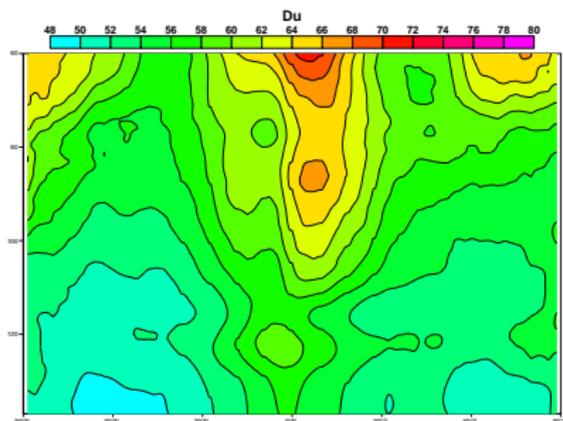
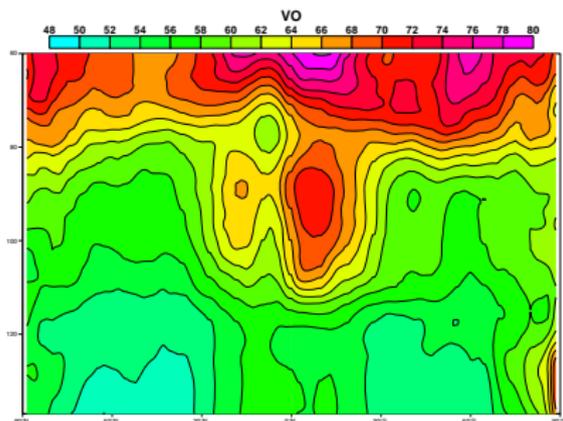
November 10, 2016

# Background errors influence on the analysis

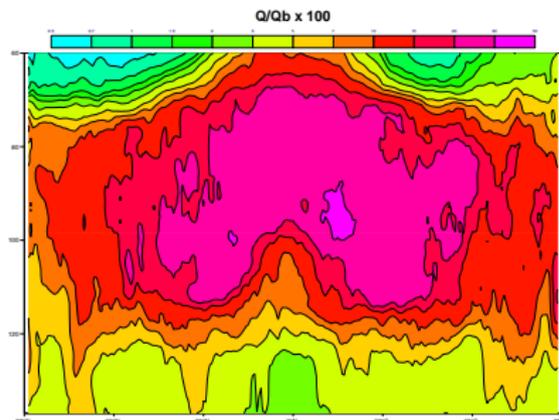
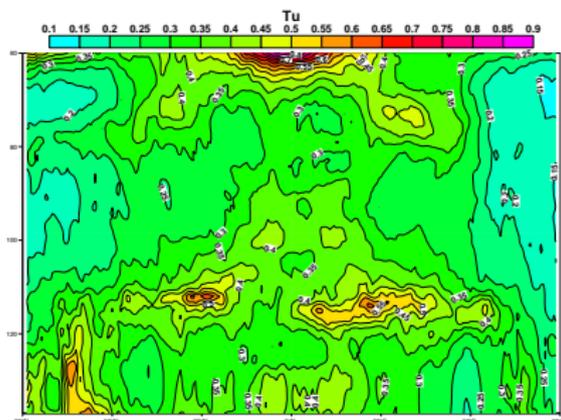
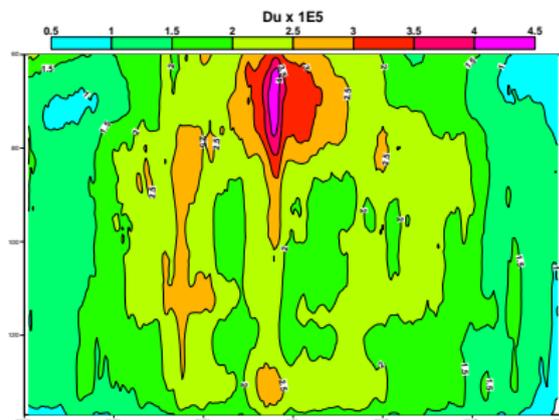
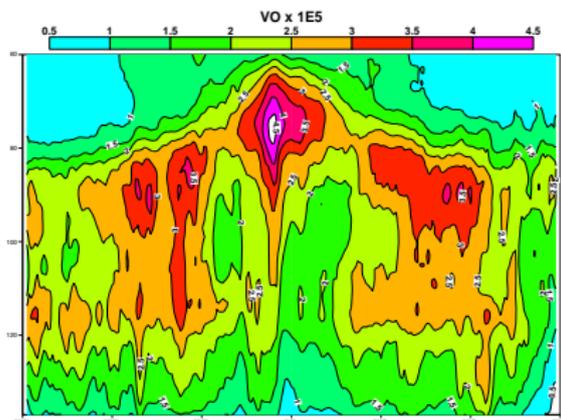
The Ensemble of Data Assimilation is input to update the background error covariance matrix **B** every analysis cycle;

- Standard deviations of all analysis variables are fully flow-dependent.
- Length-scales of the correlations are flow-dependent with climatological length-scales mixed in particularly for the low wavenumbers.
- The balance operator is a combination of analytical, flow-dependent functions and statistical climatological regressions.
- How does it look and what does it mean for the analysis?

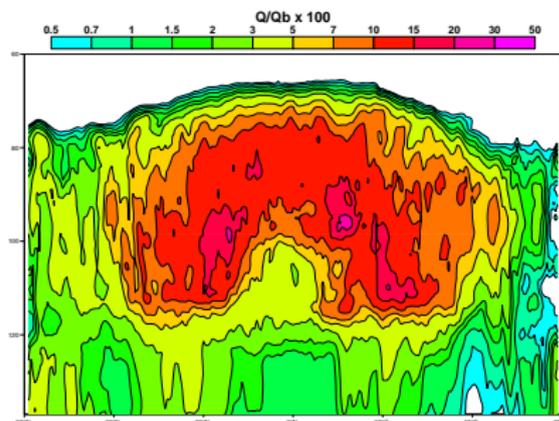
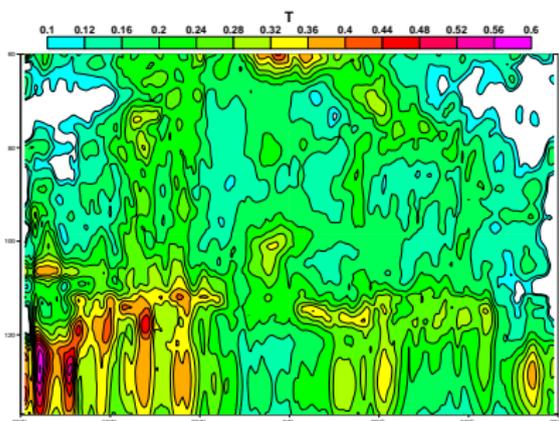
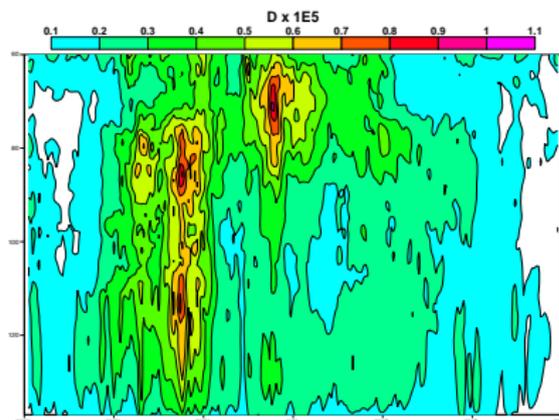
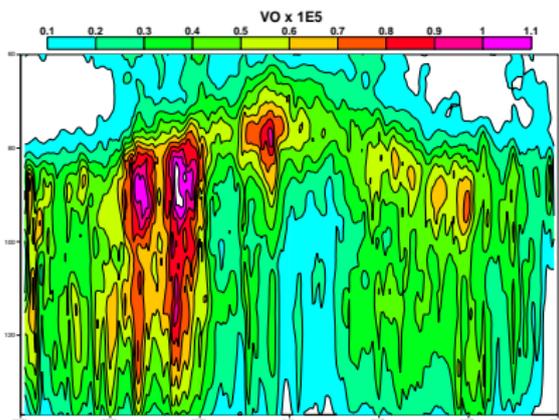
# Lengthscales $B$ [km], zonal ave



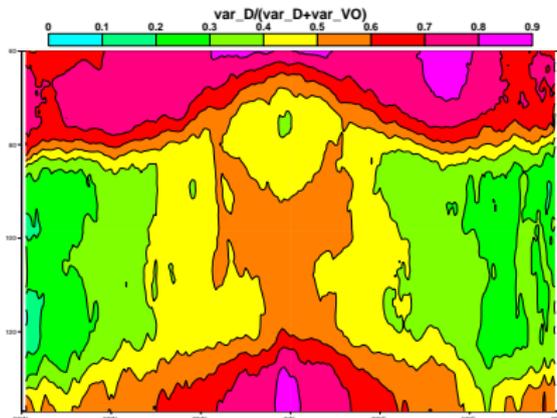
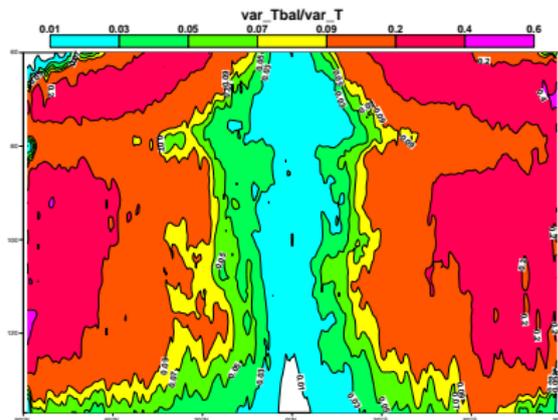
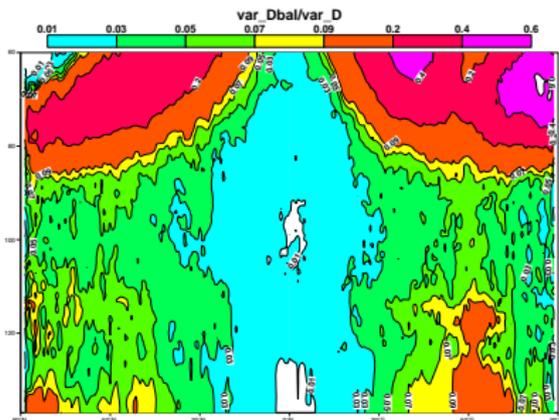
# Standard deviations **B**, zonal ave



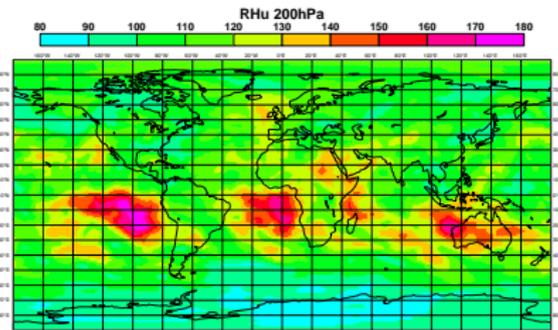
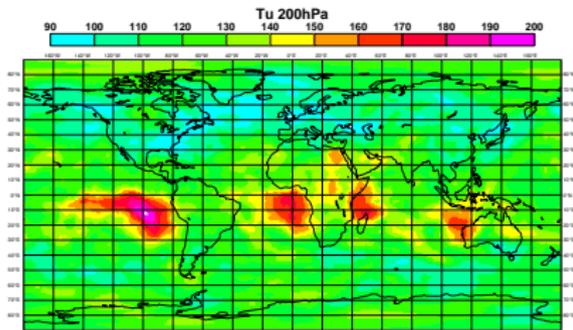
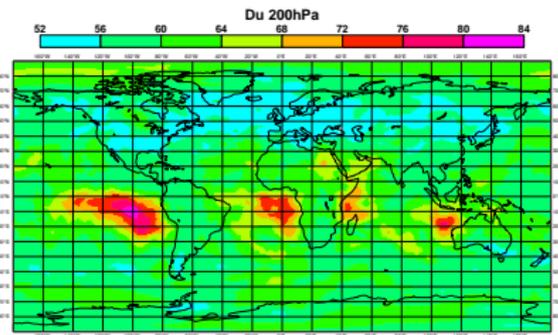
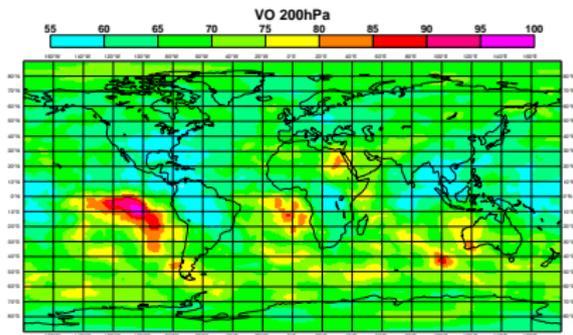
# Analysis increments absolute values, zonal ave



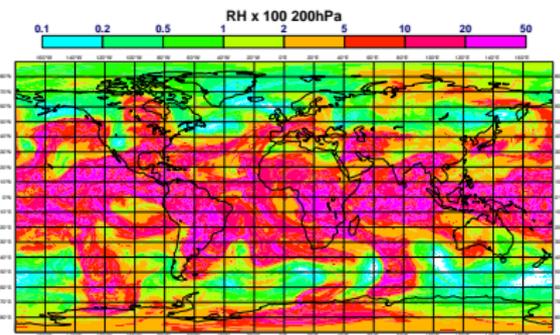
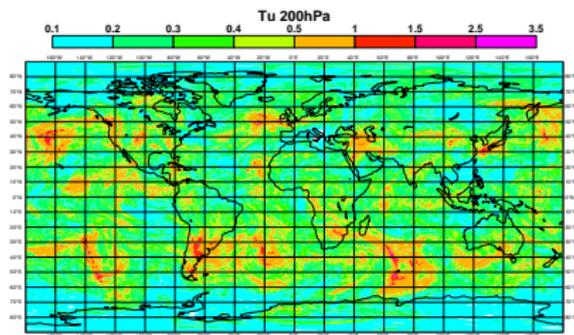
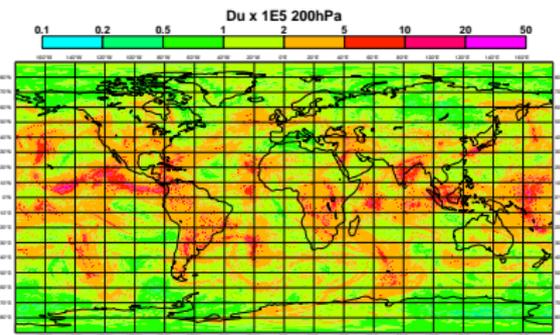
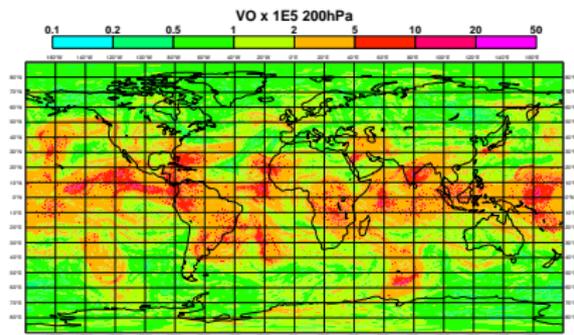
# Variance of **B** explained by balance, zonal ave



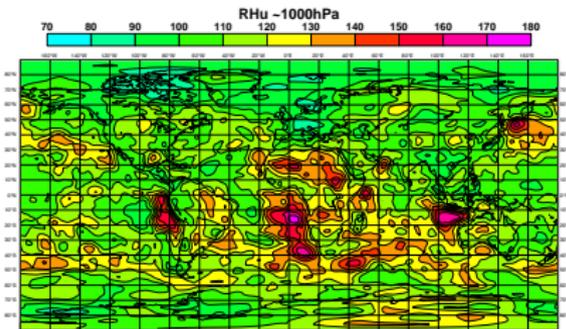
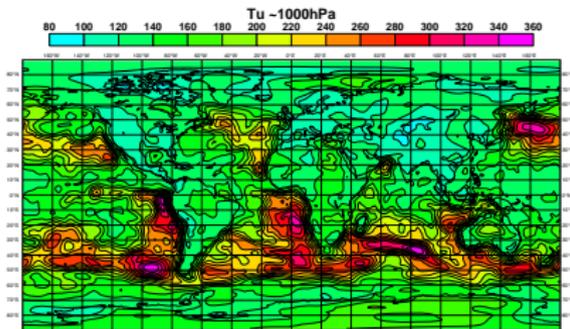
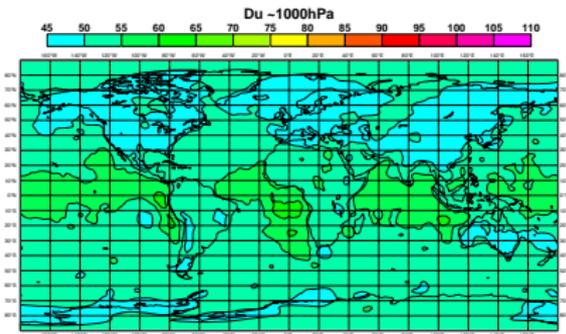
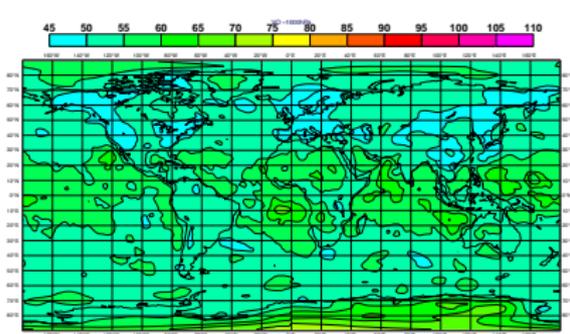
# Lengthscales **B** [km], level 74 200hPa



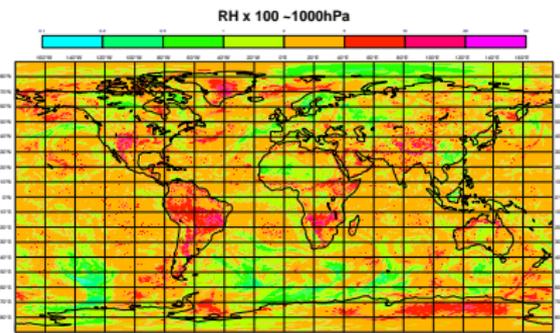
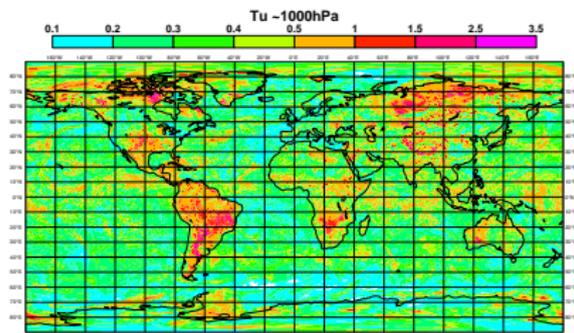
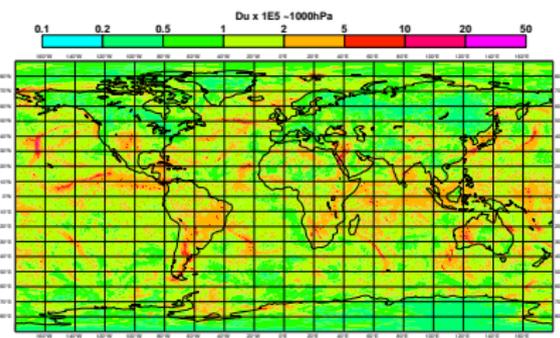
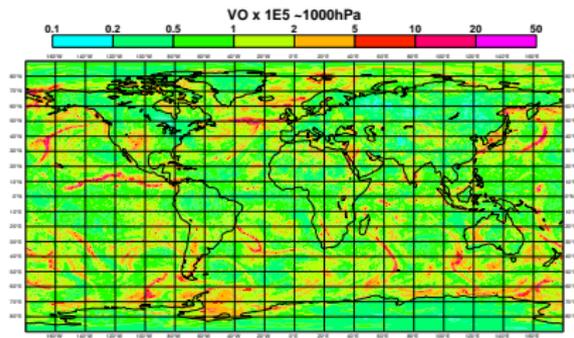
# Standard deviations **B**, level 74 200hPa



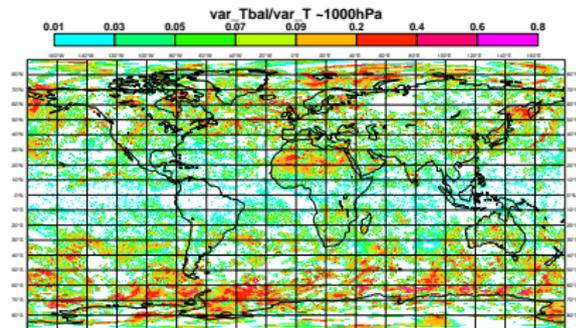
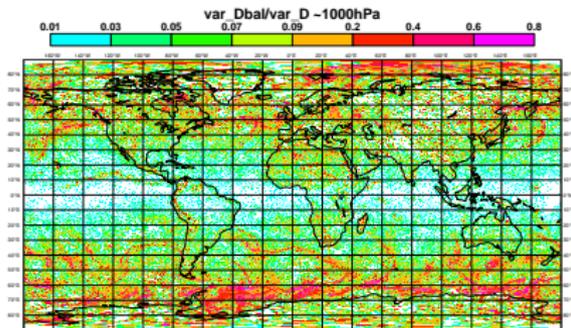
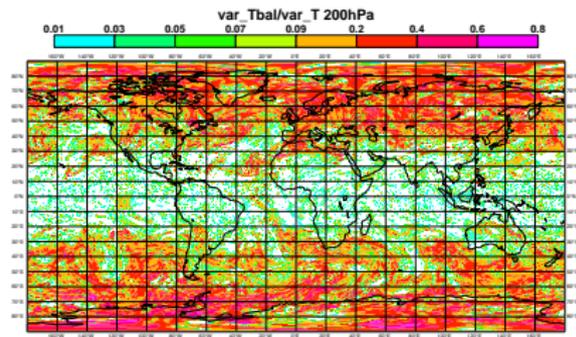
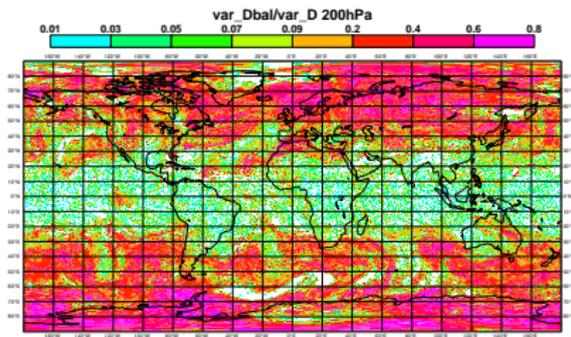
# Lengthscales **B** [km], level 137 1000hPa



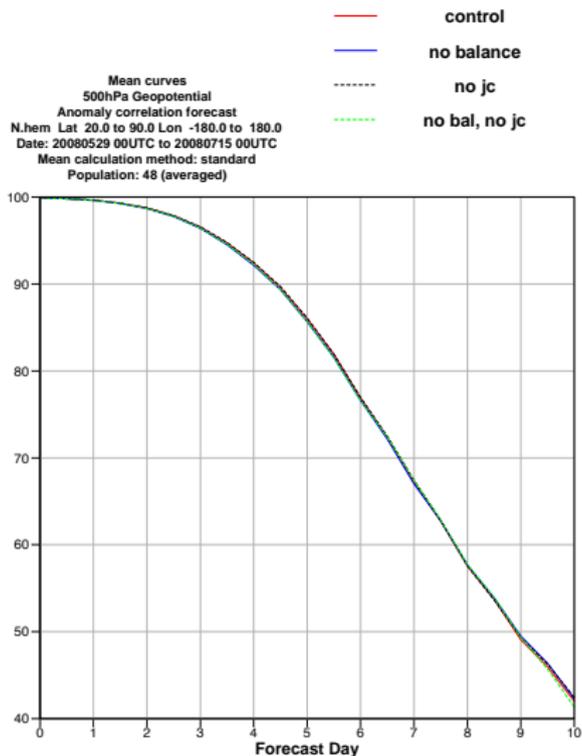
# Standard deviations **B**, level 137 1000hPa



# Variance of **B** explained by balance, 200hPa and 1000hPa



# Does balance matter for forecast quality?



## Does balance matter for forecast quality? Yes, but...

- The 4D-Var analysis manages without balance operator, creating negligible extra gravity wave noise.
- The current system is well observed with small analysis increments, enabling 4D-Var to infer balance from the temporal information in the observations.
- Tropospheric scores 1-2% worse without balance, so worth keeping on.

# The dynamic balance operator

The balance operator consists of the dynamic horizontal simplified and linearized nonlinear balance (Fisher, 2003),

$\nabla^2 P_b = (f + \zeta) \times v_\psi + \frac{1}{2} \nabla(v_\psi \cdot v_\psi)$ , combined with vertical balance operators (from statistical regression),

$$\begin{pmatrix} \delta\zeta \\ \delta\eta_n \\ \delta(T_n, p_s) \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ M & 1 & 0 \\ N & P & 1 \end{pmatrix} \begin{pmatrix} \delta\zeta \\ \delta\eta_u \\ \delta(T_u, p_{su}) \end{pmatrix}$$

and simplified and linearized version of quasi-geostrophic  $\omega$ -equation balance (Fisher, 2003),  $(\sigma \nabla^2 + f_0^2 \frac{\partial^2}{\partial p^2}) \omega' = -2 \nabla \cdot \mathbf{Q}$ ,

$$\begin{pmatrix} \delta\zeta \\ \delta\eta \\ \delta T \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ Q_2 & 1 & Q_1 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} \delta\zeta \\ \delta\eta_n \\ \delta T \end{pmatrix}$$

## Diabatic balance through linear saturation adjustment

Use linear saturation adjustment (based on Asai 1965 and Hólm et al., 2002),

$$\delta T = \delta T_n + C^b a \frac{L}{c_p} \left( \delta q_{vu} - \frac{L q_s(T^b)}{R_v (T^b)^2} \delta T_n \right)$$

$$\delta q_v = \delta q_{vu} - C^b a \left( \delta q_{vu} - \frac{L q_s(T^b)}{R_v (T^b)^2} \delta T_n \right)$$

$$\delta q_c = \delta q_{cu} + C^b a \left( \delta q_{vu} - \frac{L q_s(T^b)}{R_v (T^b)^2} \delta T_n \right)$$

In matrix form this becomes

$$\begin{pmatrix} \delta T \\ \delta q_v \\ \delta q_l \\ \delta q_i \end{pmatrix} = \begin{pmatrix} 1 - \frac{L}{c_p} C^b a \gamma & \frac{L}{c_p} C^b a & 0 & 0 \\ C^b a \gamma & 1 - C^b a & 0 & 0 \\ -\alpha C^b a \gamma & \alpha C^b a & 1 & 0 \\ -(1 - \alpha) C^b a \gamma & (1 - \alpha) C^b a & 0 & 1 \end{pmatrix} \begin{pmatrix} \delta T_n \\ \delta q_{vu} \\ \delta q_{lu} \\ \delta q_{iu} \end{pmatrix}$$

## Details of linear saturation adjustment

- Increments  $\delta T_n$  and  $\delta q_{vu}$  assumed uniform over the gridcell.
- Saturation adjustment takes place in the in-cloud portion  $C^b$  of the gridcell, with  $C^b$  approximated by a regression formula as a function of  $rh^b$  and model level.
- $q^b = q_s(T^b)$  in the in-cloud part of the gridcell.
- Cloud condensate adjustment distributed by  $\alpha(T^b)$  between  $\delta q_l$  and  $\delta q_i$  with  $\alpha(T^b)$  varying between 0 and 1 according to mixed-phase formula.
- The adjustment conserves total water.
- The adjustment is unchanged for  $\delta T$  and  $\delta q_v$  whether  $\delta q_l$  and  $\delta q_i$  are included or not.
- Here  $a = \frac{1}{1 + \frac{L^2 q_s(T^b)}{c_p R_v (T^b)^2}}$  and  $\gamma = \frac{L q_s(T^b)}{R_v (T^b)^2}$

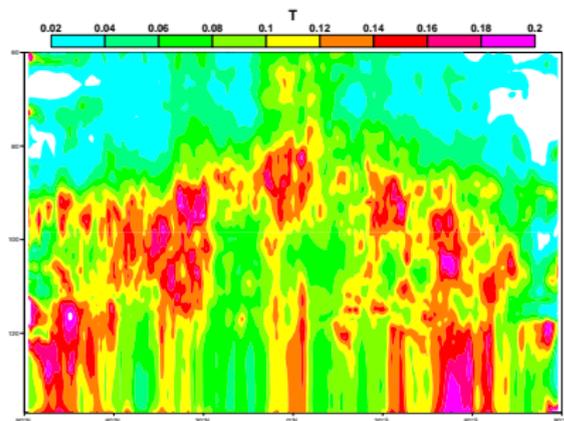
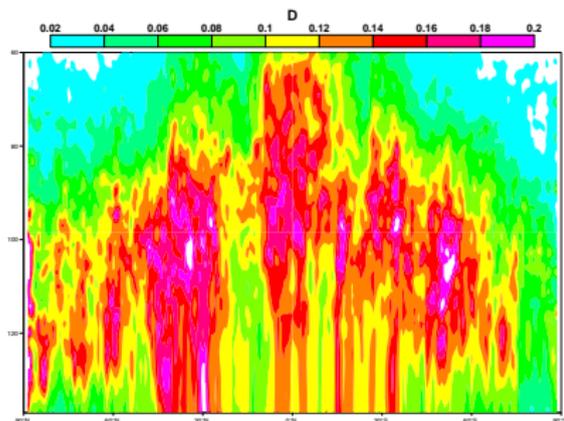
## Apply $\omega$ -equation after saturation adjustment

By applying the  $\omega$ -equation balance after the saturation adjustment, the final divergence dynamically supports the water vapour and cloud condensate changes in an adaptive way without any special treatment:

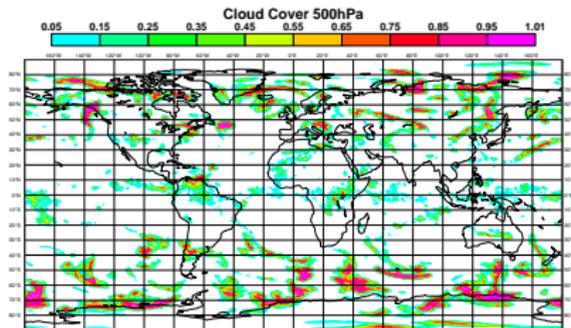
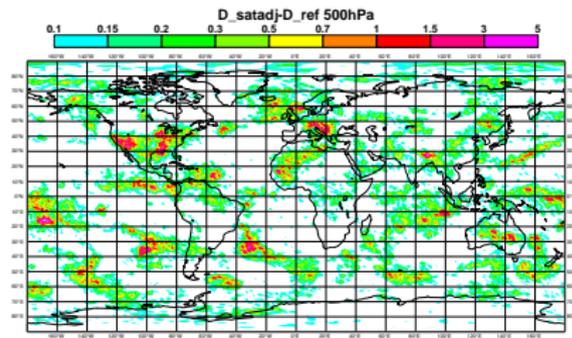
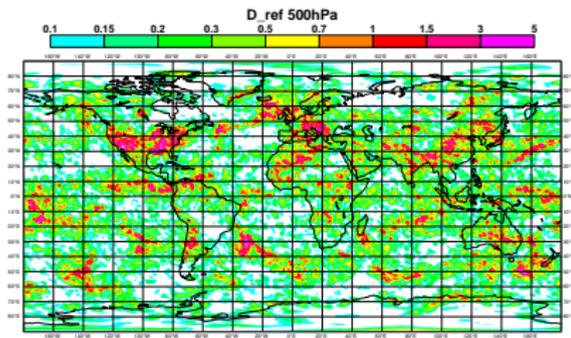
$$\begin{pmatrix} \delta\zeta \\ \delta\eta \\ \delta T \\ \delta q_v \\ \delta q_c \end{pmatrix} = \begin{pmatrix} Q_2 + M + Q_1 N \left(1 - \frac{1}{c_p} C^b_{a\gamma}\right) & 1 + Q_1 P \left(1 - \frac{1}{c_p} C^b_{a\gamma}\right) & Q_1 \left(1 - \frac{1}{c_p} C^b_{a\gamma}\right) & Q_1 \frac{1}{c_p} C^b_a & 0 \\ N \left(1 - \frac{1}{c_p} C^b_{a\gamma}\right) & P \left(1 - \frac{1}{c_p} C^b_{a\gamma}\right) & 1 - \frac{1}{c_p} C^b_{a\gamma} & \frac{1}{c_p} C^b_a & 0 \\ NC^b_{a\gamma} & PC^b_{a\gamma} & C^b_{a\gamma} & 1 - C^b_a & 0 \\ -NC^b_{a\gamma} & -PC^b_{a\gamma} & -C^b_{a\gamma} & C^b_a & 1 \end{pmatrix} \begin{pmatrix} \delta\zeta \\ \delta\eta_u \\ \delta T_u \\ \delta q_{vu} \\ \delta q_{cu} \end{pmatrix}$$

with  $\delta q_c = \delta q_l + \delta q_i$  and  $\delta T = \delta(T, p_s)$  and  $\delta T_u = \delta(T, p_s)_u$ .

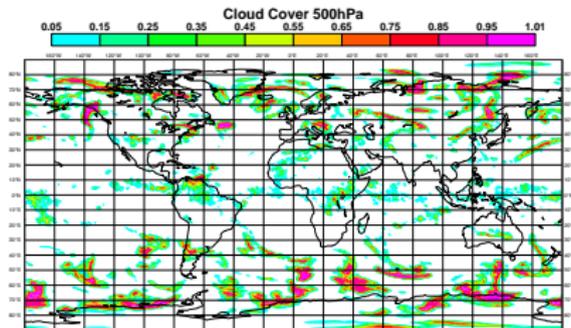
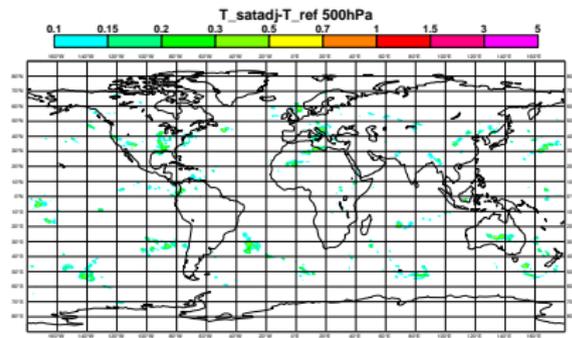
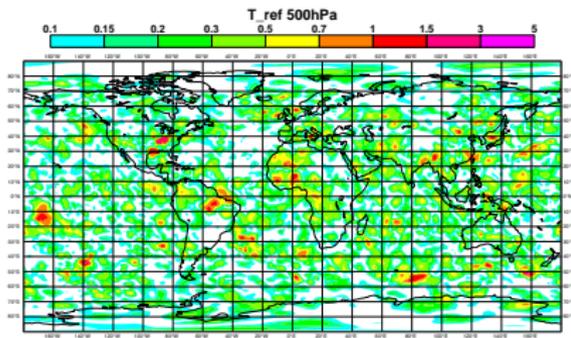
# Increment ratio $\text{abs}(\text{SatAdj} - \text{Ref})/\text{abs}(\text{Ref})$ , zonal ave



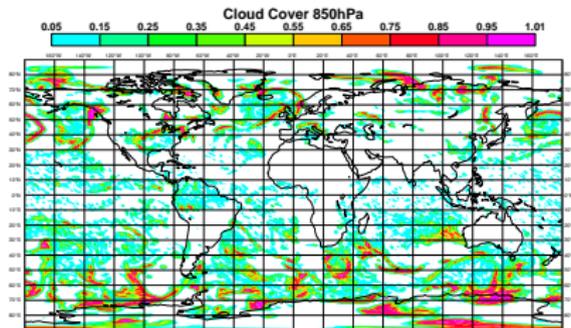
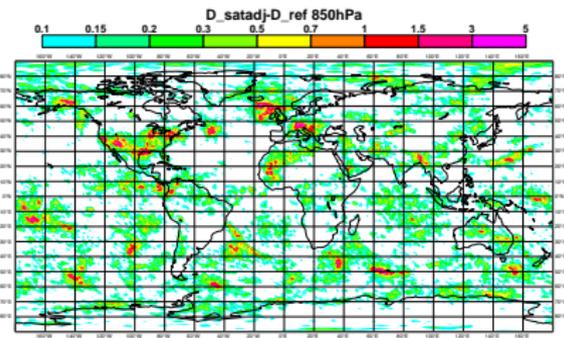
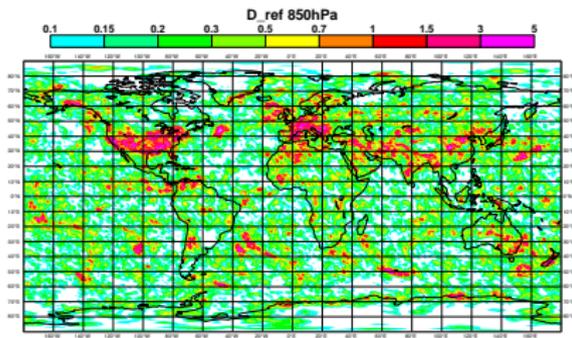
# D 500hPa increments: abs(Ref), abs(SatAdj-Ref), cc



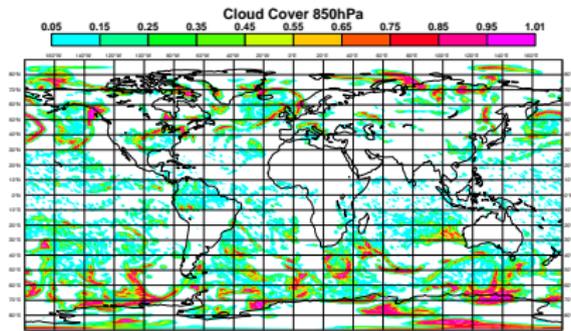
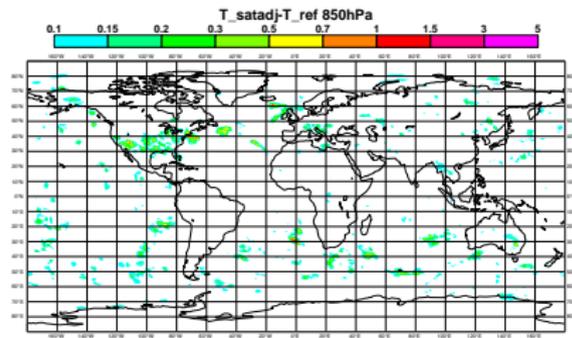
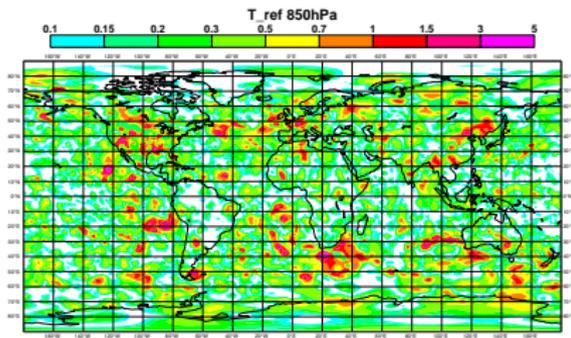
# T 500hPa increments: abs(Ref), abs(SatAdj-Ref), cc



# D 850hPa increments: abs(Ref), abs(SatAdj-Ref), cc



# T 850hPa increments: abs(Ref), abs(SatAdj-Ref), cc

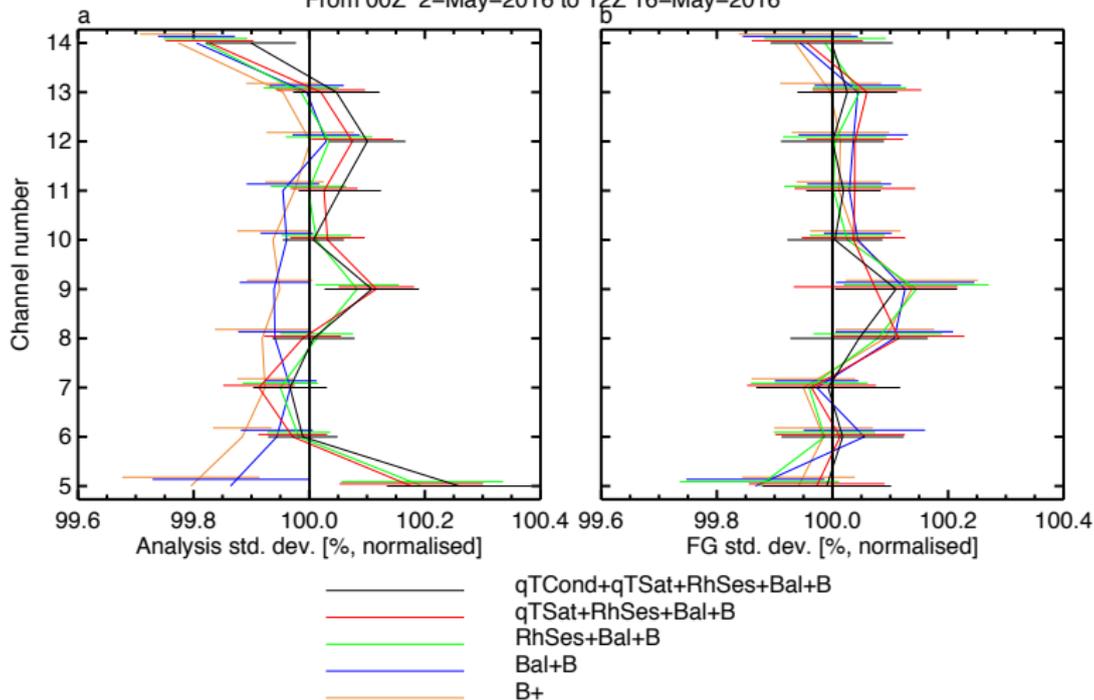


# Results for AMSU-A (O-B) - NHem

Instrument(s): AQUA metop-a metop-b noaa-15 noaa-18 noaa-19 sky - AMSU-A

Area(s): N.Hemis

From 00Z 2-May-2016 to 12Z 16-May-2016

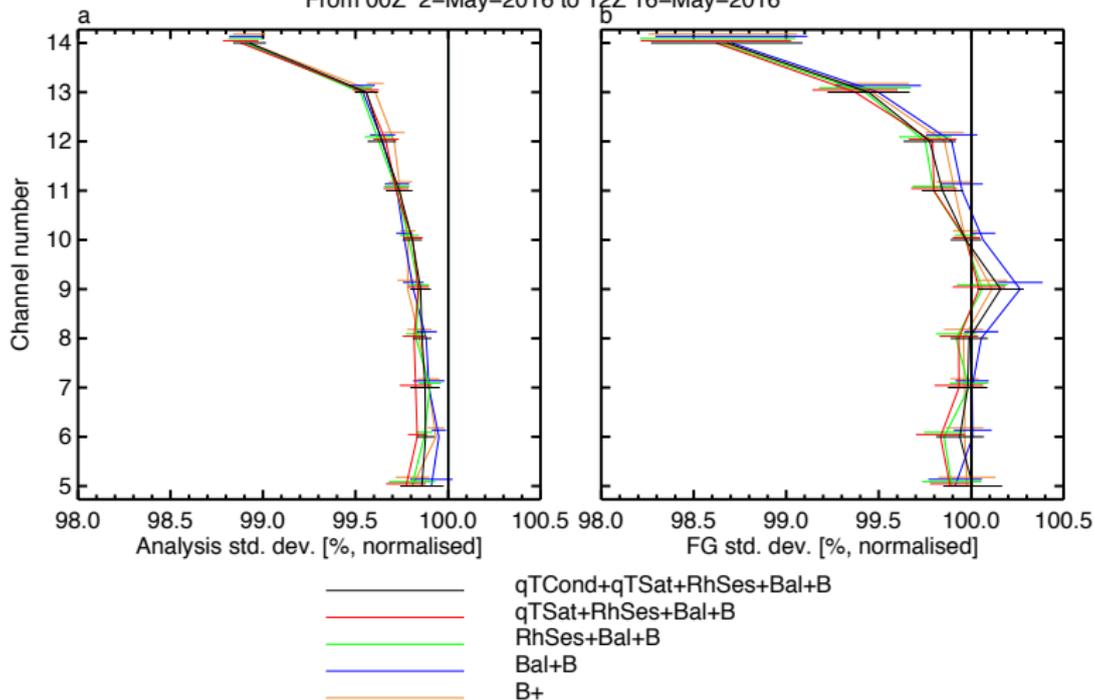


# Results for AMSU-A (O-B) - SHem

Instrument(s): AQUA metop-a metop-b noaa-15 noaa-18 noaa-19 sky - AMSU-A

Area(s): S.Hemis

From 00Z 2-May-2016 to 12Z 16-May-2016

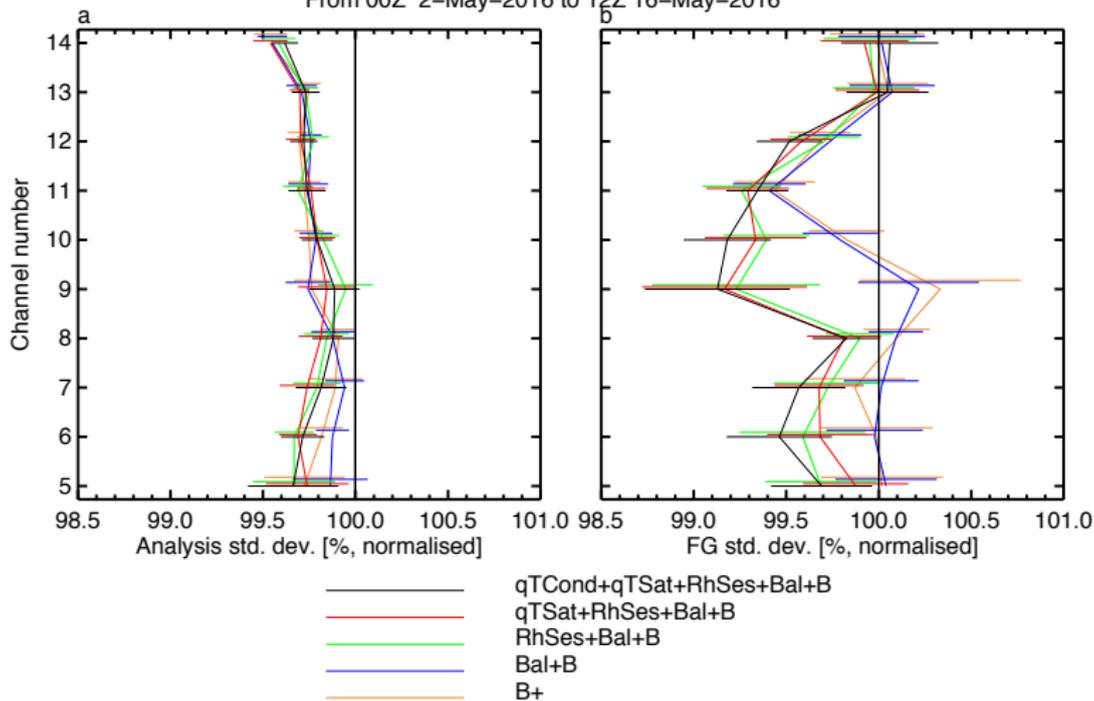


# Results for AMSU-A (O-B) - Tropics

Instrument(s): AQUA metop-a metop-b noaa-15 noaa-18 noaa-19 sky - AMSU-A

Area(s): Tropics

From 00Z 2-May-2016 to 12Z 16-May-2016



## References

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- Hólm, E., E. Andersson, A. Beljaars, P. Lopez, J-F. Mahfouf, A.J. Simmons and J.N. Thpaut, (2002): *Assimilation and Modelling of the Hydrological Cycle: ECMWF's Status and Plans*. ECMWF Tech. Memorandum No. **383**, available from ECMWF, Shinfield Park, Reading RG2 9AX, UK.