

# Sequential data assimilation on high-performance computers with the Parallel Data Assimilation Framework PDAF

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# Overview

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- Sequential data assimilation
  - Ensemble-based Kalman filters
- Parallel Data Assimilation Framework PDAF
- Parallel performance of PDAF
- Application examples

# Sequential Data Assimilation

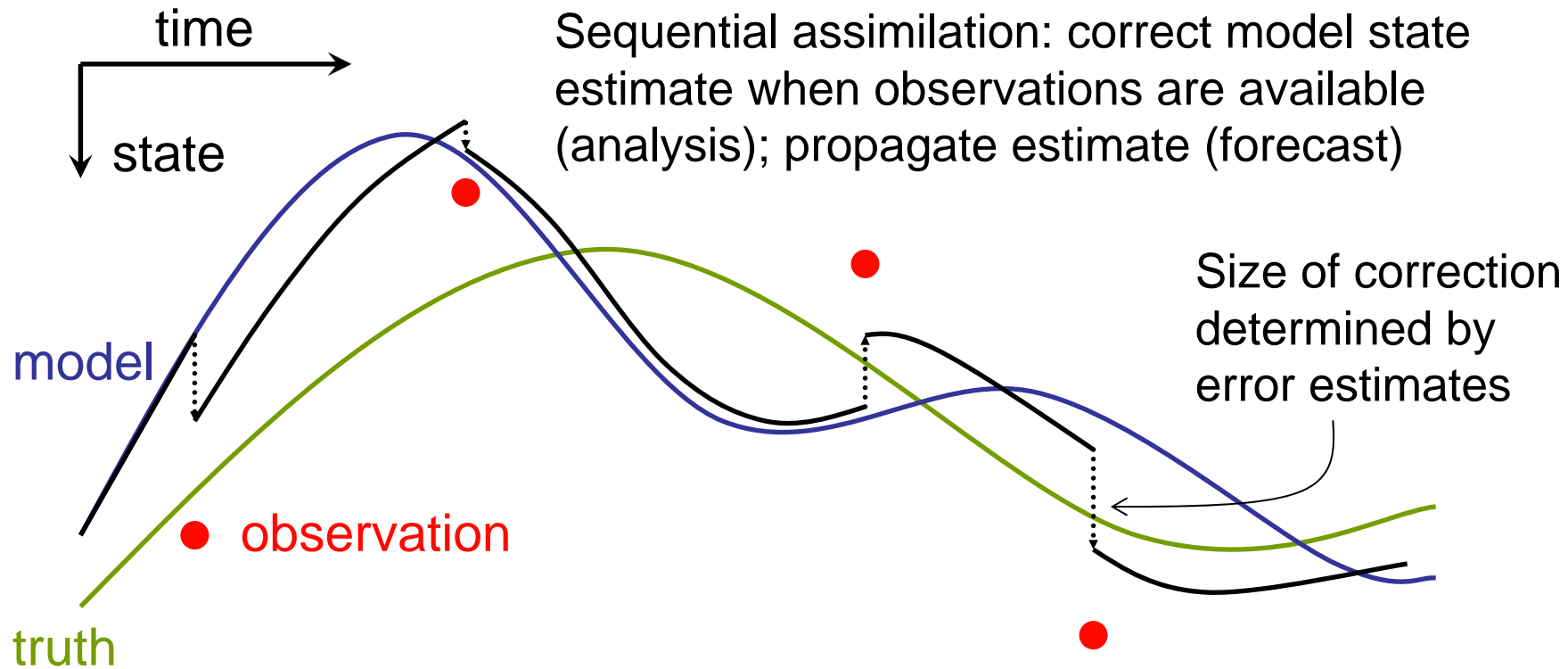
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# Data Assimilation

- Optimal estimation of system state:
  - initial conditions (for weather forecasts, ...)
  - trajectory (temperature, concentrations, ...)
  - parameters (growth of phytoplankton, ...)
  - fluxes (heat, primary production, ...)
  - boundary conditions and 'forcing'
  
- Characteristics of system:
  - high-dimensional numerical model -  $O(10^7)$
  - sparse observations
  - non-linear

# Sequential Data Assimilation

Consider some physical system (ocean, atmosphere,...)

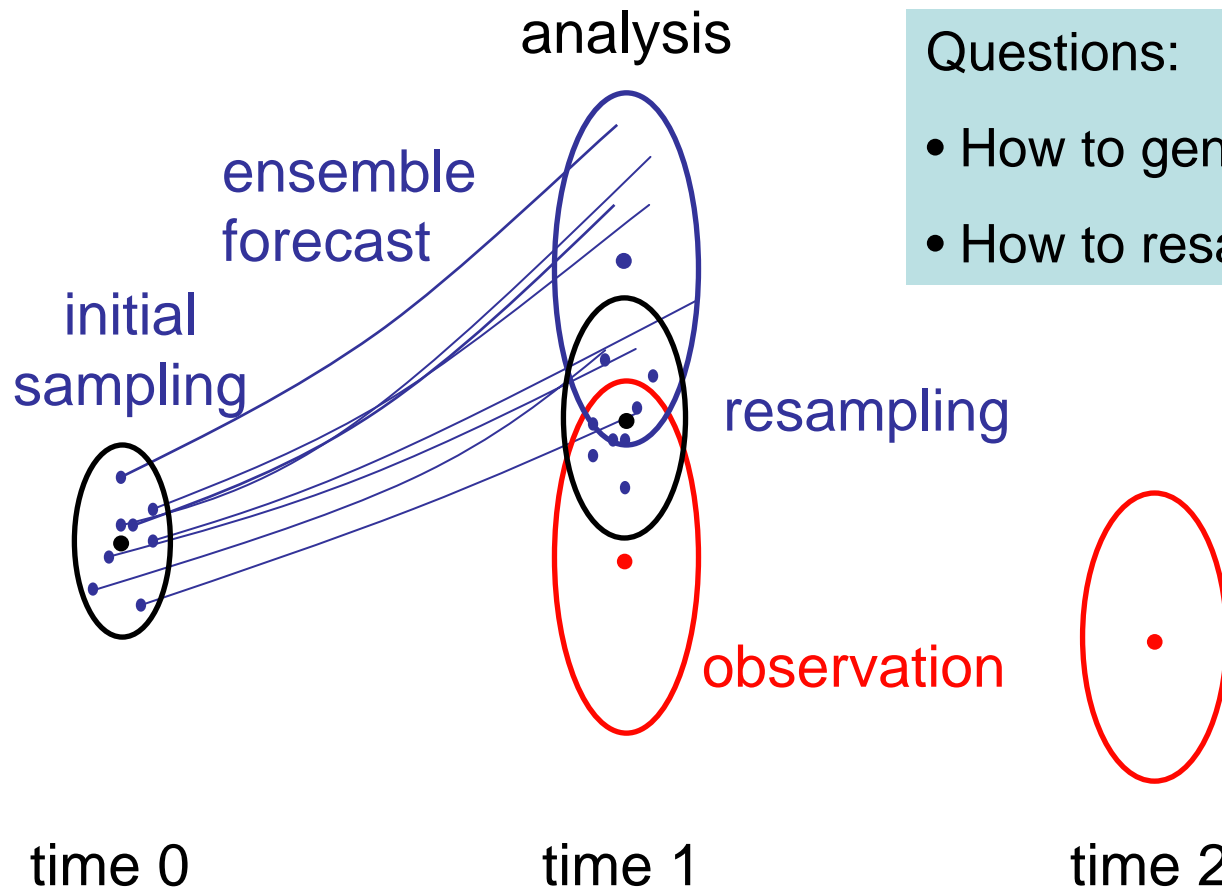


# Kalman Filters (Kalman, 1960)

- Optimal estimation problem
- Assume errors to be Gaussian distributed
  - Analysis is combination of two Gaussian distributions
  - Analysis is variance-minimizing
- Express problem in terms of mean state  $\mathbf{x}$  and state error covariance matrix  $\mathbf{P}$
- Propagate matrix  $\mathbf{P}$  by (linearized) model
- Issues:
  - Nonlinearity will not conserve Gaussianity
  - Storage of state covariance matrix can be unfeasible
  - Evolution of covariance matrix extremely costly
  - Reduce cost: simplify dynamics and/or approximate  $\mathbf{P}$

# Ensemble-based Kalman Filter

Approximate probability distributions by ensembles



Questions:

- How to generate initial ensemble?
- How to resample after analysis?

Some filters:

- EnKF (Evensen 1994)
- SEIK (Pham et al. 1998)
- ETKF, EAKF, ... (2001 - ...)

# Computational and Practical Issues

- Huge amount of memory required (model fields and ensemble matrix)
- Huge requirement of computing time (ensemble integrations)
- Natural parallelism of ensemble integration exists - but needs to be implemented
- Existing models often not prepared for data assimilation



# Parallel Data Assimilation Framework

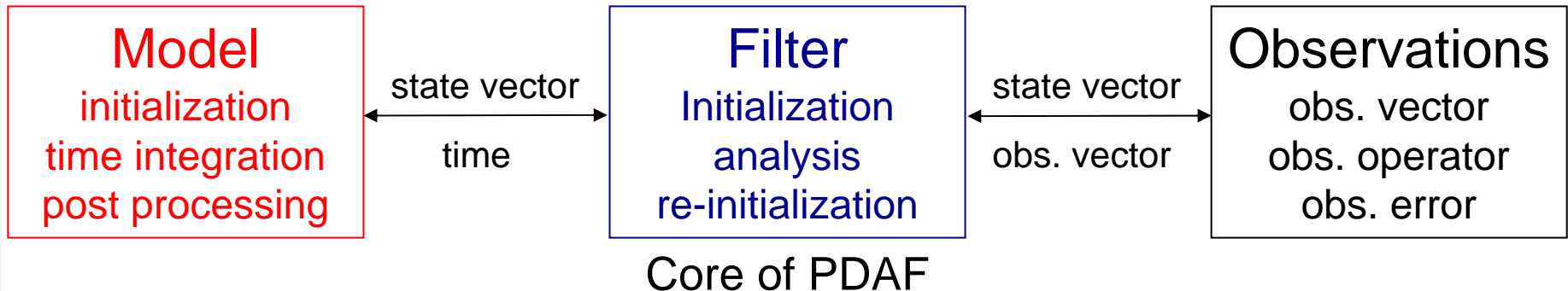
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# Motivation

- Parallelization of ensemble forecast can be implemented independently from model
- Filter algorithms can be implemented independently from model
  
- Goals
  - Simplify implementation of data assimilation systems based on existing models
  - Provide parallelization support for ensemble forecasts
  - Provide parallelized and optimized filter algorithms
  - Provide collection of „fixes“ for filters, which showed good performance in studies

# PDAF: Considerations for Implementation

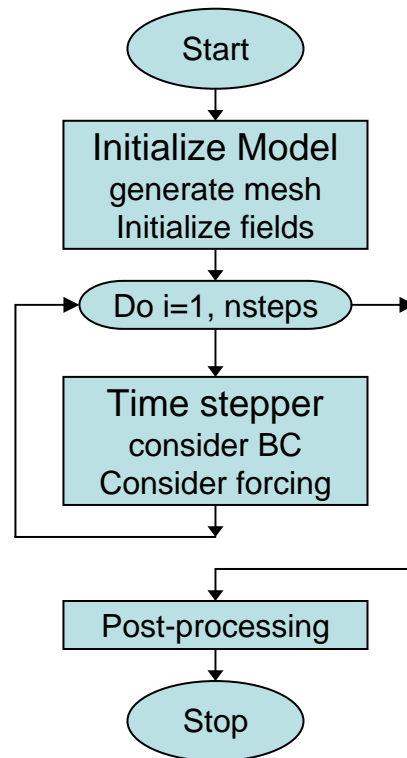
## Logical separation of problem



## Further considerations

- Combination of filter with model with minimal changes to model code
- Control of assimilation program coming from model
- Simple switching between different filters and data sets
- Complete parallelism in model, filter, and framework

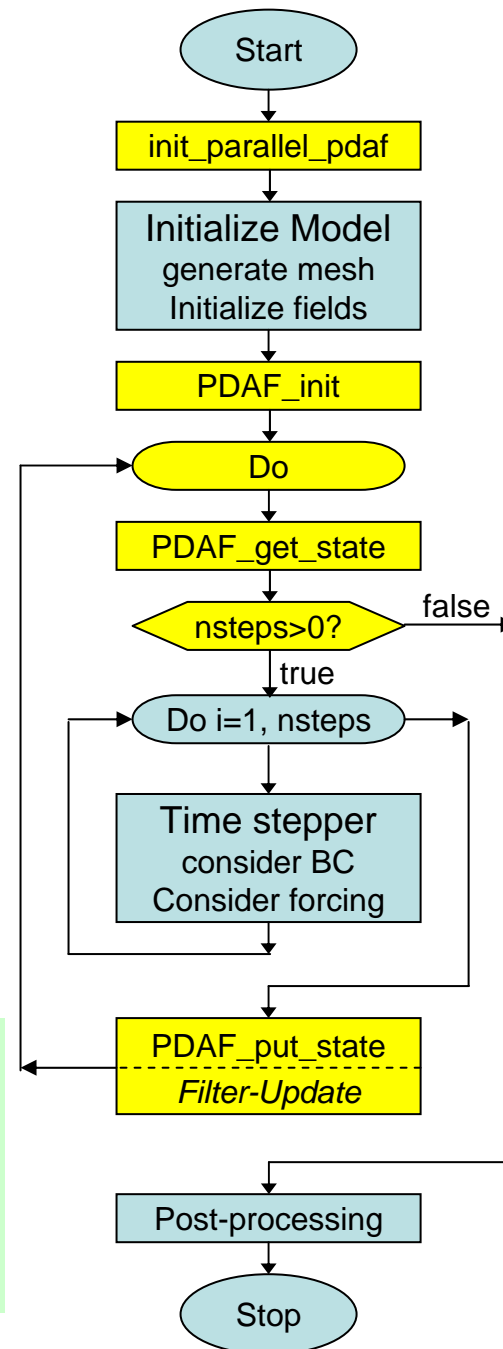
## Model



PDAF also has an offline-mode:

- Run forecasts with model
- Read model outputs, perform analysis & write restart files

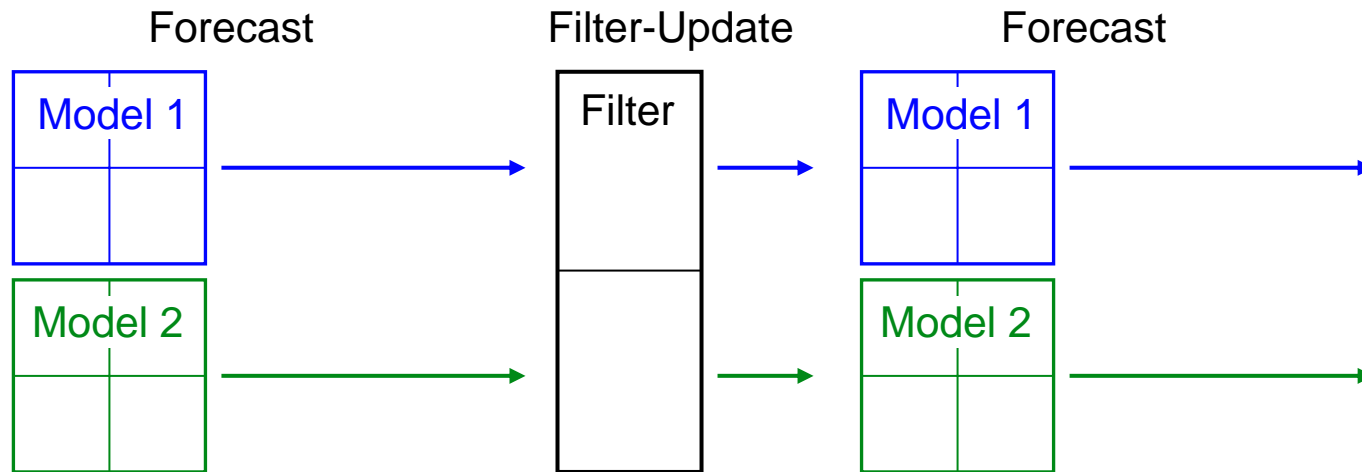
Extension for  
data assimilation



# PDAF interface structure

- Interface independent of filter  
(except for names of user-supplied subroutines)
- User-supplied routines for elementary operations:
  - field transformations between model and filter
  - observation-related operations
  - filter pre/post-step
- User supplied routines can be implemented as routines of the model  
(e.g. share common blocks or modules)

## 2-level Parallelism



1. Each model task can be parallelized
2. Multiple concurrent model tasks
  - Filter-update is parallel
  - 2 parallelization strategies:  
distribute ensemble members or state in sub-domains

# Current KF algorithms in PDAF

- Ensemble Kalman filter (EnKF, Evensen, 1994)
  - original ensemble-based KF
  - simplest formulation of ensemble-based KFs
- SEIK filter (Pham et al., 1998)
  - very efficient ensemble-based KF
- LSEIK filter (Nerger et al., 2006)
  - localized analyses for better filter performance
- SEEK filter (Pham et al., 1998)
  - explicit low-rank (error-subspace) formulation
  - linearized error forecast

# Parallel Performance of PDAF

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# Parallel performance of PDAF

- Performance tests on

SGI Altix ICE at HRLN (German “High performance computer north”)

nodes: 2 quad-core Intel Xeon Harpertown at 3.0GHz

network: 4x DDR Infiniband

compiler: Intel 10.1, MPI: MVAPICH2

- Ensemble forecasts

- are naturally parallel

- dominate computing time

  - E.g. parallel forecast over 10 days: 45s

    - SEIK with 16 ensemble members: 0.1s

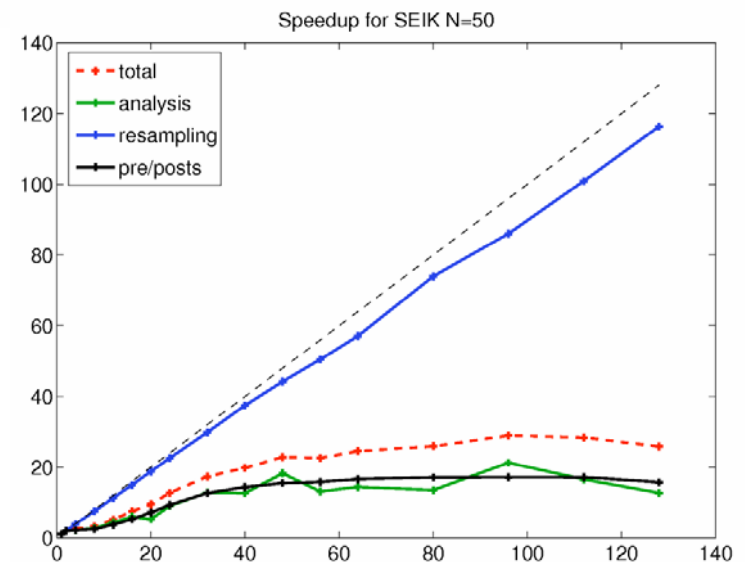
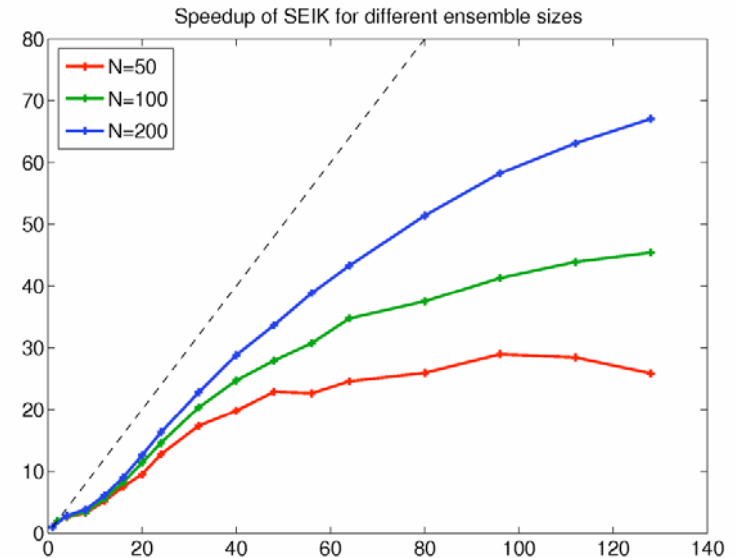
    - LSEIK with 16 ensemble members: 0.7s

- parallel efficiency near 1

# Speedup of SEIK with domain decomposition

- Test only assimilation without model dynamics
- SEIK performs global optimization
  - better speedup for larger ensembles
  - resampling is local, but no ideal speedup (MKL library?)
  - analysis and pre/poststep show very small speedup
    - behavior seems to be due to network latency of the machine used

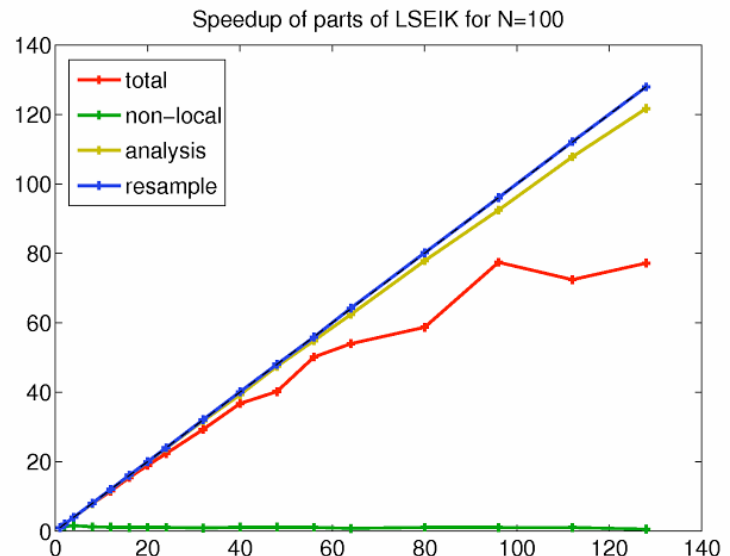
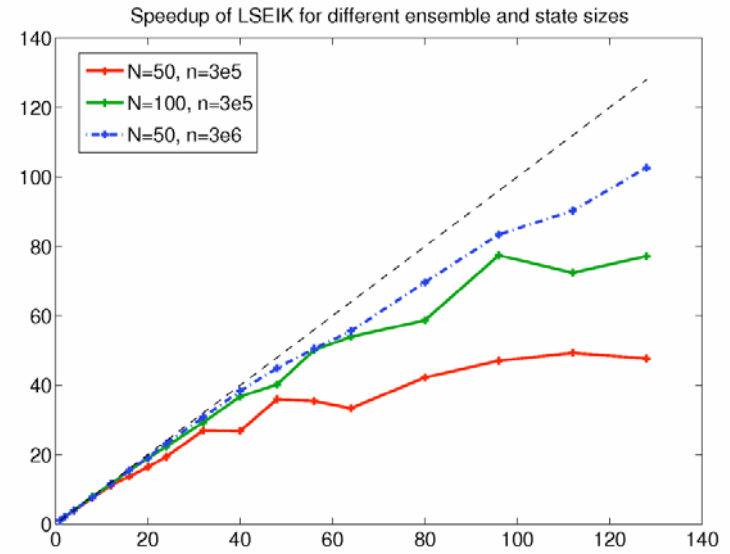
State dimension  $n = 3,000,000$   
Observations  $m = 30,000$   
Ensemble size  $N$



# Speedup of LSEIK with domain decomposition

- LSEIK performs sequence of local optimizations on sub-subdomains defined by influence radius for observations
  - near-ideal speedup for analysis step and resampling (ensemble transformation)
    - non-local gathering of observation-state residuals
    - pre/poststep
- total speedup is limited by

State dimension  $n = 300,000$   
Observations  $m = 30,000$   
Ensemble size  $N$



# Application examples

- Assimilation of satellite altimetry  
(Project Tandem, @ AWI T. Janjic Pfander)
  - with finite element ocean model FEOM
  - utilize information from tandem mission of Topex/Poseidon and Jason 1
- Ocean chlorophyll assimilation into global NASA Ocean Biogeochemical Model (with Watson Gregg, NASA GSFC)
  - Generation of daily re-analysis maps of chlorophyll at ocean surface
- Coastal assimilation of ocean surface temperature  
(within project “DeMarine Environment”, AWI and BSH)
  - Improve operational forecast skill, e.g. for storm surges

## PDAF is available!

- With a restricted GPL-license
- Upon request (not yet downloadable ☹)
- Mail me (Lars.Nerger@awi.de)
- Go to

**[www.awi.de/en/go/pdaf](http://www.awi.de/en/go/pdaf)**

to get contact information

- Distributed is the source code of PDAF together with an example implementation

# Requirements

- Fortran compiler (gfortran works!)
  - MPI (OpenMPI works!)
  - BLAS & LAPACK
  - make
- 
- I don't have a Matlab version!

# Summary

- Sequential data assimilation is not serial
  - ⇒ Mixed parallel efficiency of ensemble-based Kalman filtering (forecasts & analysis/resampling)
- Parallel Data Assimilation Framework PDAF
  - Simplified implementation of assimilation systems
  - Flexibility: Different assimilation algorithms and data configurations within one executable
  - Full utilization of parallelism in models and filters
  - Available upon request

**Thank you!**

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