

# Error diagnostics for PC scores assimilation

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# Introduction

- **Specifying errors is essential for the assimilation of any observation.**
- **Simpler error characteristics were a key argument for moving to the assimilation of raw radiances.**
- **What are the characteristics of observation and background error in PC-space?**
- **In radiance space, representativeness, RT, and QC errors are correlated between channels – what do they look like in PC-space?**
- **For a given assumed observation error in PC-space, what is the equivalent error in radiance space?**
- **PC-truncation is not addressed in this talk.**

# Observation error in PC-space

- **When PCs are calculated from noise-normalised radiances, the observation error is:**

$$\mathbf{R}_{PC} = \mathbf{I} + \mathbf{F}_{PC}$$

$\mathbf{I}$  – Identity matrix

$\mathbf{F}_{PC}$  – “other errors” (e.g., forward model errors, representativeness errors, QC errors, etc)

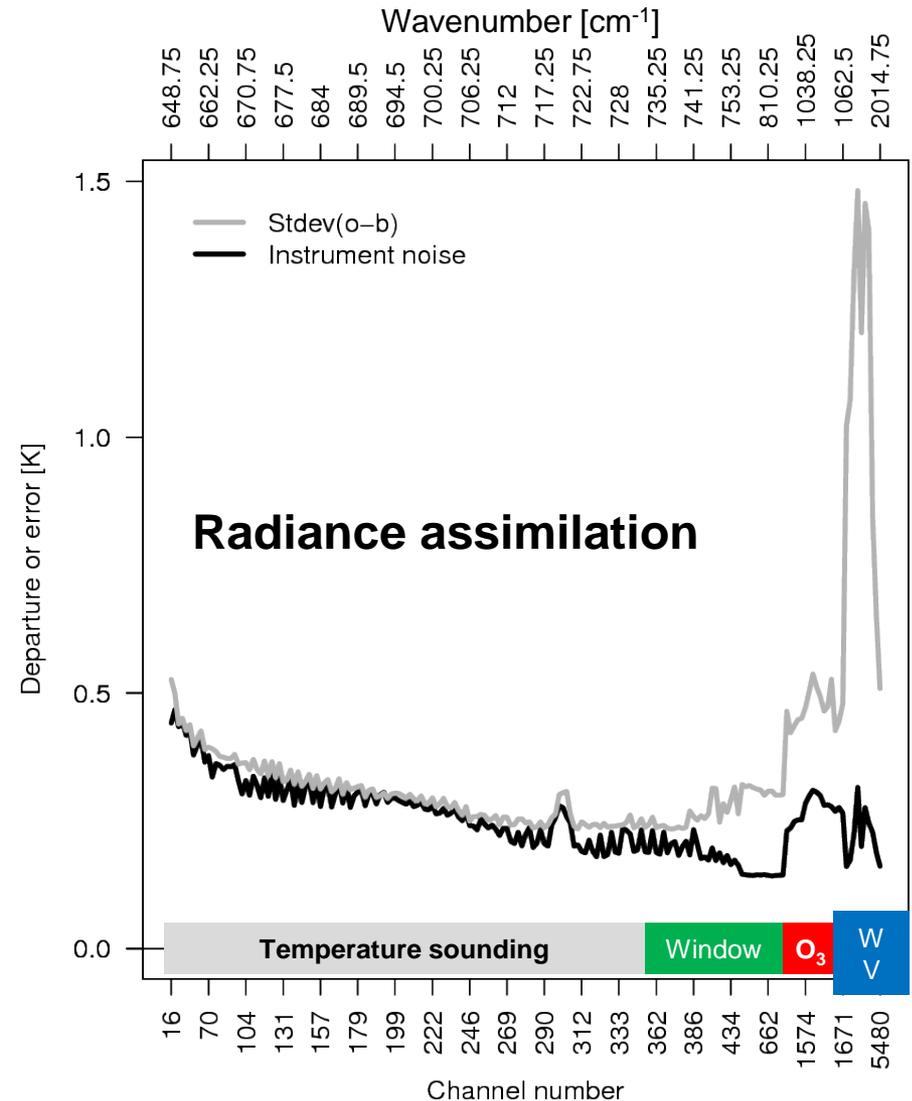
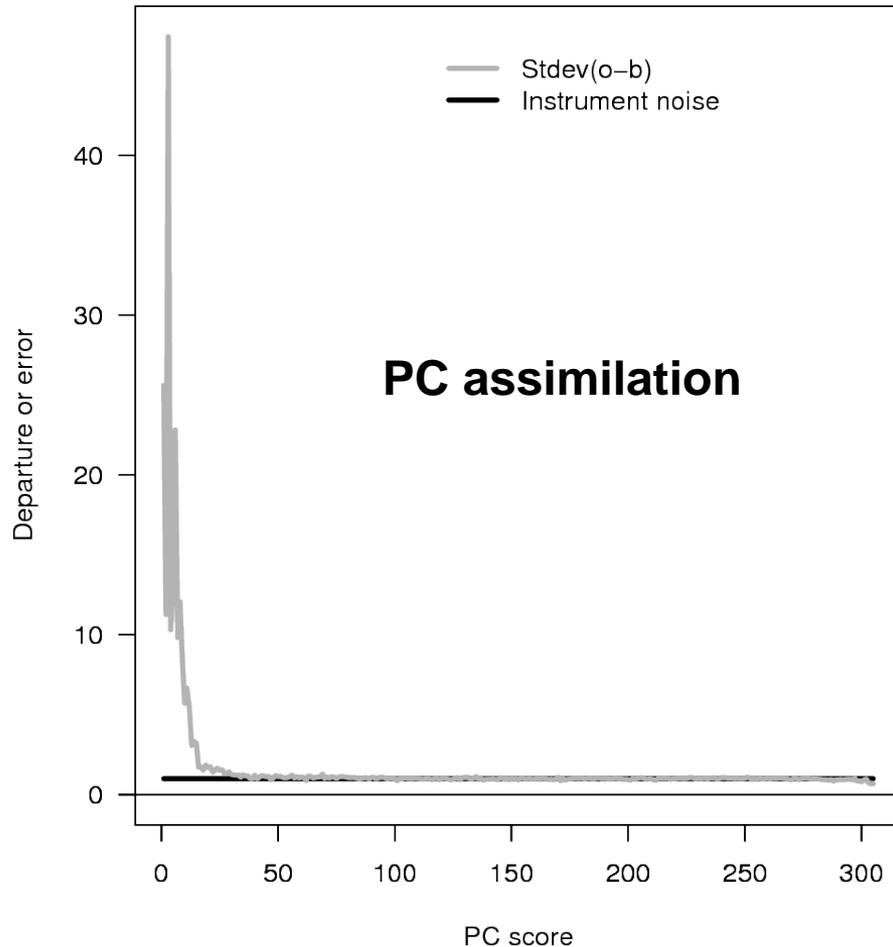
- **What does  $\mathbf{F}$  look like in PC space?**
- **→ Observation-space diagnostics**

# Experiments

- **Diagnostics taken from assimilation systems with the full observing system (19 June – 19 July 2012):**
  - **PC-scores assimilation:**
    - Assimilation of 305 PC-scores derived from **305 channels** from IASI bands 1 & 2
    - Assimilation of **completely clear scenes** only; **new cloud detection**
    - → Marco Matricardi's talk yesterday
  - **Radiance assimilation:**
    - Assimilation of brightness temperatures from **191 channels** (as performed in operations).
    - Assimilation of **clear channels and overcast scenes**
- **Error diagnostics with Hollingsworth/Lönnberg method from completely clear scenes (Desroziers gives qualitatively similar results).**

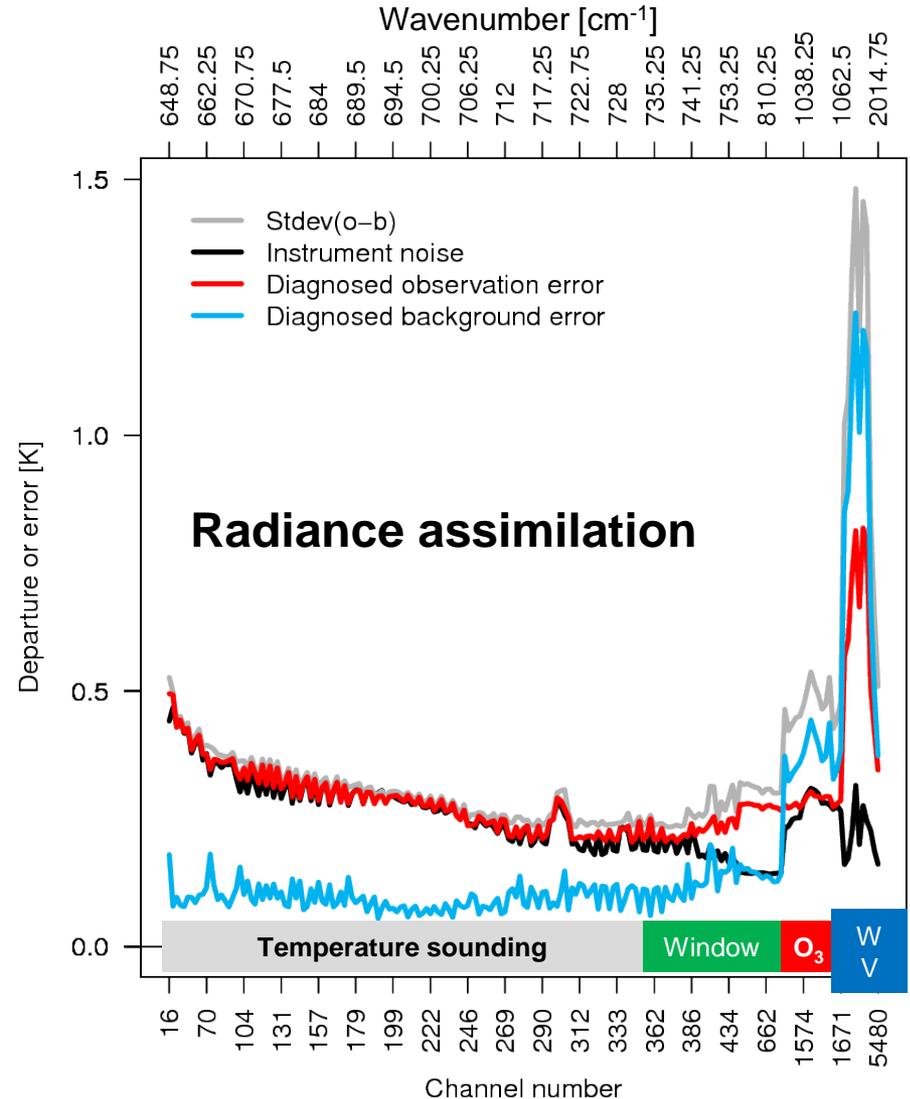
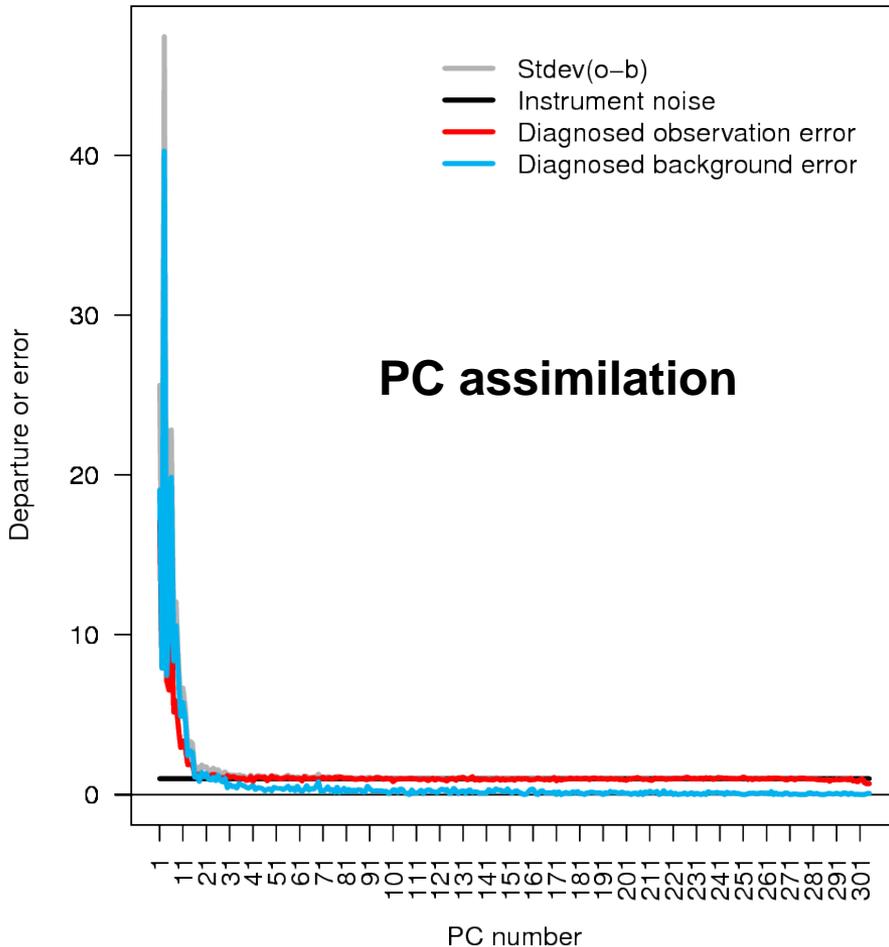
# Background departures

B1 + B2 PCs



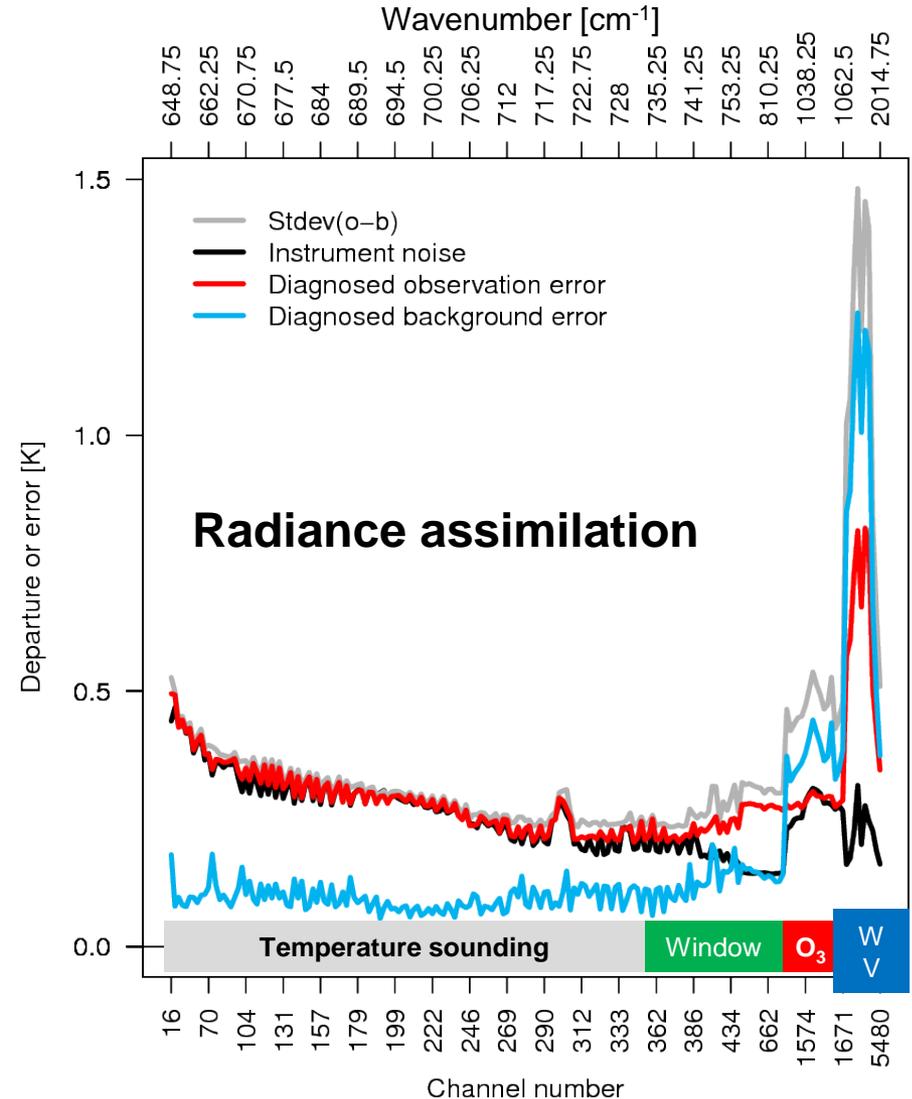
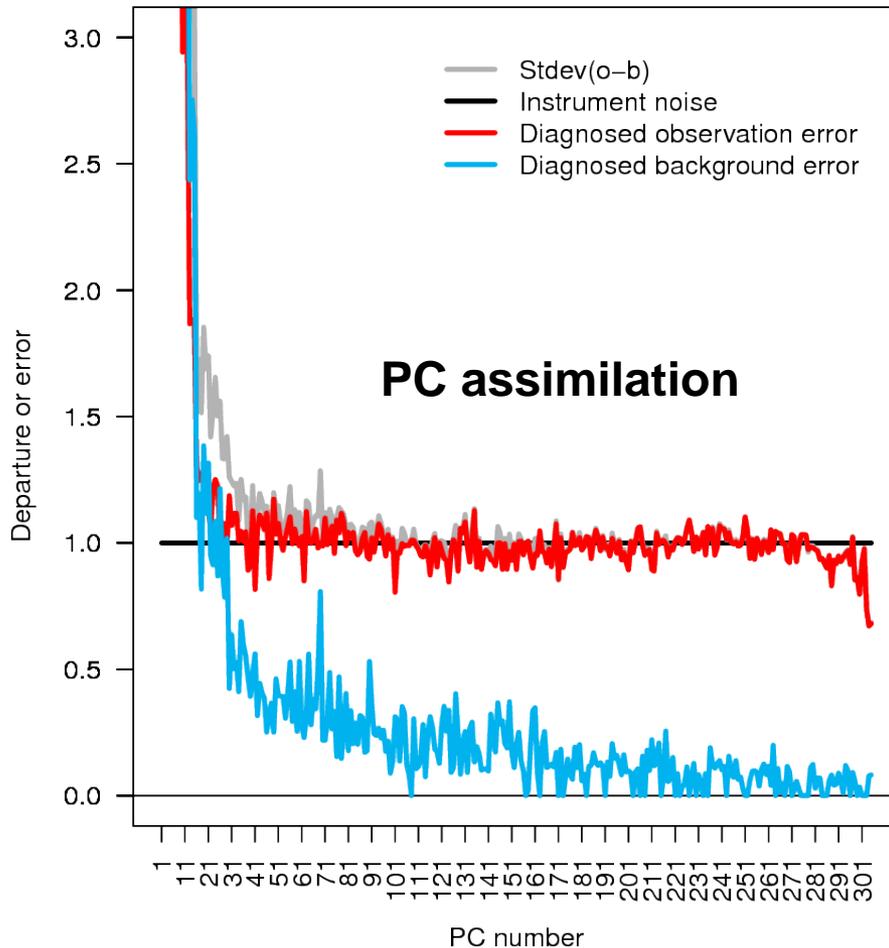
# Diagnosed background and observation error

B1 & B2 PCs



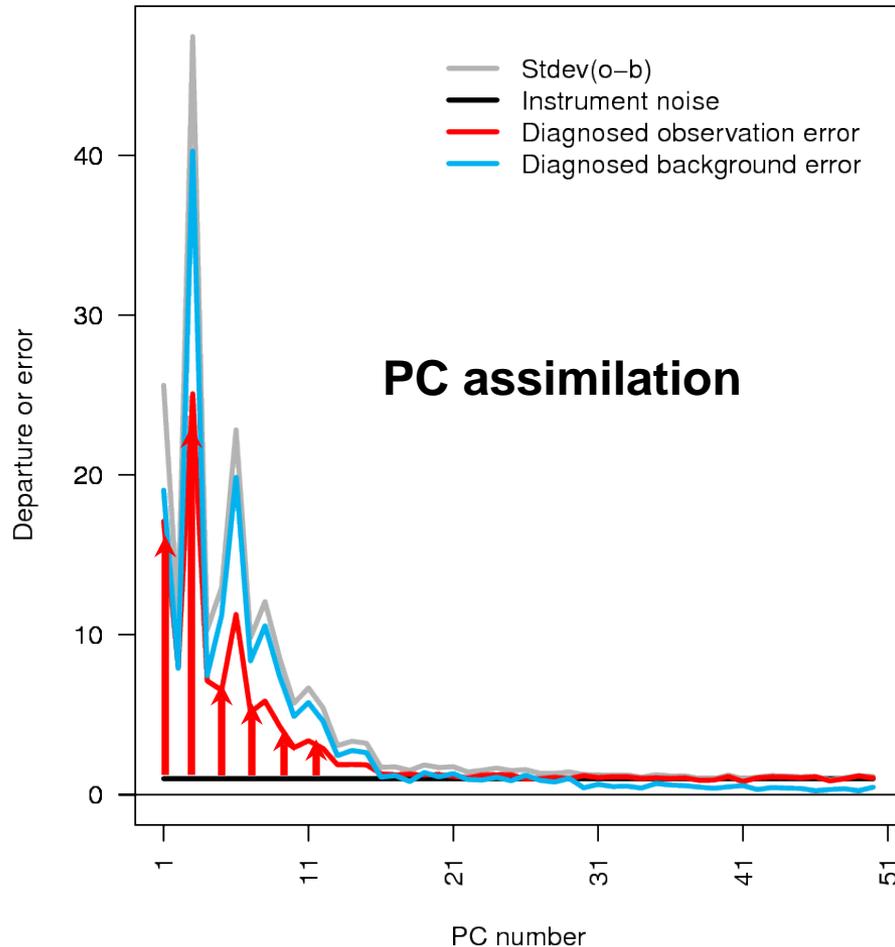
# Diagnosed background and observation error

B1 & B2 PCs

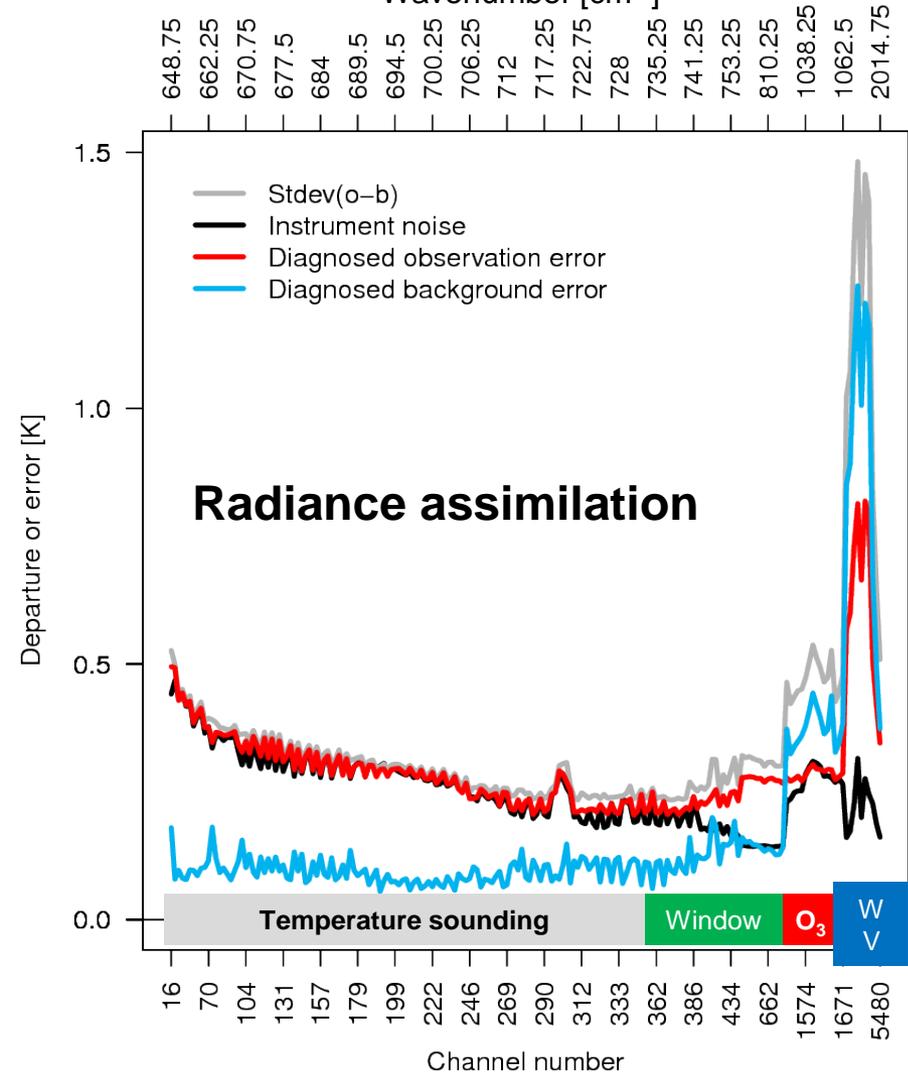


# Diagnosed background and observation error

B1 & B2 PCs



Wavenumber [cm<sup>-1</sup>]



# Diagnostics: Some points

- **For raw radiance assimilation:**

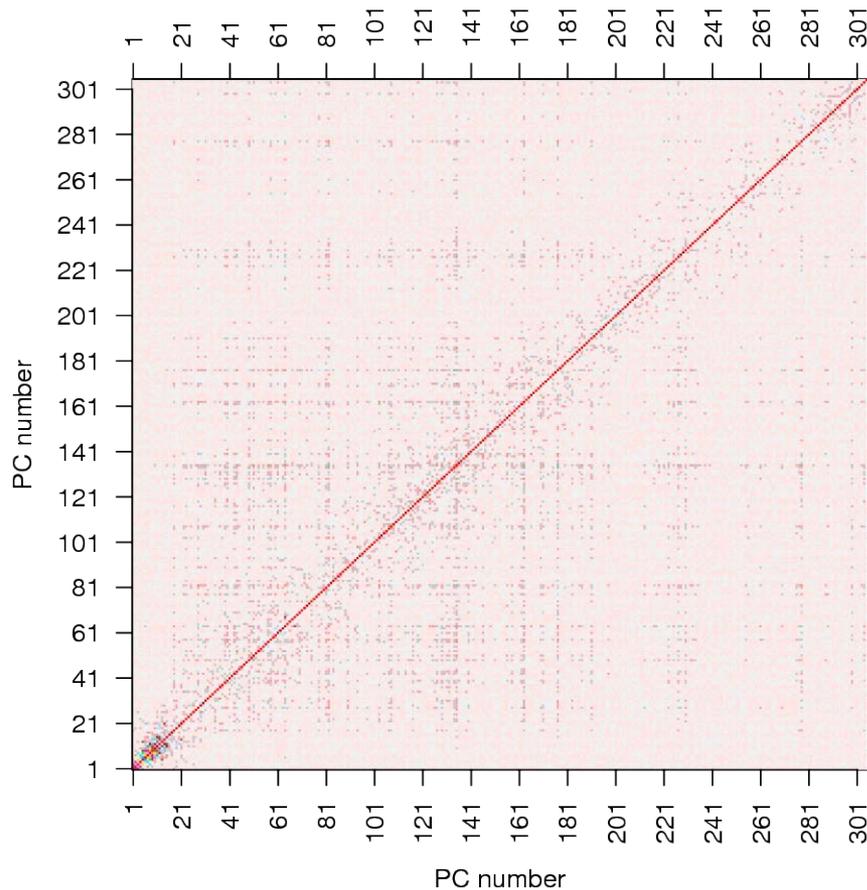
- **Background error small for T-sounding; instrument noise dominates observation errors.**
- **Significant contribution from “other” errors for window channels, H<sub>2</sub>O, O<sub>3</sub>.**
- **Background errors larger than observation errors for window channels, H<sub>2</sub>O.**

- **For PC-scores assimilation:**

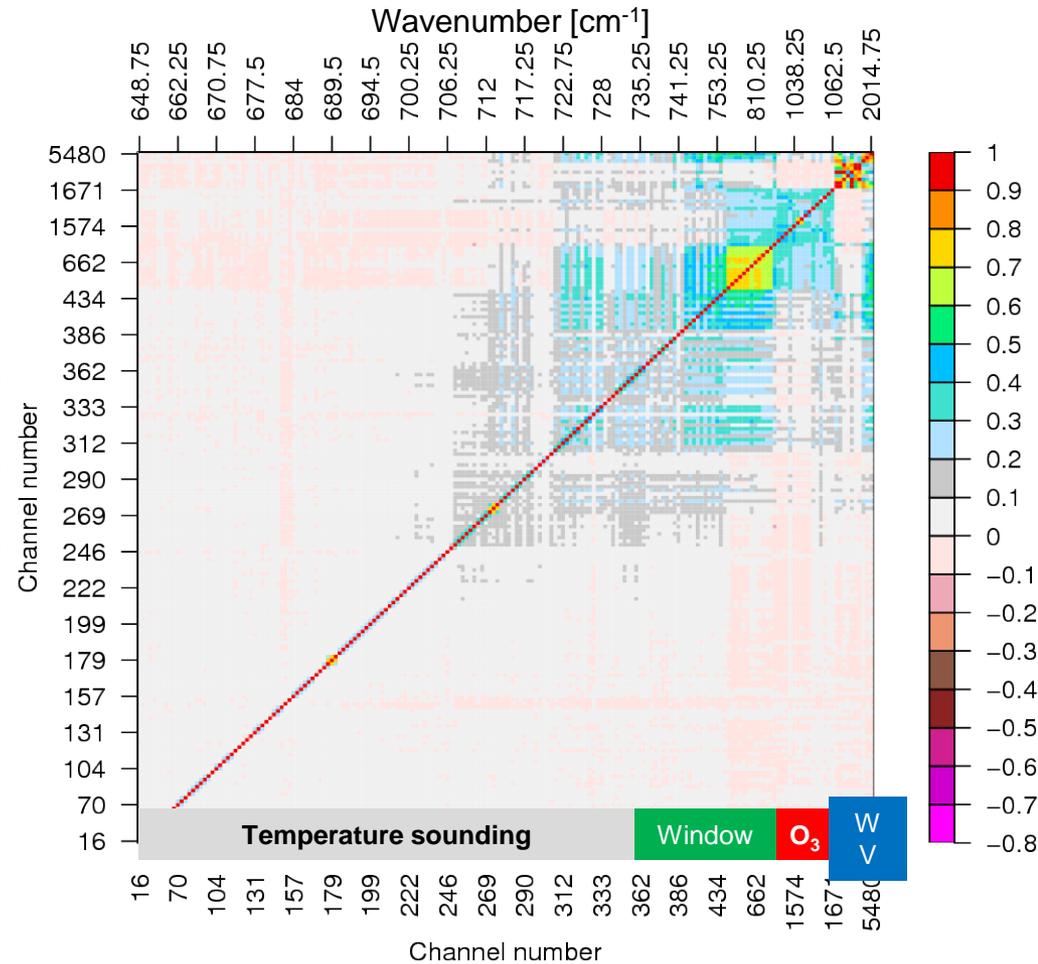
- **Background and observation error comparable for leading PC-scores.**
- **Significant contribution from “other” errors for leading PC-scores.**
- **Instrument noise dominates for higher-order PC-scores.**

# Diagnosed observation error correlations

## PC assimilation

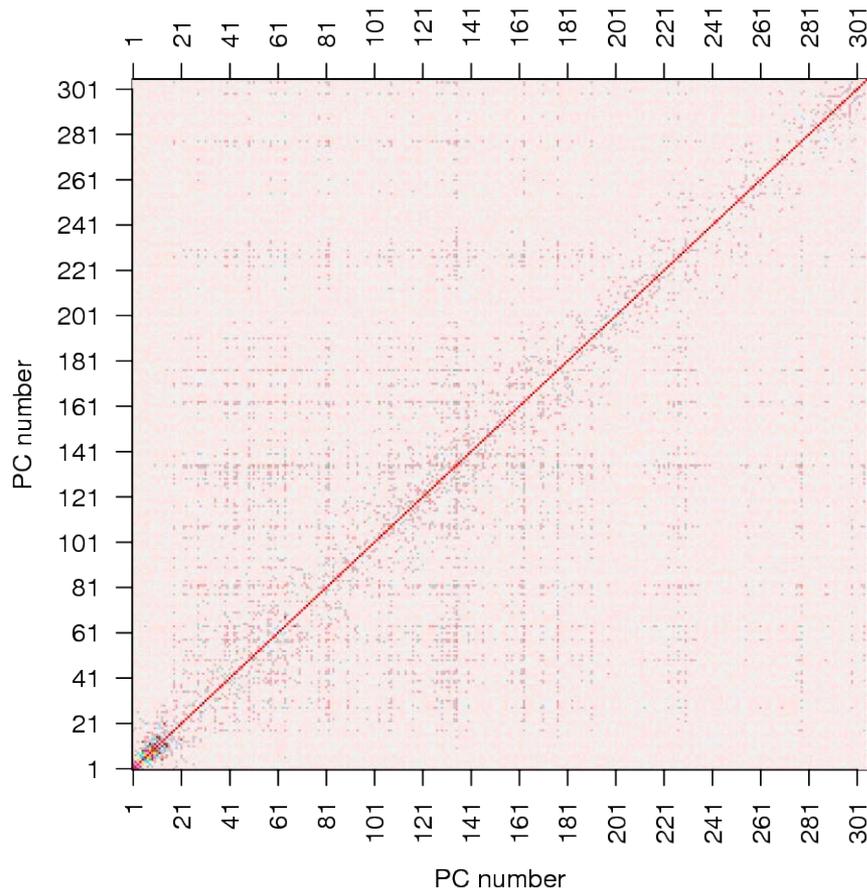


## Radiance assimilation

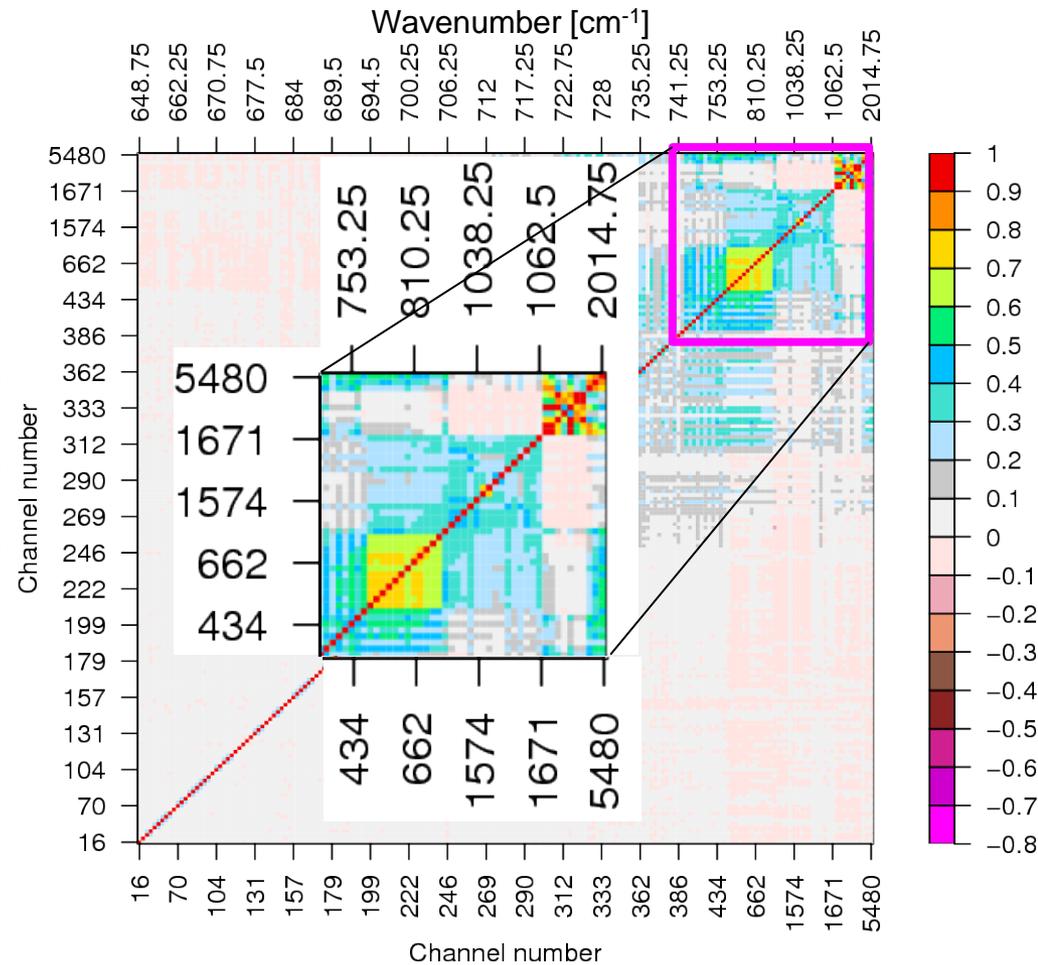


# Diagnosed observation error correlations

## PC assimilation

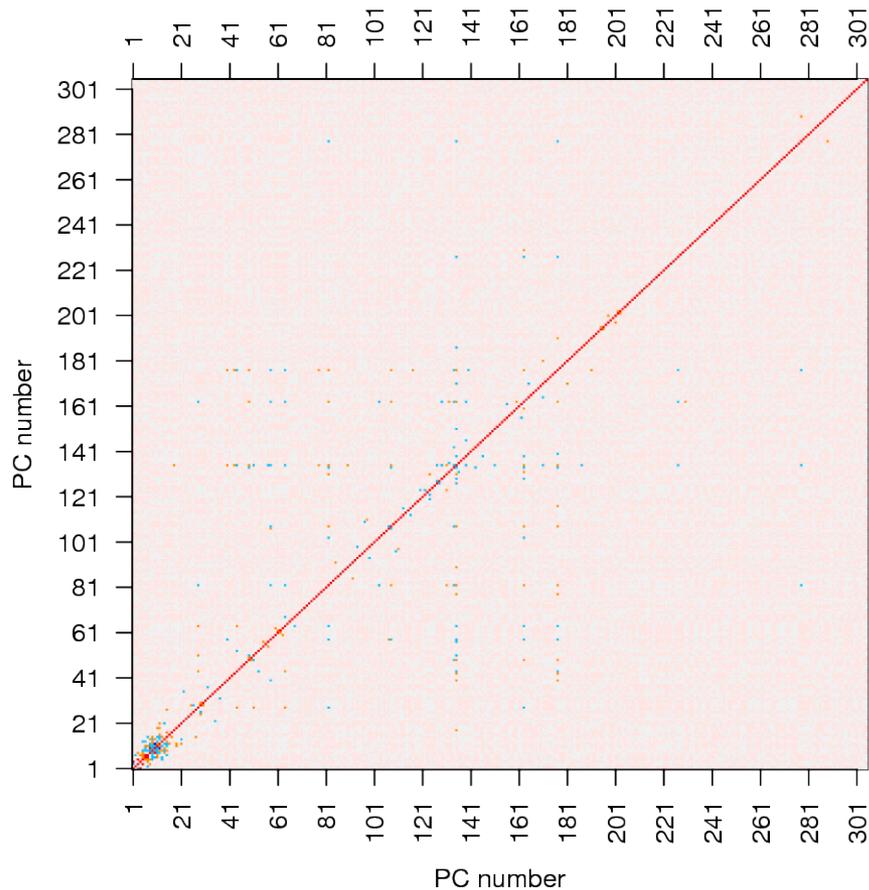


## Radiance assimilation

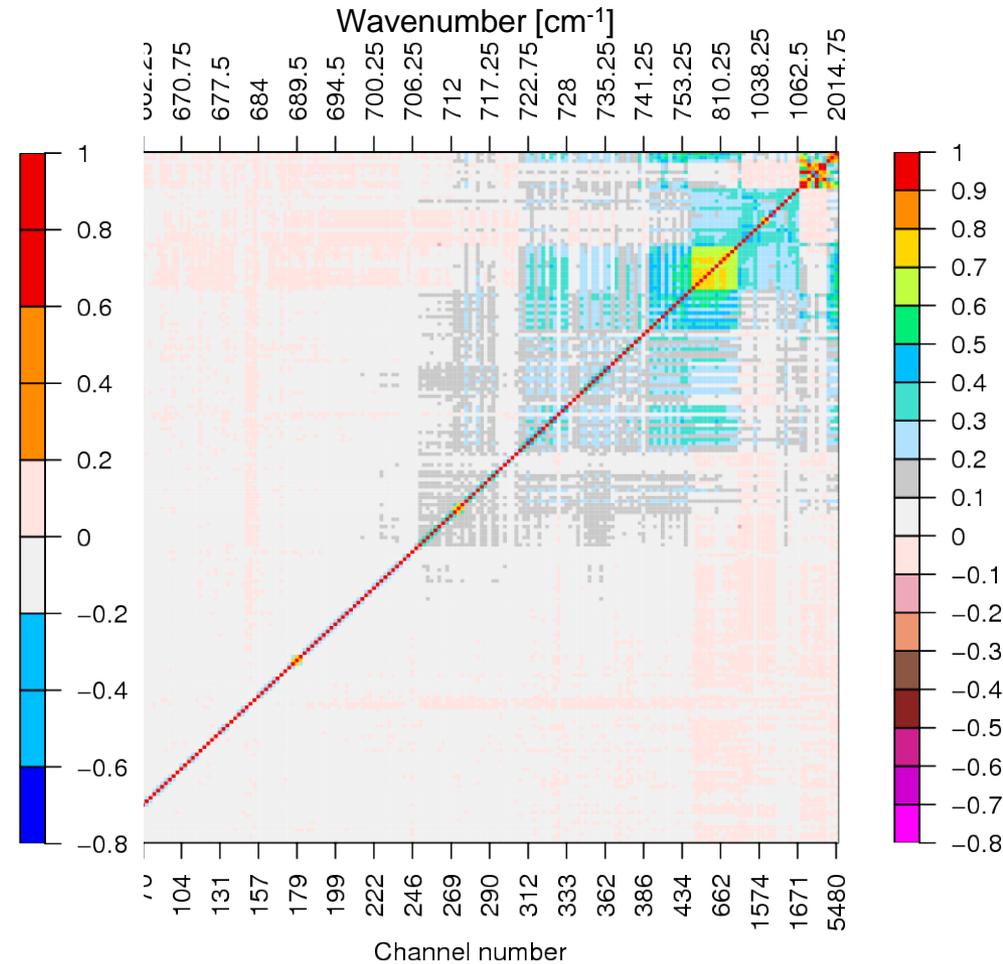


# Diagnosed observation error correlations

## PC assimilation

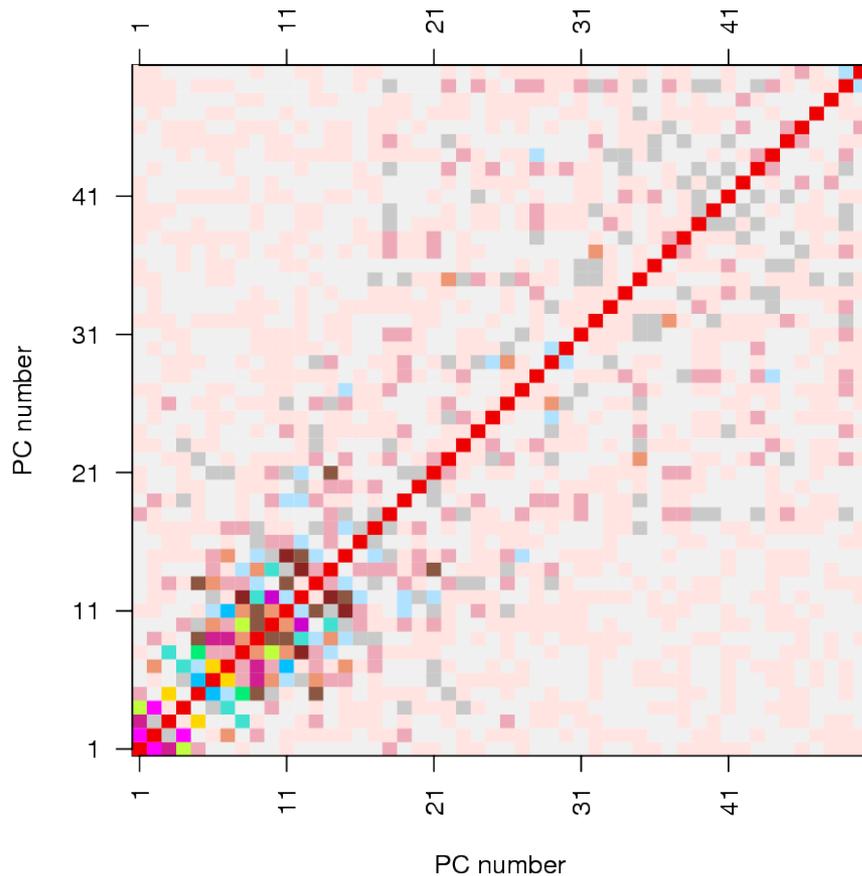


## Radiance assimilation

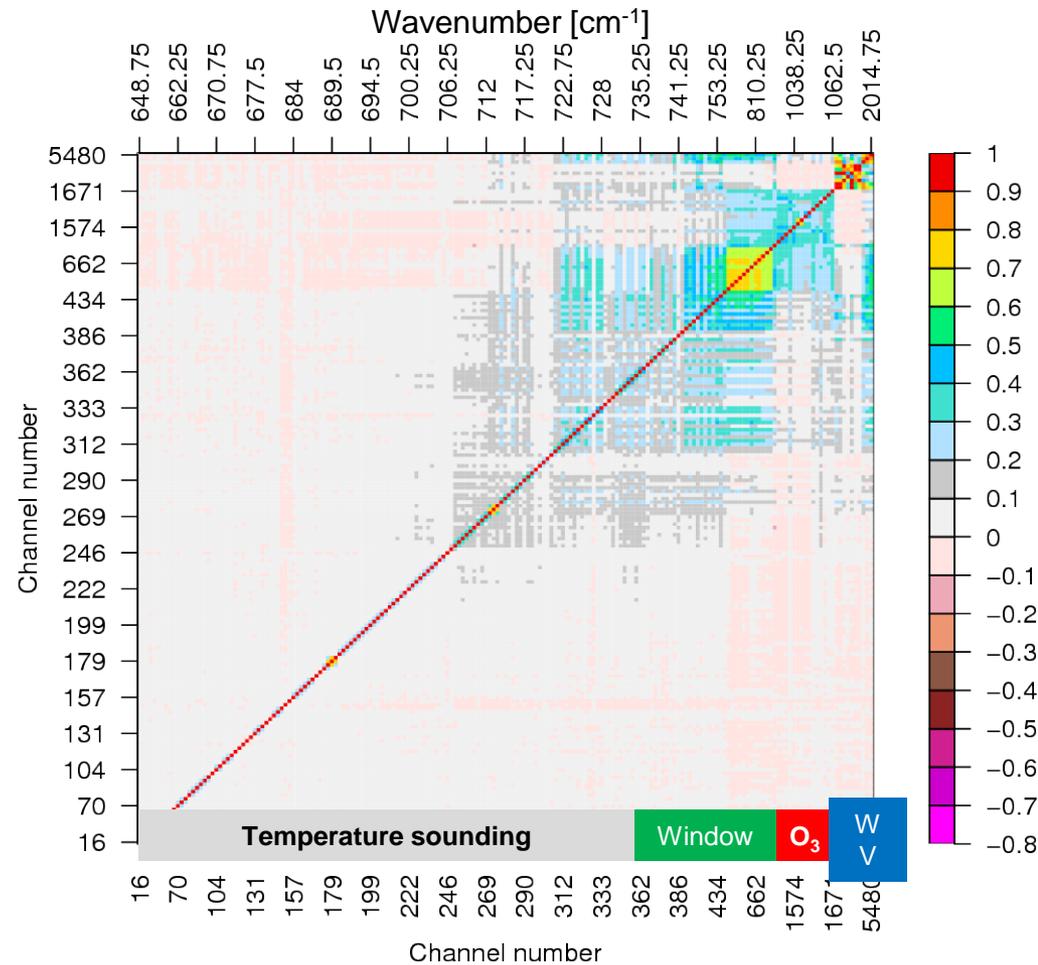


# Diagnosed observation error correlations

## PC assimilation



## Radiance assimilation



**How do the *diagnosed* observation errors compare  
in brightness temperature space?**

# Conversion PC scores ↔ brightness temperatures

- From radiances to PC-space:

$$\mathbf{y}_{PC} = \mathbf{U} \mathbf{N}^{-1/2} (\mathbf{y}_{Rad} - \overline{\mathbf{y}_{Rad}})$$

- $\mathbf{y}$  – observations
- $\mathbf{U}$  – matrix with rows of eigenvectors of covariance matrix
- $\mathbf{N}$  – covariance of instrument noise

- Convert observation error covariance  $\mathbf{R}$  diagnosed in PC-space to radiance space:

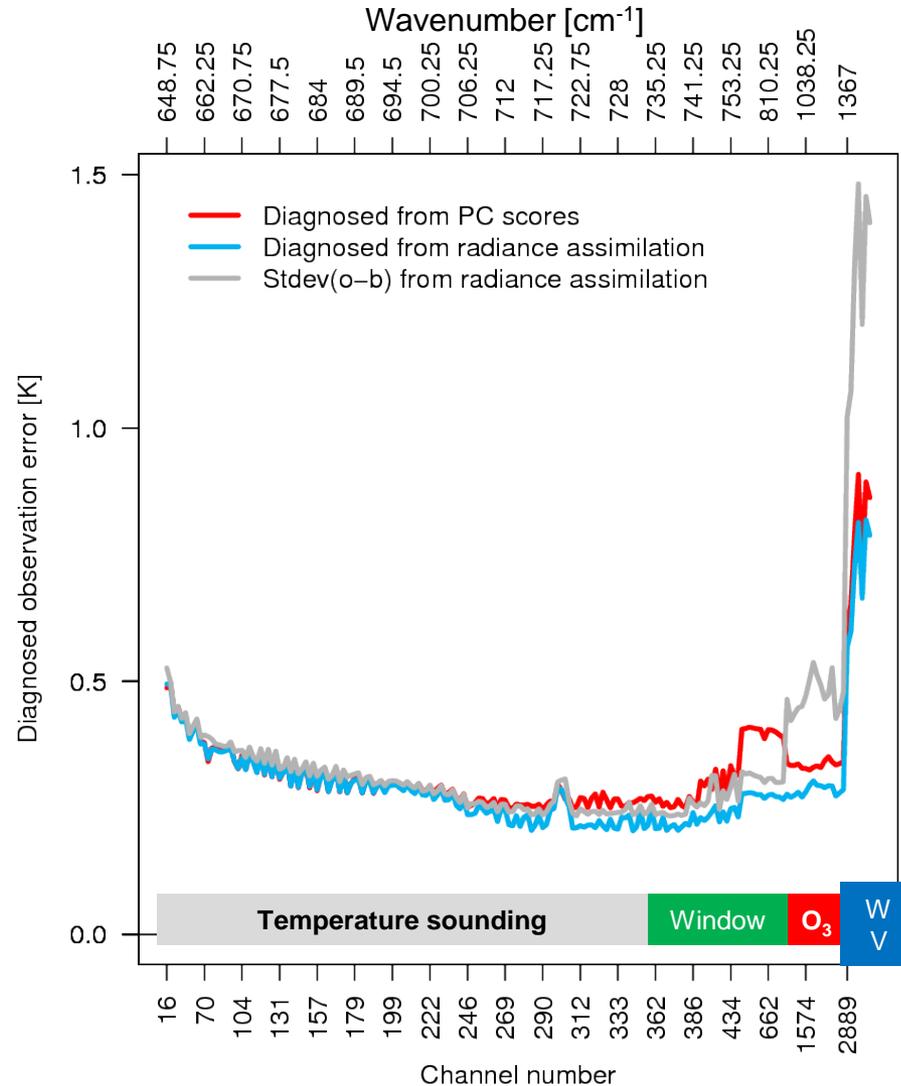
$$\mathbf{R}_{Rad} = \mathbf{U}^T \mathbf{N}^{-1/2} \mathbf{R}_{PC} (\mathbf{N}^{-1/2})^T \mathbf{U}$$

- Conversion to brightness temperature space:

$$\mathbf{R}_{BT} = \mathbf{P} \mathbf{R}_{Rad} \mathbf{P}^T$$

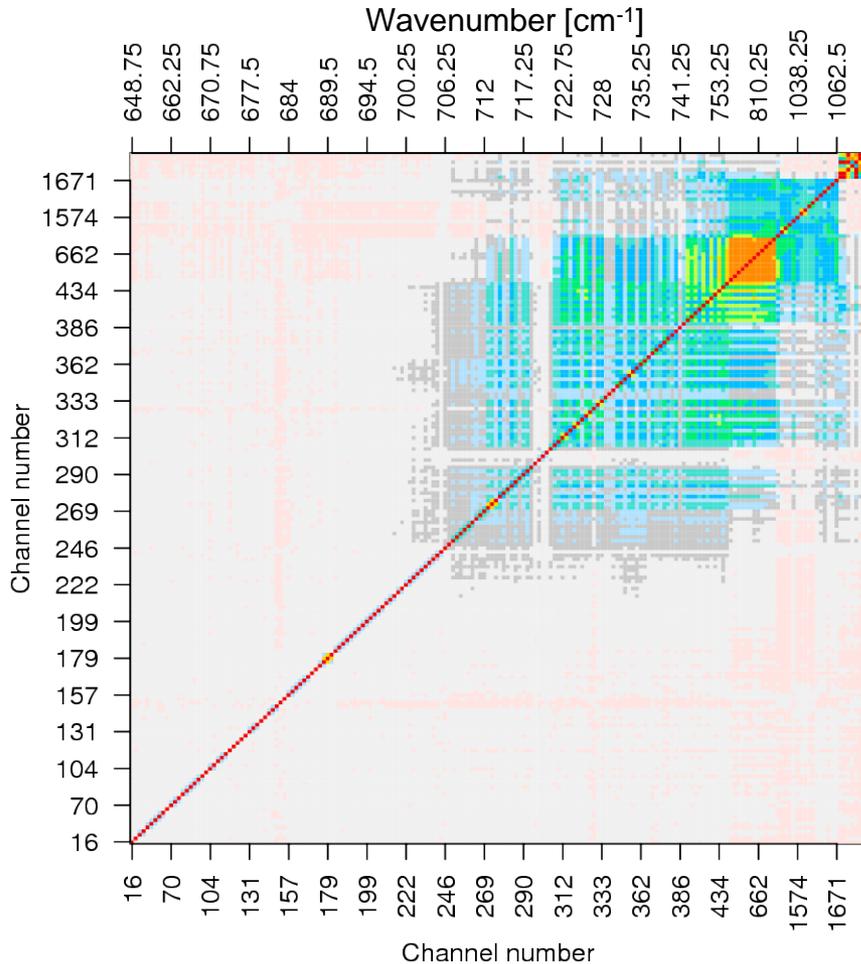
$\mathbf{P}$  – Jacobian of the inverse Planck function at mean scene temperature

# Diagnosed observation errors, subsampled for common channel set

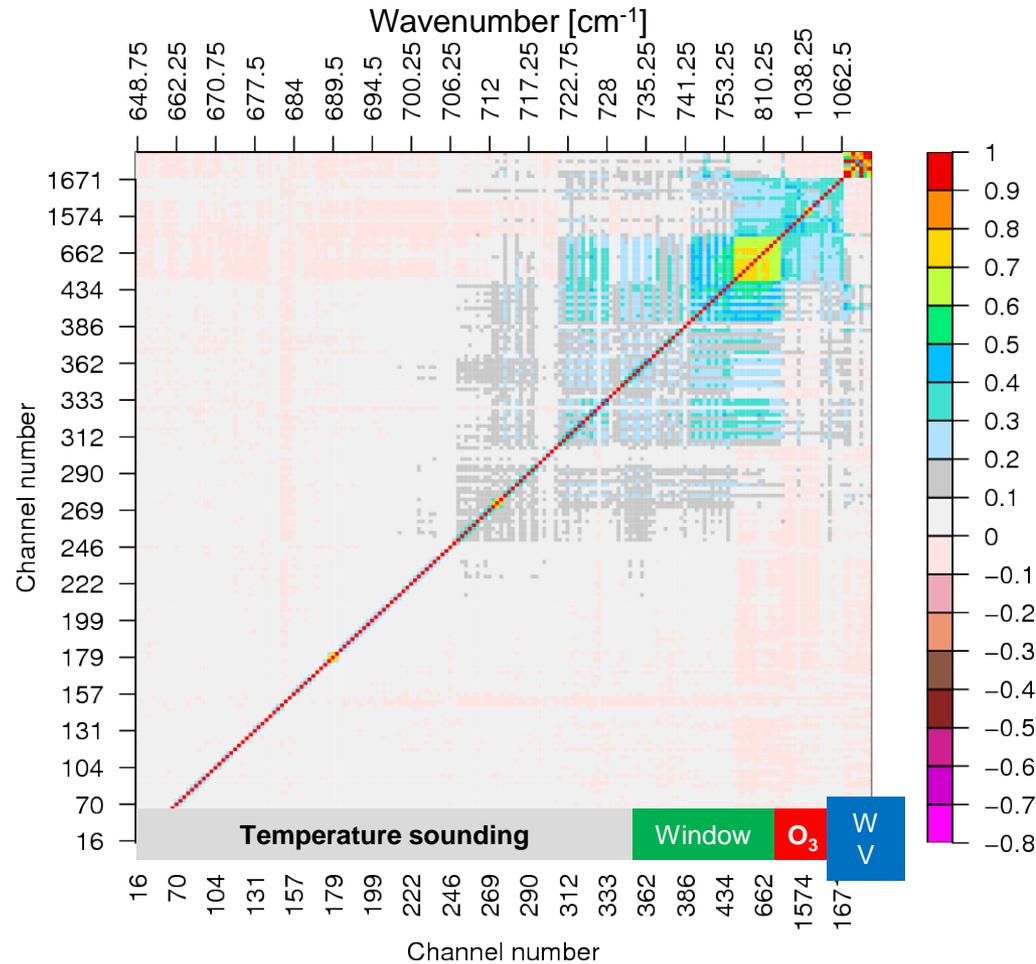


# Diagnosed observation error correlations, subsampled for common channel set

## PC assimilation, converted to radiance space

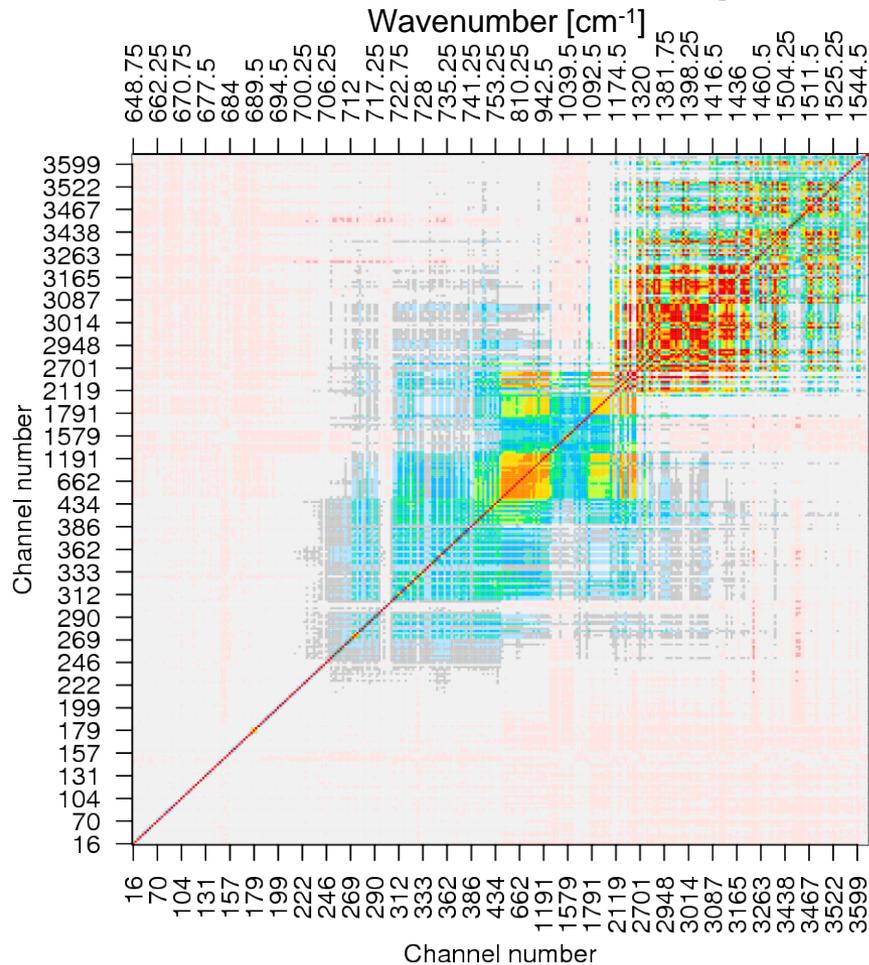


## Radiance assimilation, common channels only

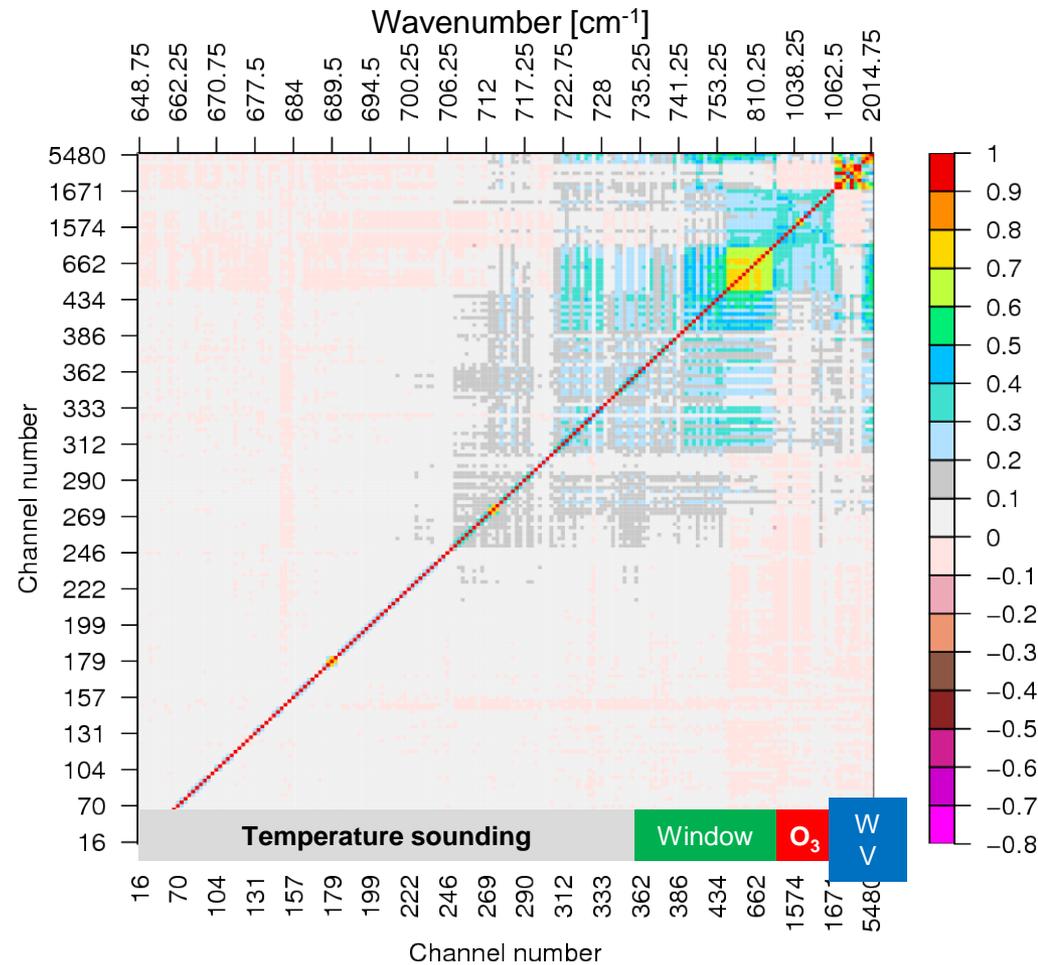


# Diagnosed observation error correlations

## PC assimilation, converted to radiance space

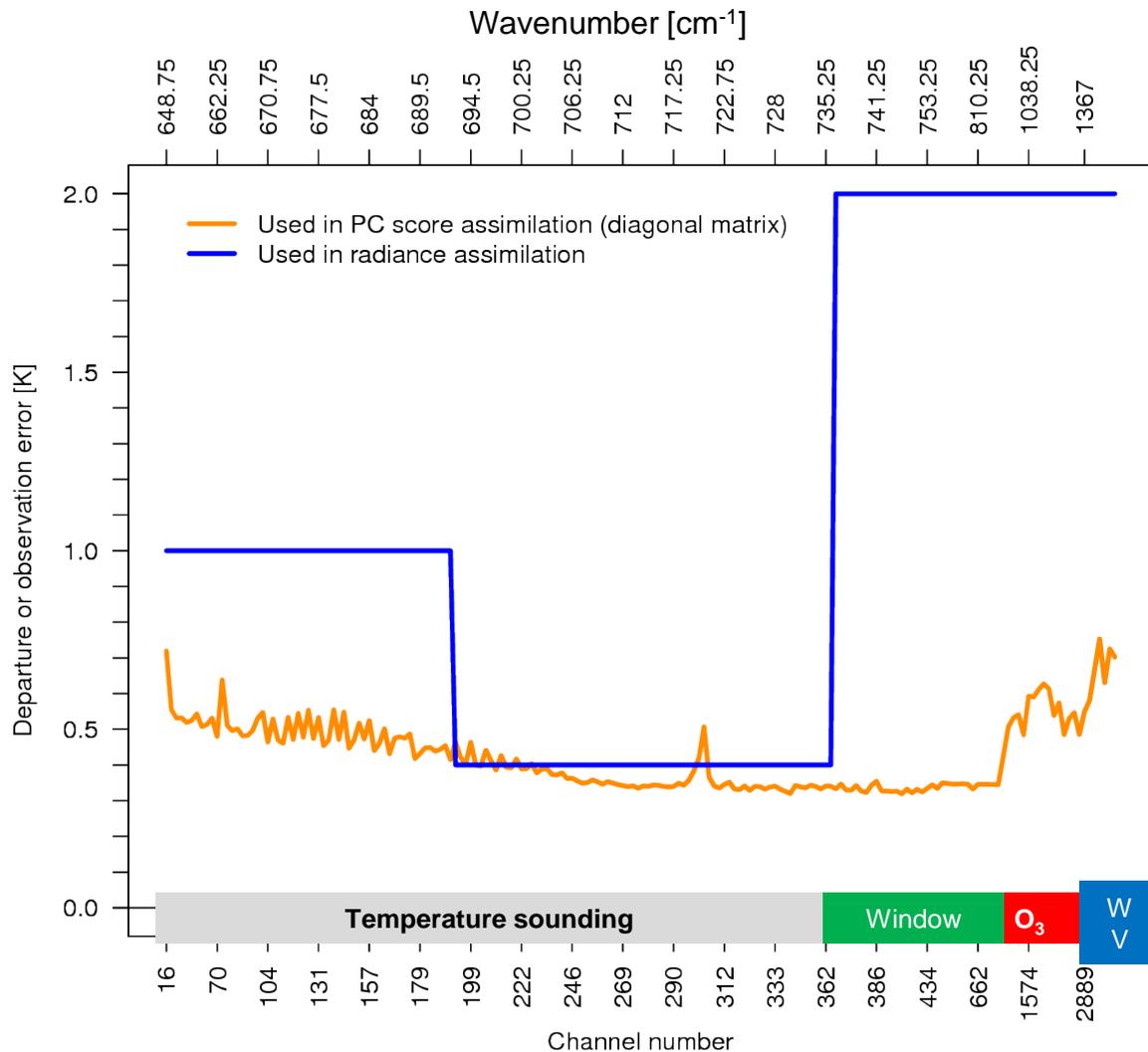


## Radiance assimilation

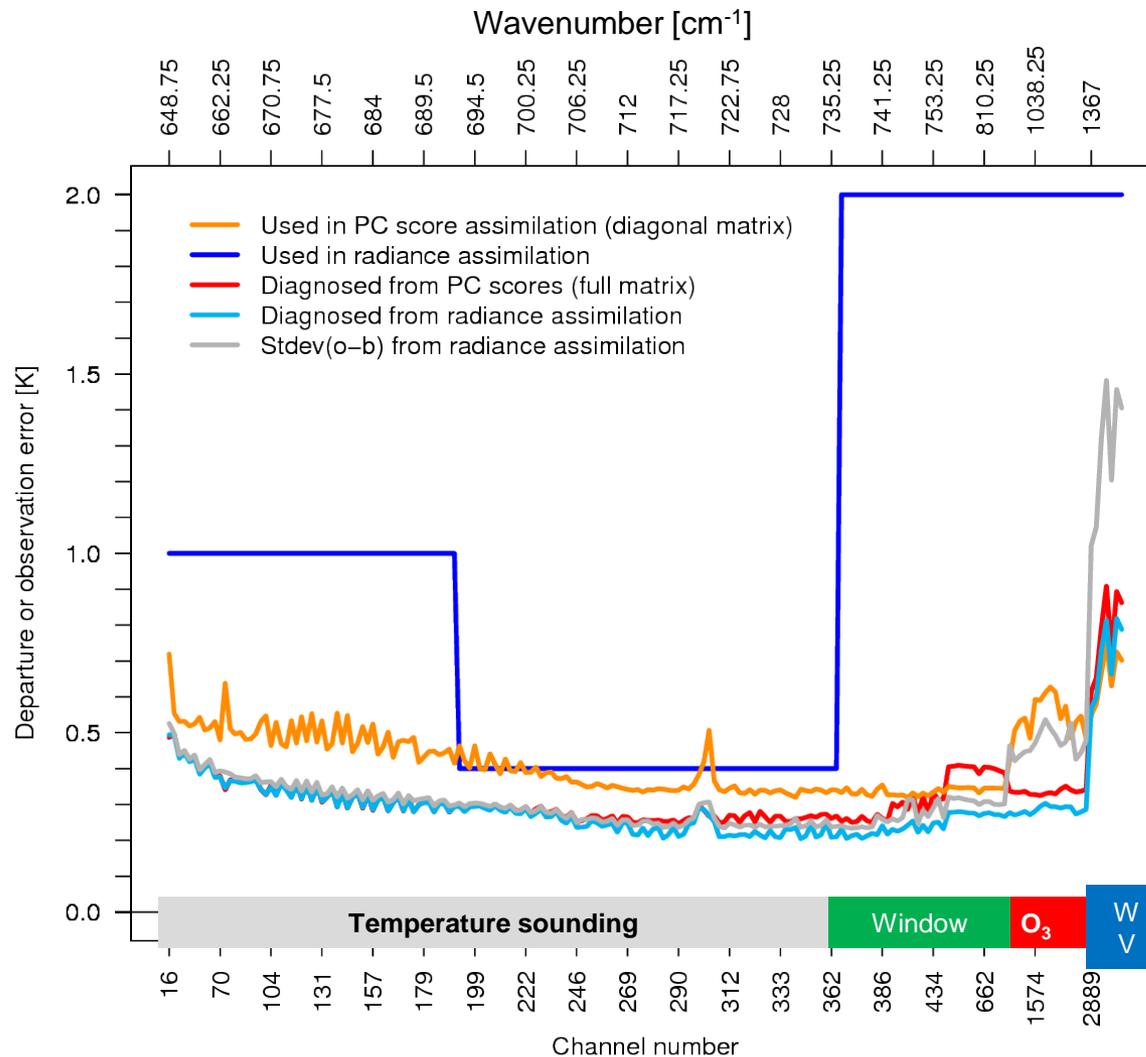


**What do the *assumed* observation errors from the radiance and the PC experiment look like in brightness temperature space?**

# Assumed observation errors (subsampling for common channel set)

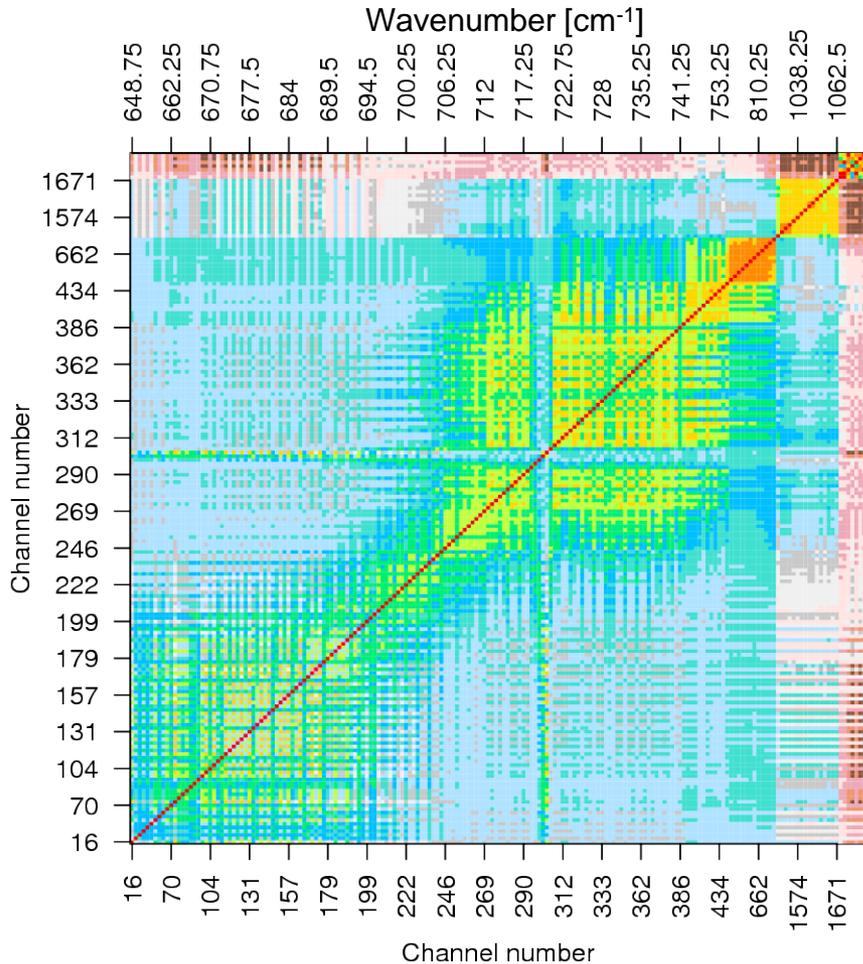


# Assumed observation errors (subsamped for common channel set)

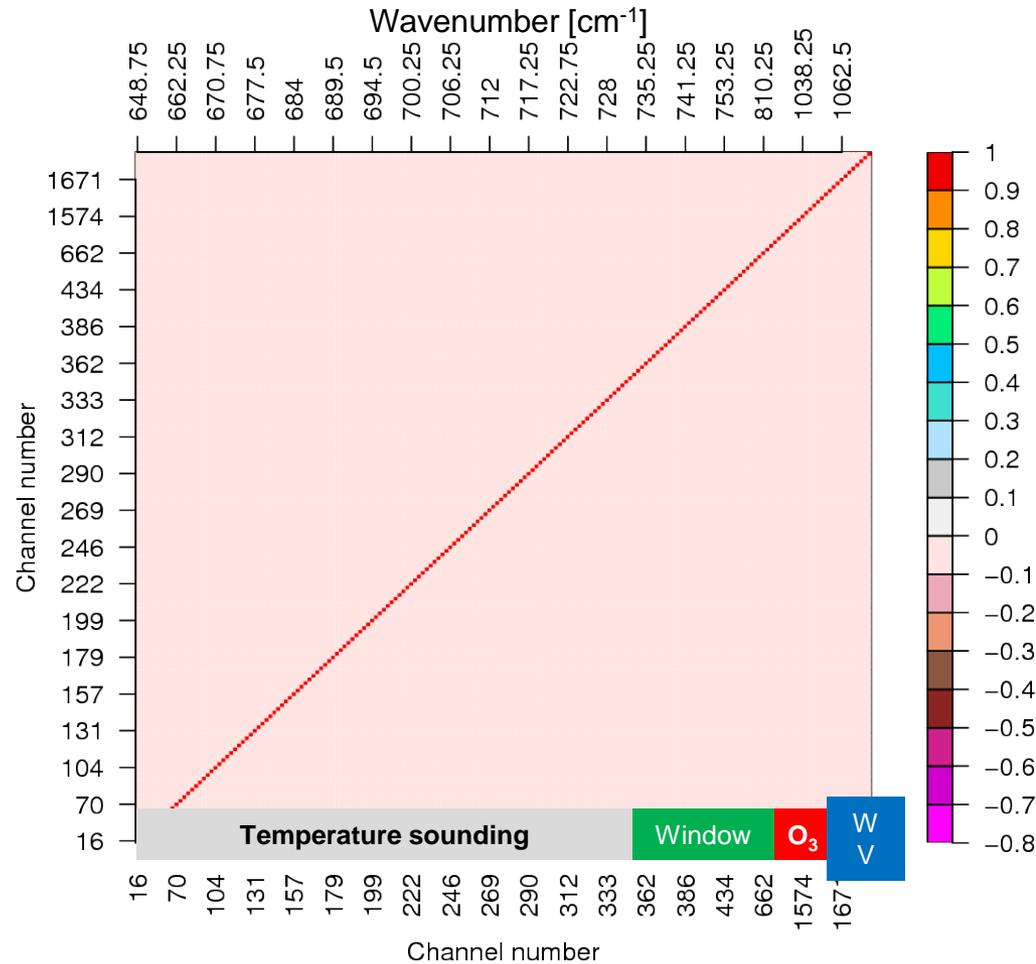


# Assumed observation error correlations (subsamped for common channel set)

**PC assimilation,  
converted to radiance space**

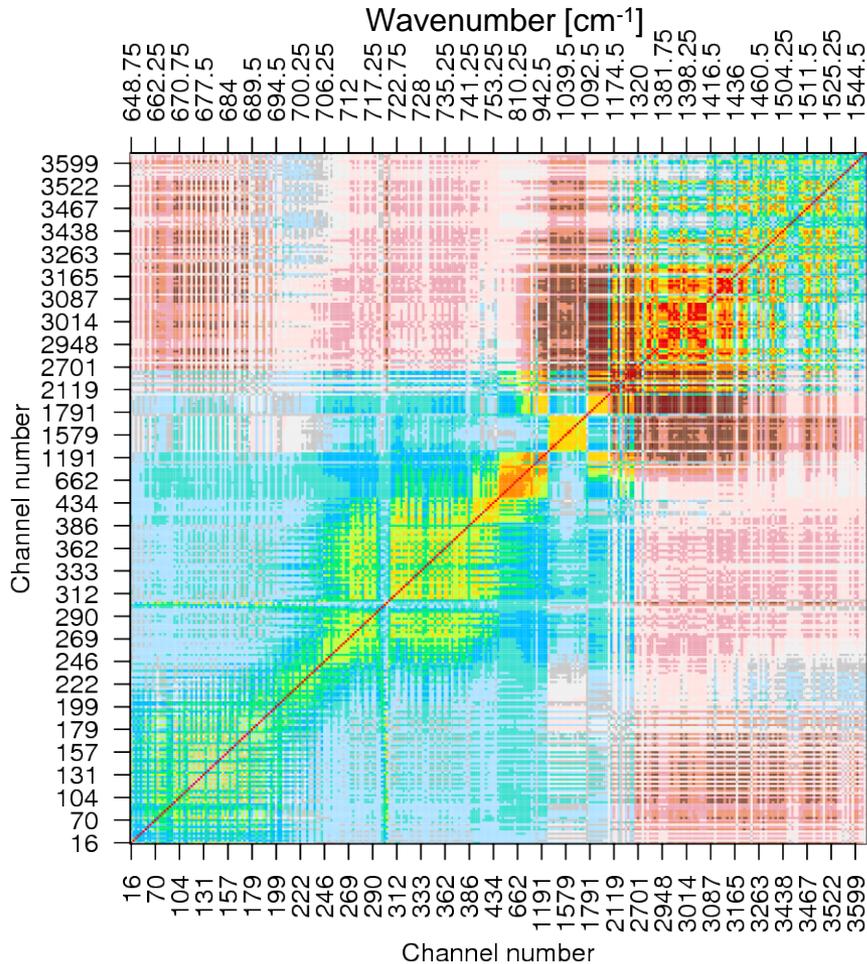


**Radiance assimilation**

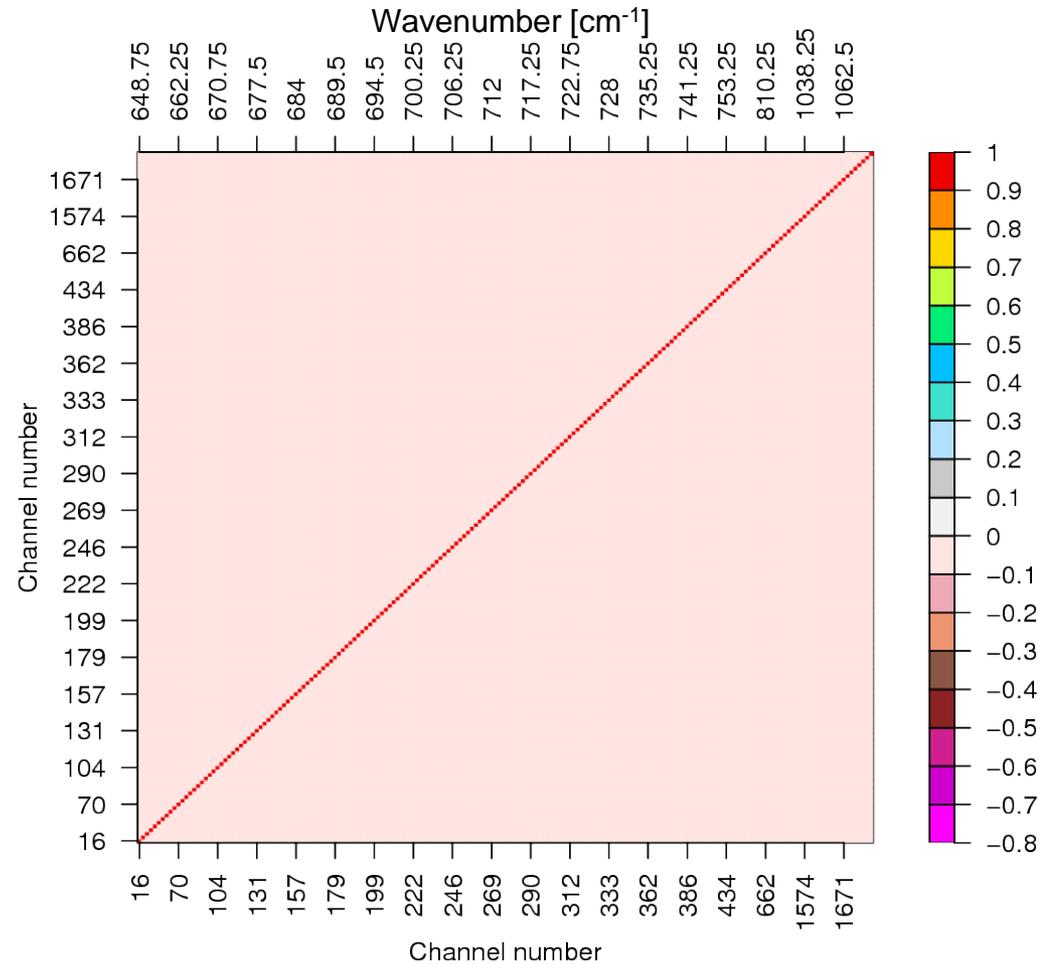


# Assumed observation error correlations

## PC assimilation, converted to radiance space

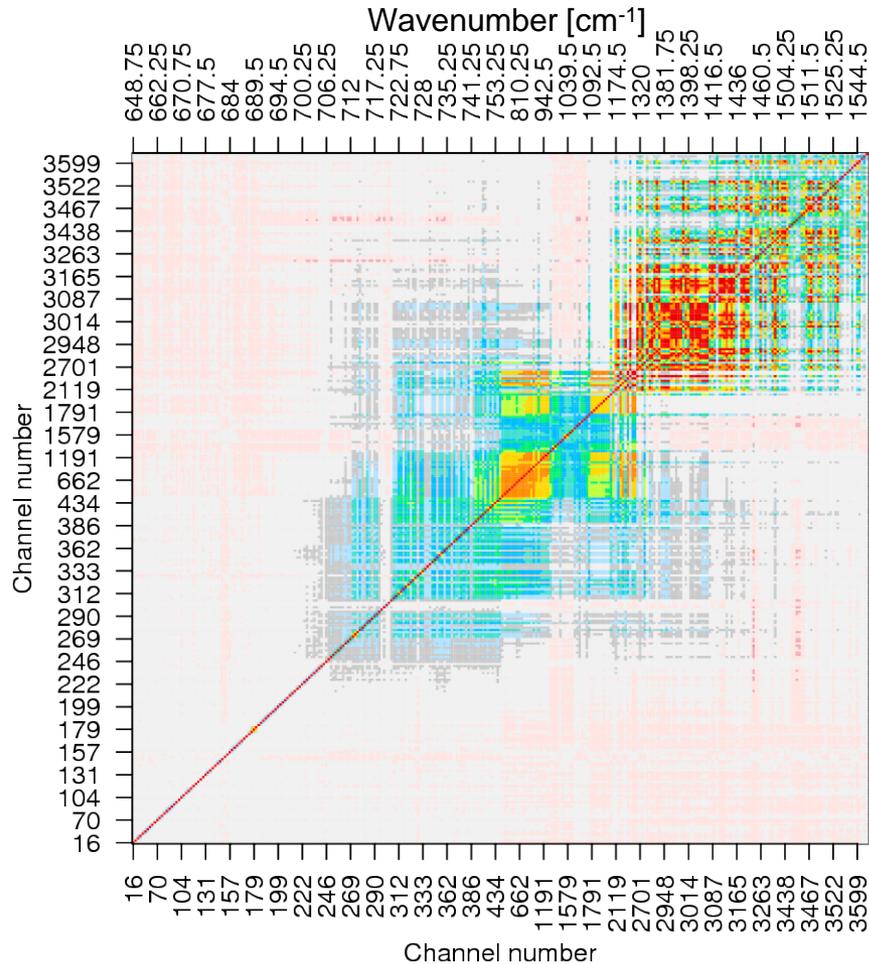


## Radiance assimilation

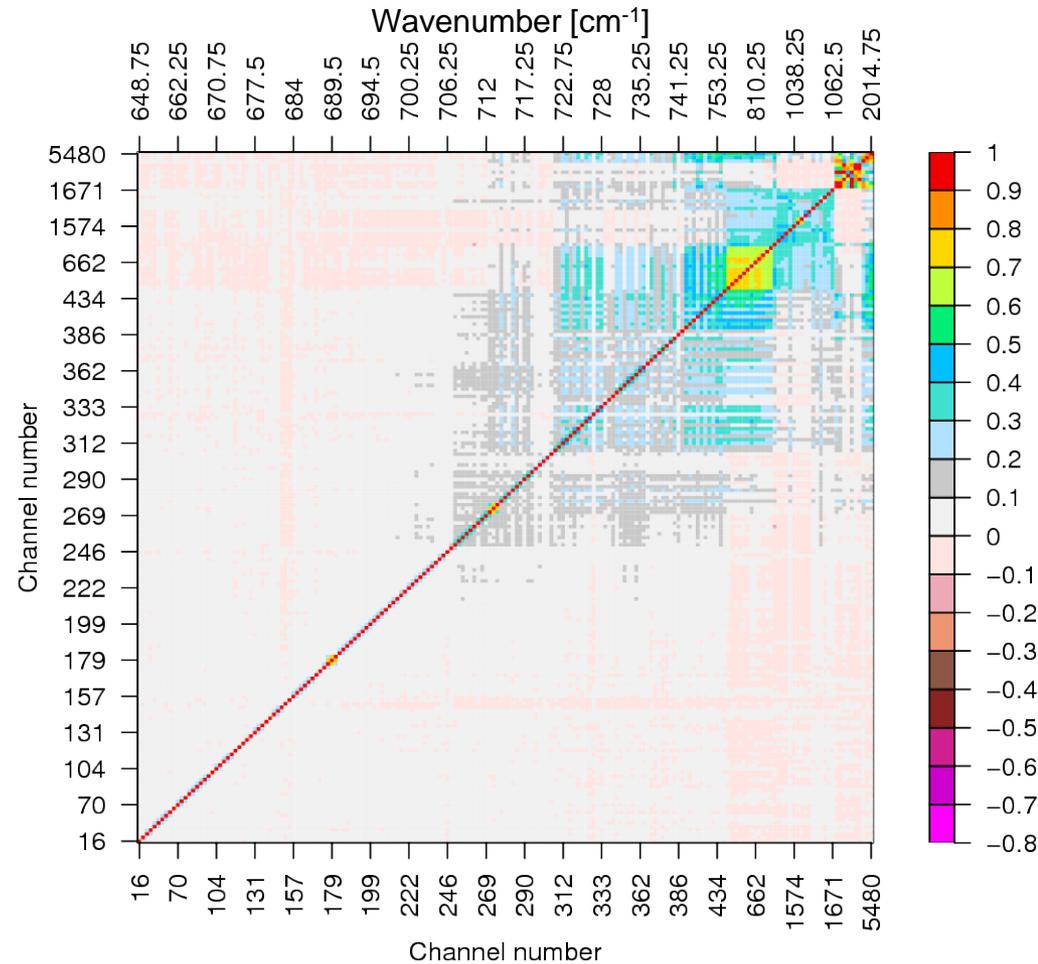


# Diagnosed observation error correlations

## PC assimilation, converted to radiance space

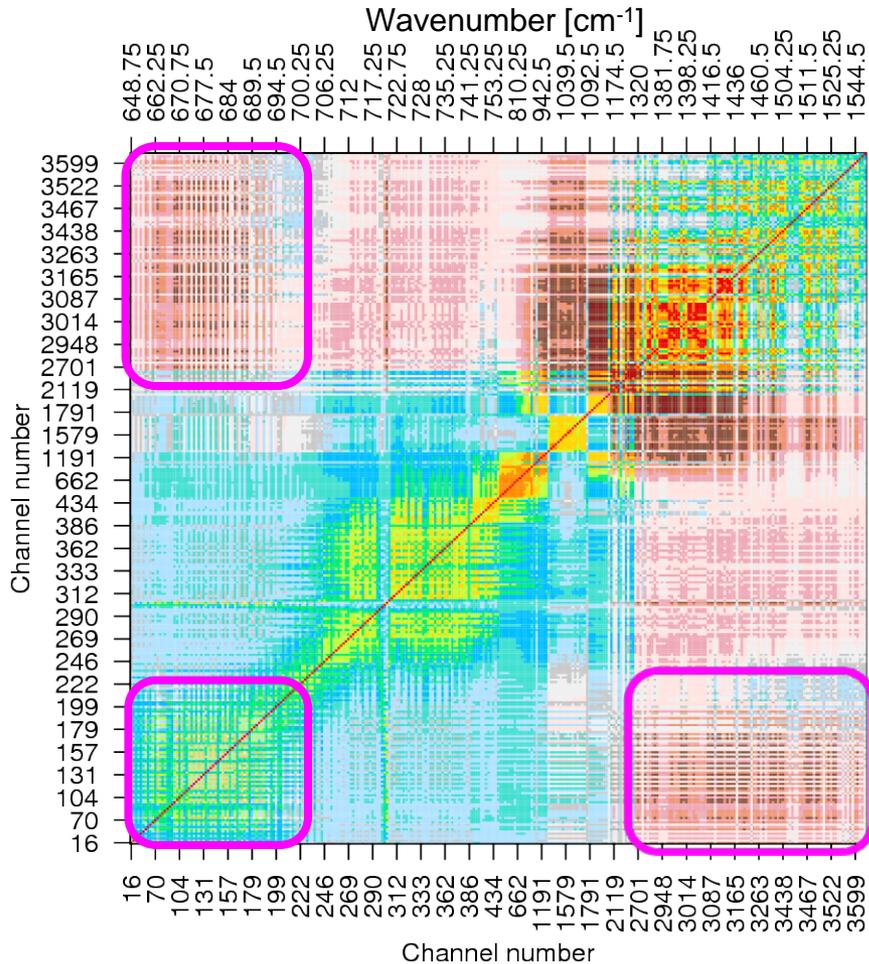


## Radiance assimilation

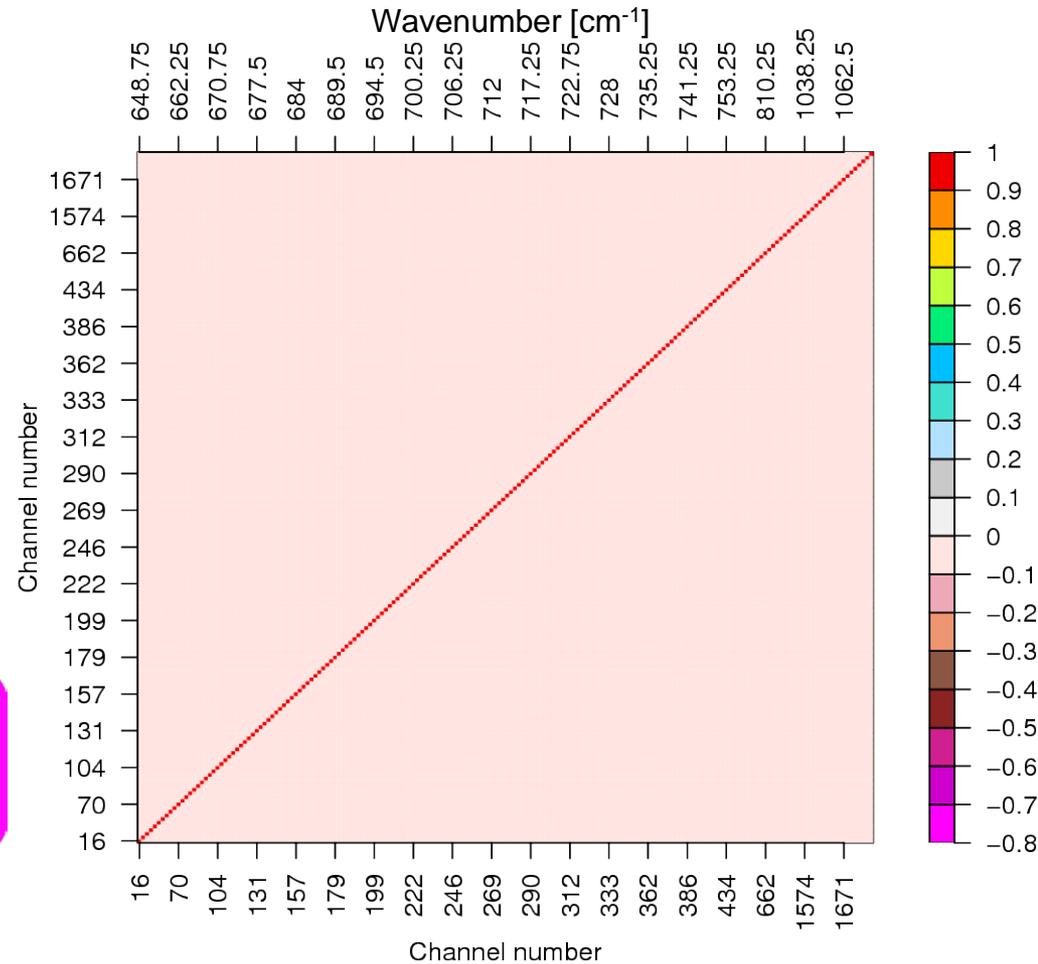


# Assumed observation error correlations

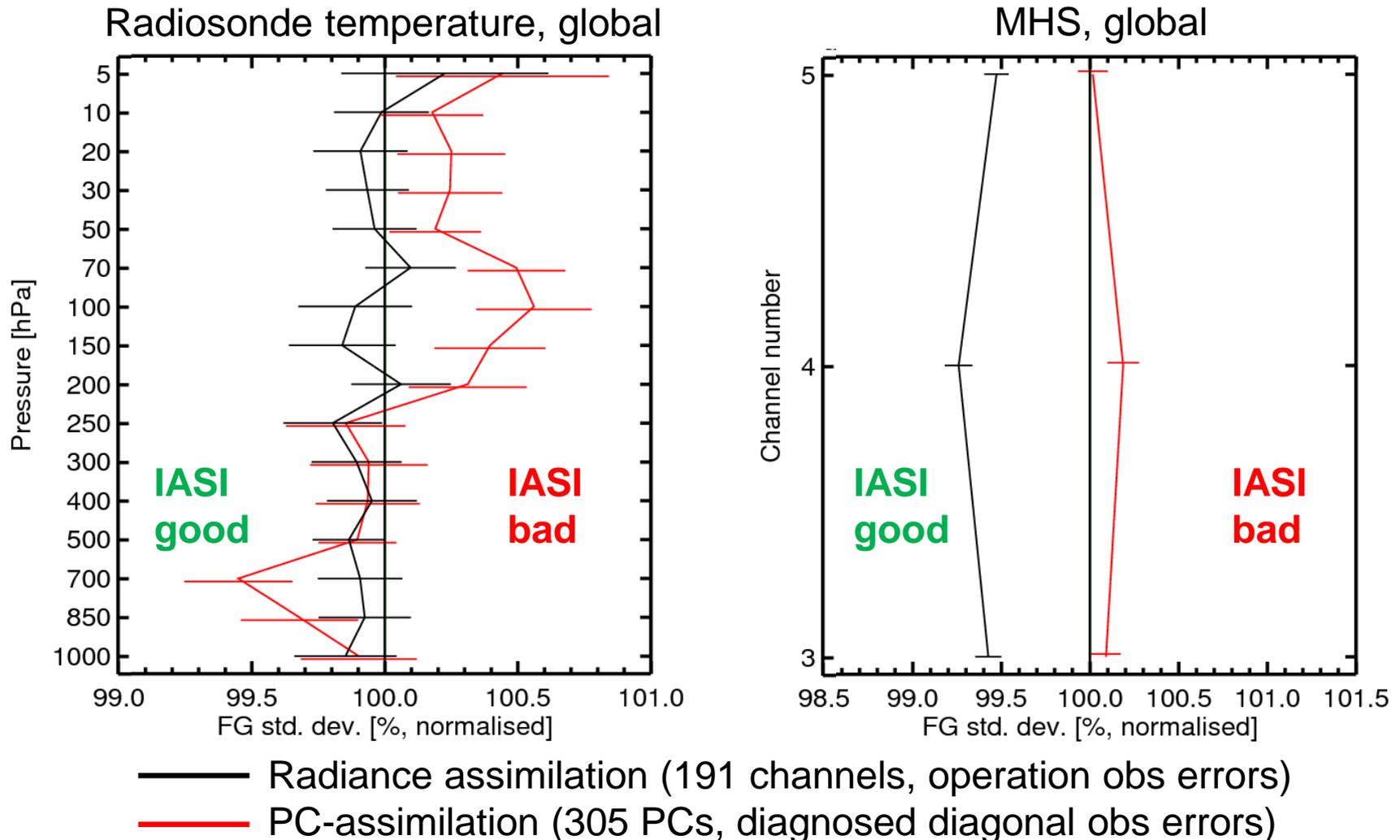
## PC assimilation, converted to radiance space



## Radiance assimilation



# Background departure statistics (normalised to no-IASI experiment)



# Summary

- **Diagnostics suggest F introduces error correlations for PCs as well as radiances.**
- **Observation error covariances diagnosed from the PC-assimilation and the radiance assimilation are qualitatively consistent.**
- **The diagonal observation error covariance used in the PC assimilation implies:**
  - **Some inter-channel error correlations when converted to radiance space,**
  - **with some of them qualitatively consistent with the diagnosed error correlations,**
  - **but with some spurious inter-channel error correlations (e.g., between stratospheric and humidity channels).**
- **There is scope for improved observation error specification for PC (and radiance) assimilation.**

# Assumed errors in PC-space (B1 only)

